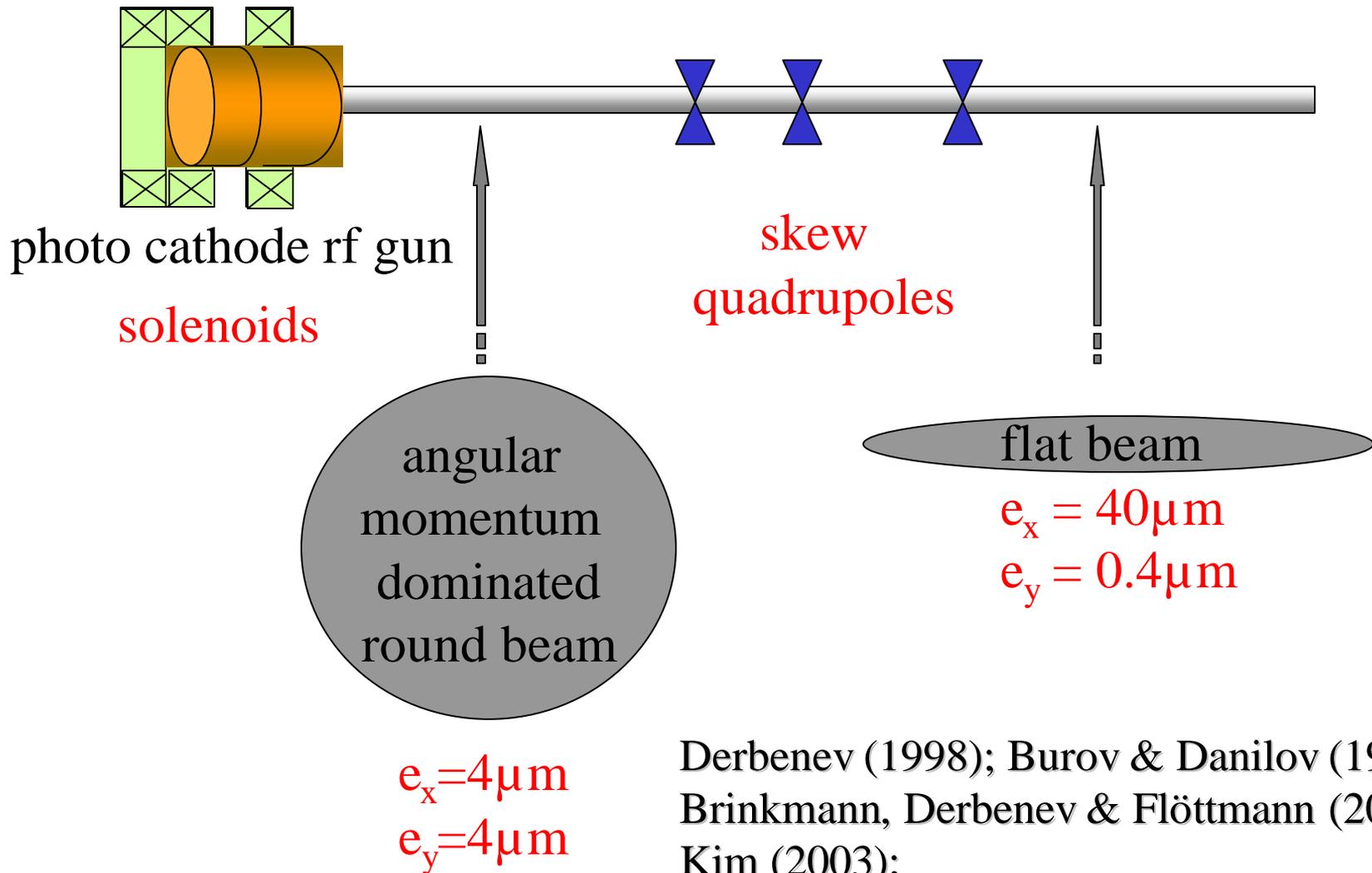

Photoinjector Production of Flat Electron Beams

Yin-e Sun

University of Chicago

the short story

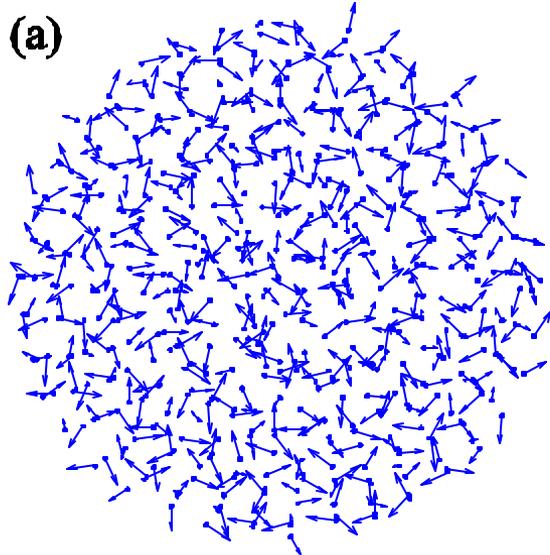


Derbenev (1998); Burov & Danilov (1998);
Brinkmann, Derbenev & Flöttmann (2001);
Kim (2003);

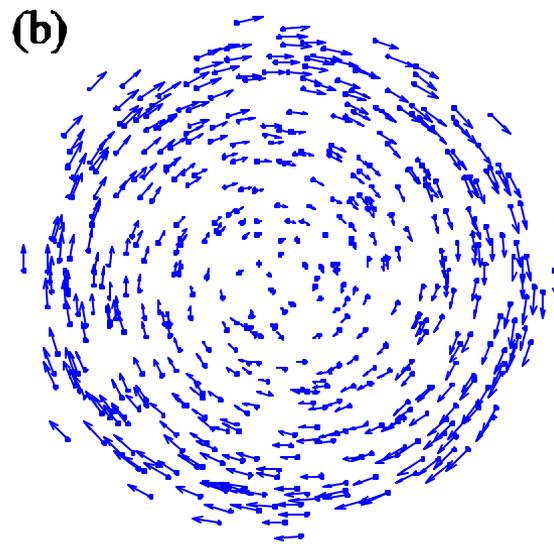
Outline

- angular-momentum-dominated electron beams;
- production and measurements of angular-momentum-dominated beam;
- removal of the angular momentum and generation of flat beam:
 - theory;
 - measurement method;
 - data analysis and results;
 - comparison with simulations;
- conclusions.

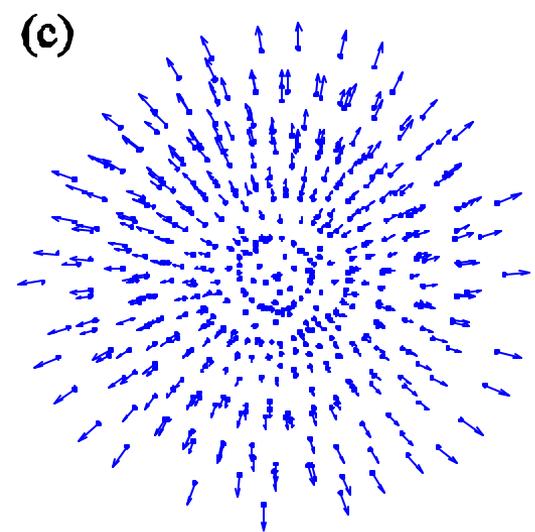
Beam dynamics: three different regimes



emittance



canonical angular momentum



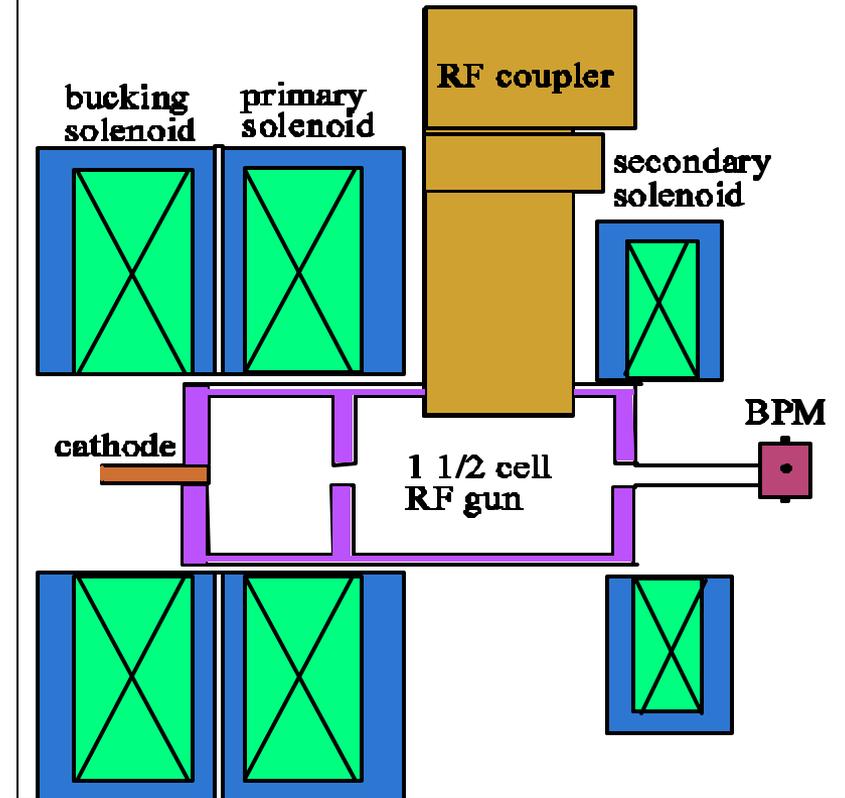
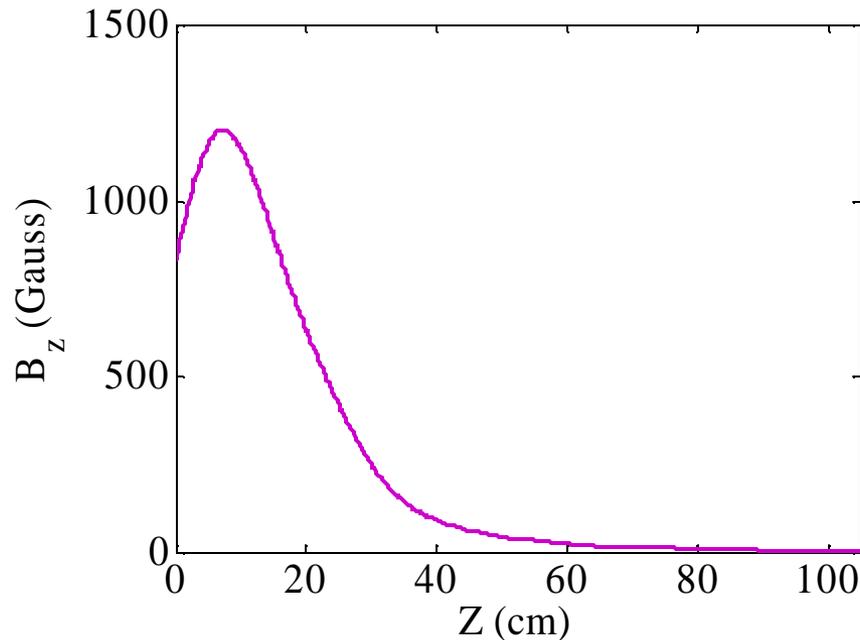
space charge

envelope equation in a drift: $\mathbf{s}'' - \frac{\mathbf{e}^2}{\mathbf{s}^3} - \frac{L^2}{\mathbf{s}^3} - \frac{K}{4\mathbf{s}} = 0$ where $K = \frac{2I}{I_0 b^3 g^3}$.

Generation of angular momentum dominated e⁻ beam

$$L = \mathbf{g}m\mathbf{r}^2\dot{\mathbf{f}} + \frac{1}{2}eB_z r^2$$

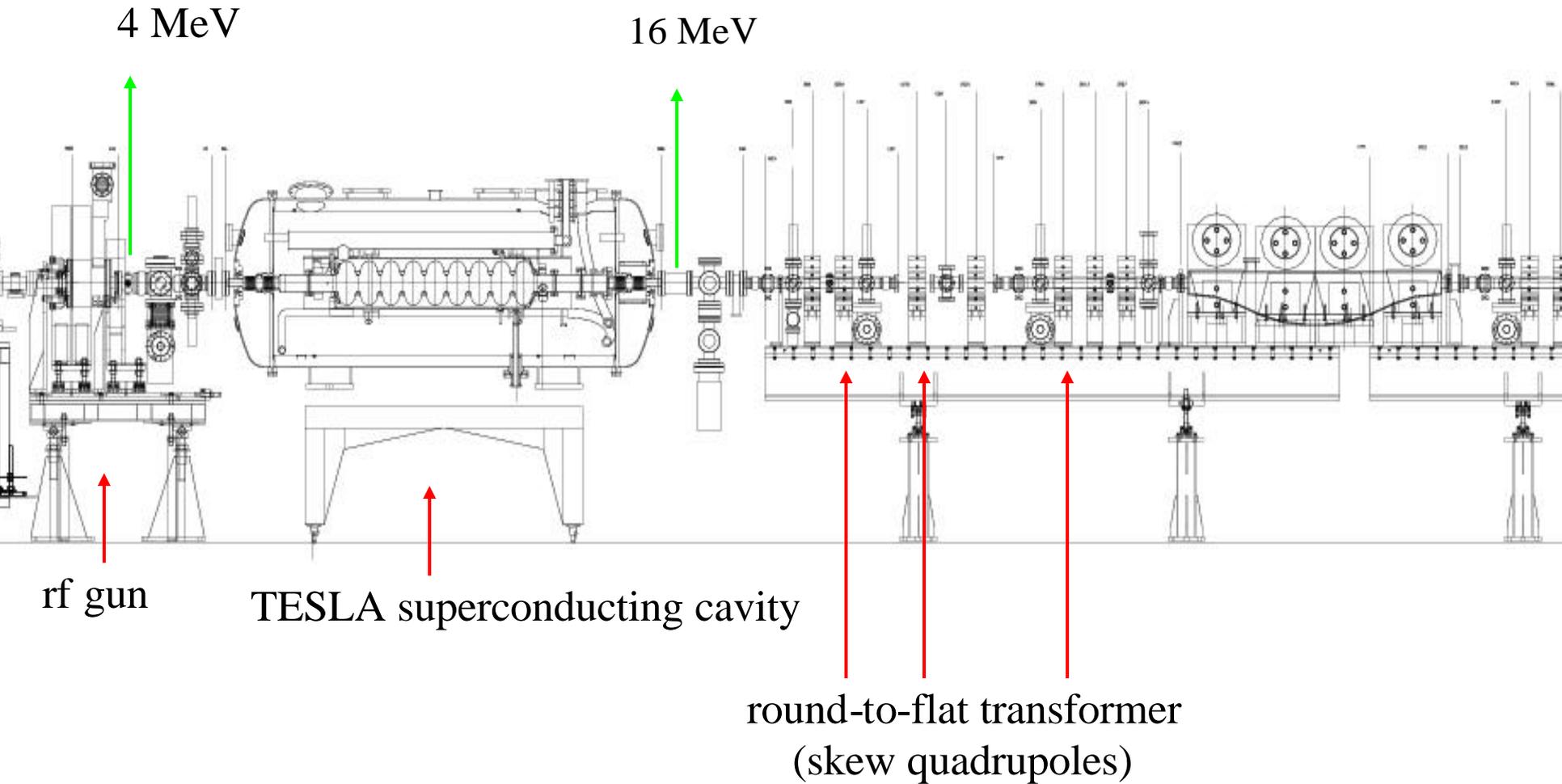
On the photocathode: $\langle L \rangle = eB_0 S_c^2$



FNPL 1.625-cell RF gun, 1.3 GHz

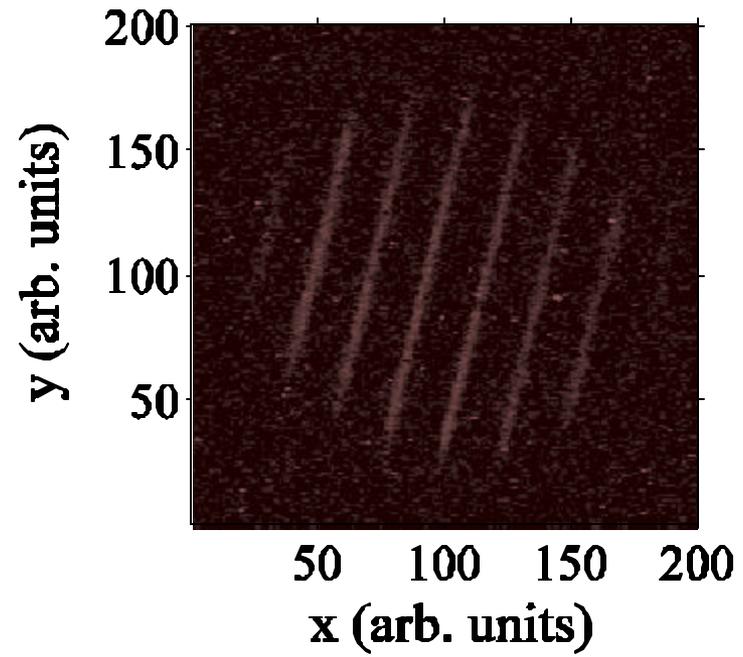
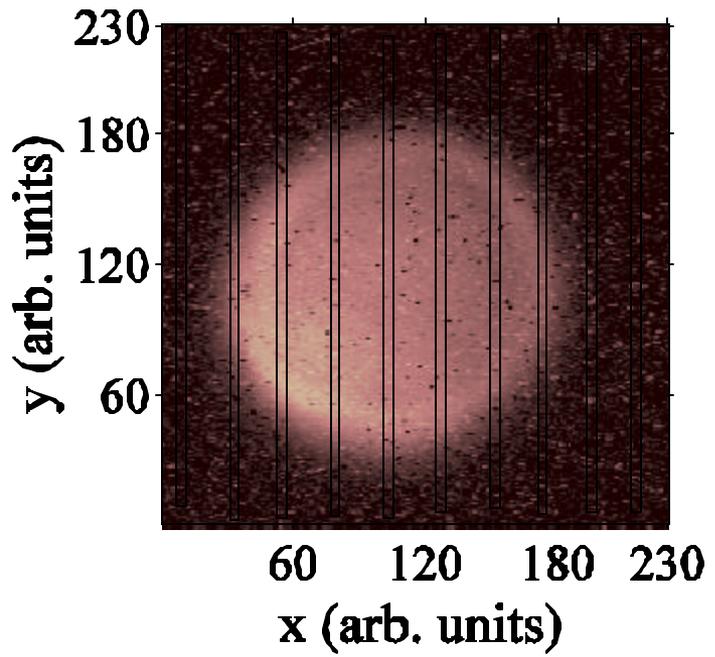
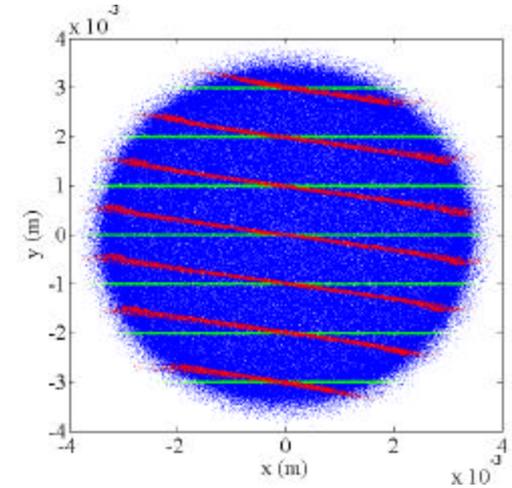
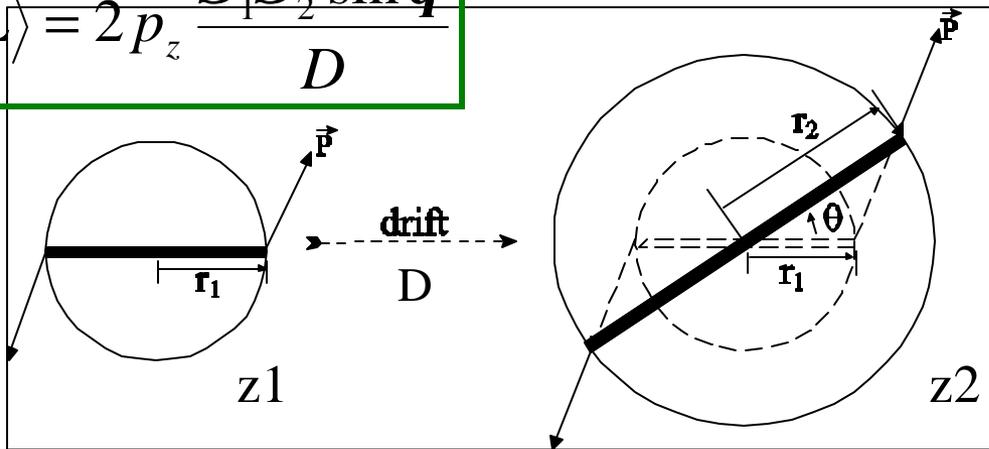
Solenoidal end field applies a torque to the beam. When $B_z=0$, canonical = mechanical angular momentum

Fermilab/NICADD Photoinjector Lab. (FNPL)



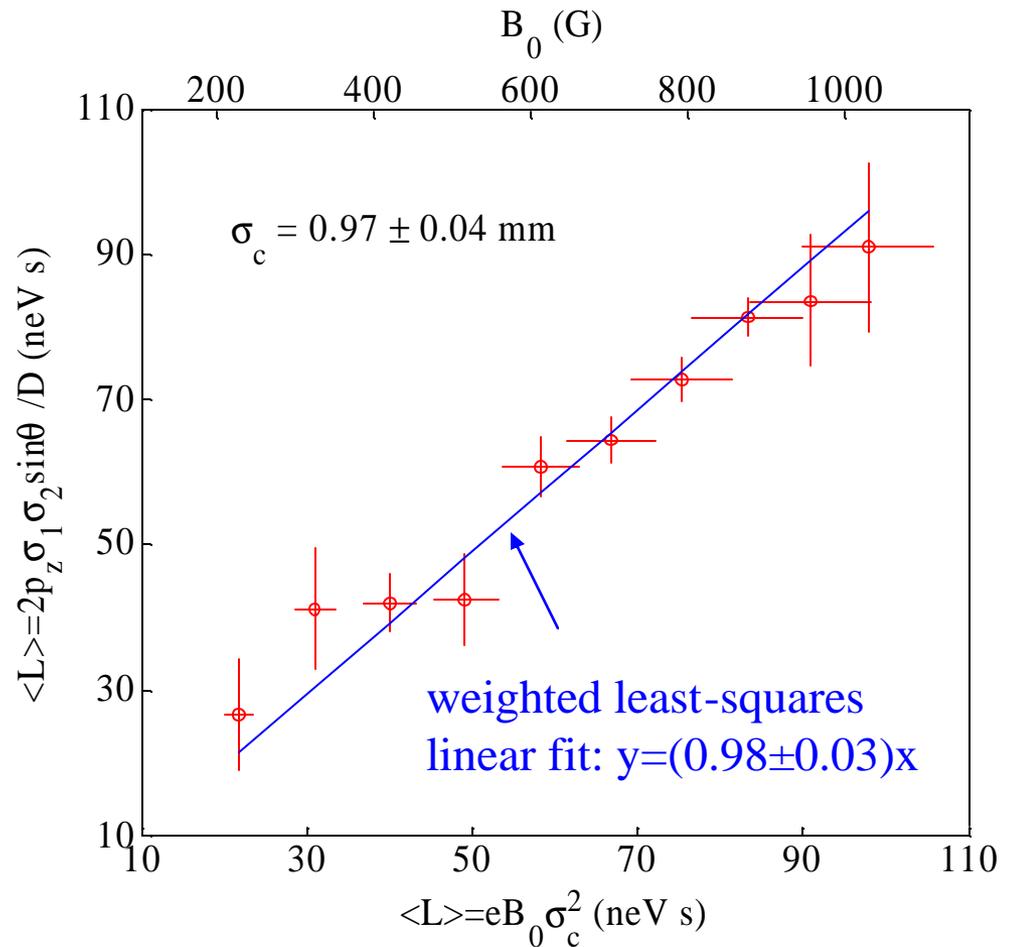
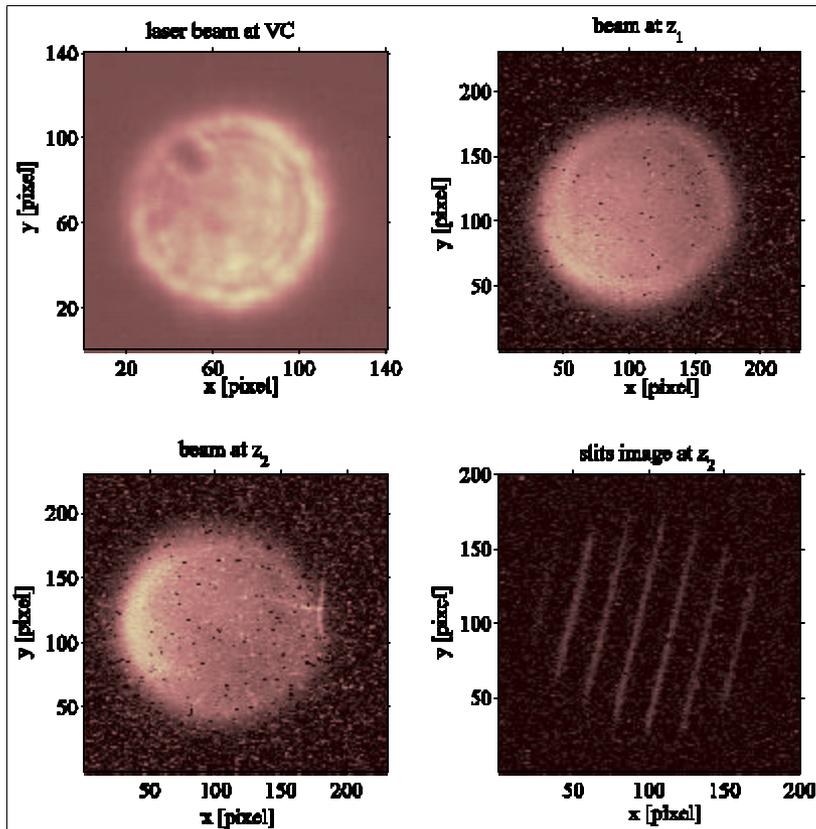
Measurement of mechanical angular momentum in a drift space

$$\langle L \rangle = 2 p_z \frac{\mathbf{s}_1 \mathbf{s}_2 \sin q}{D}$$



Demonstration of conservation of canonical angular momentum

as a function of magnetic field on cathode



Round-to-flat beam transformation

$$\Sigma_{round} = \begin{bmatrix} \mathbf{e}_{eff} \mathbf{b} & 0 & 0 & L \\ 0 & \mathbf{e}_{eff} / \mathbf{b} & -L & 0 \\ 0 & -L & \mathbf{e}_{eff} \mathbf{b} & 0 \\ L & 0 & 0 & \mathbf{e}_{eff} / \mathbf{b} \end{bmatrix}$$

General form of a round beam at beam waist location

(K.-J. Kim)

$$e_{eff} = \sqrt{\mathbf{e}_u^2 + L^2}$$

uncorrelated emittance

“normalized” canonical angular momentum

$$\Sigma_{flat} = M \Sigma_{round} \tilde{M}$$

Transfer matrix of the round-to-flat beam transformer

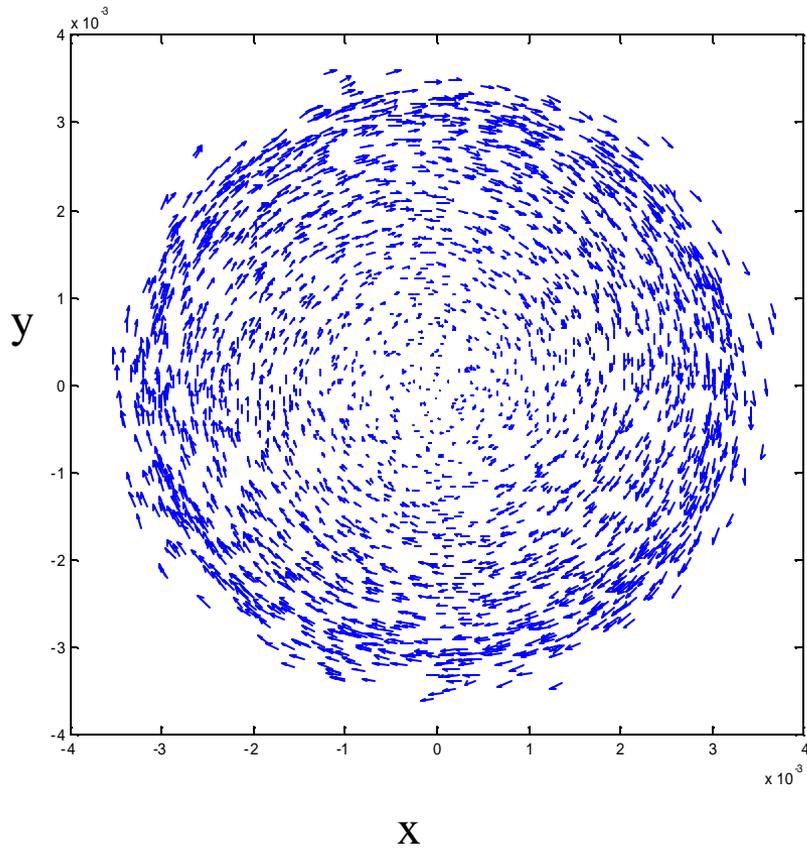
$$\Sigma_{flat} = \begin{bmatrix} \mathbf{e}_- \mathbf{b} & 0 & 0 & 0 \\ 0 & \mathbf{e}_- / \mathbf{b} & 0 & 0 \\ 0 & 0 & \mathbf{e}_+ \mathbf{b} & 0 \\ 0 & 0 & 0 & \mathbf{e}_+ / \mathbf{b} \end{bmatrix}$$

Flat beam emittances given by:

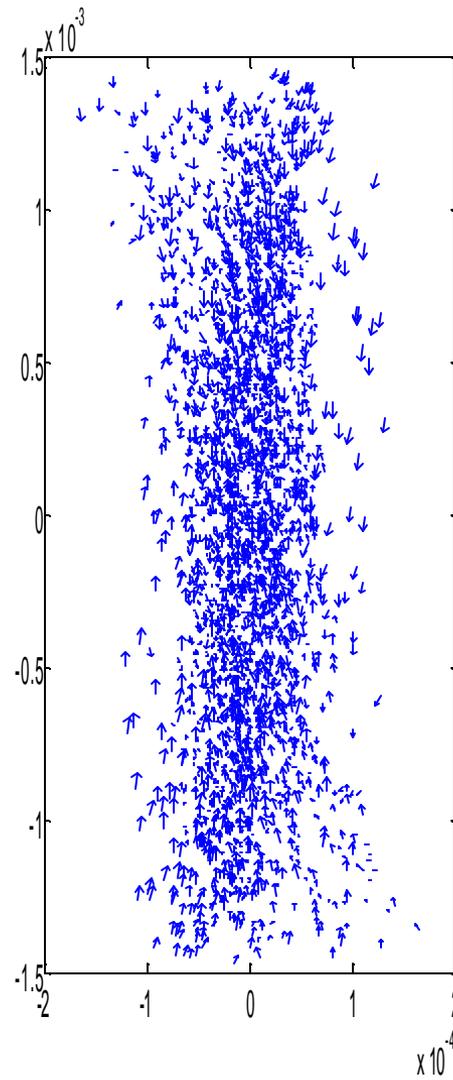
$$\mathbf{e}_{\pm} = \sqrt{\mathbf{e}_u^2 + L^2} \pm L$$

e.g. $L=20$ mm mrad, $\mathbf{e}_u=4$ mm mrad
 $\mathbf{e}_+=40$ mm mrad; $\mathbf{e}_-=0.4$ mm mrad

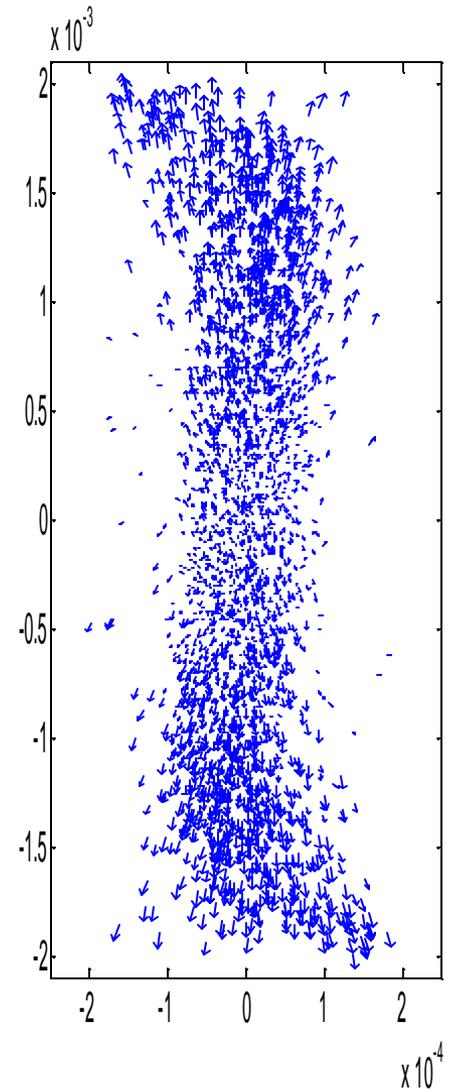
Position and velocity snapshots at the entrance/exit of the transformer



Round beam



flat beam

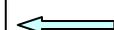
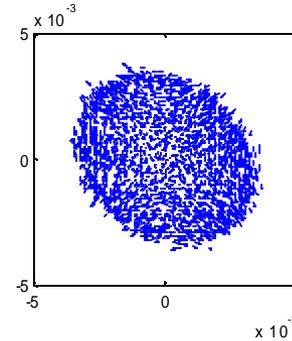
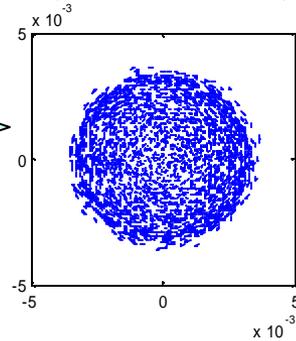


Beam evolution through the transformer for the first solution

10 mm

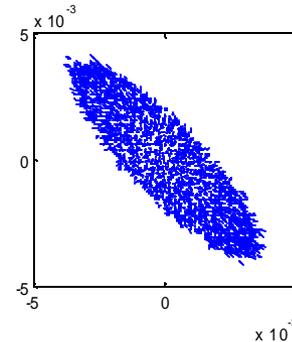
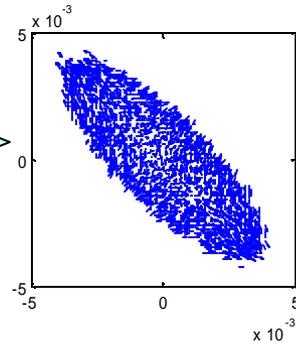


Right before 1st quad



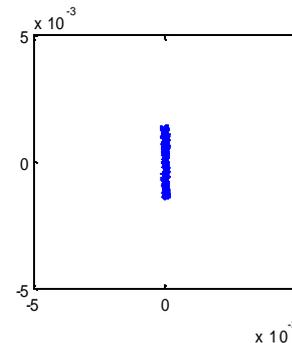
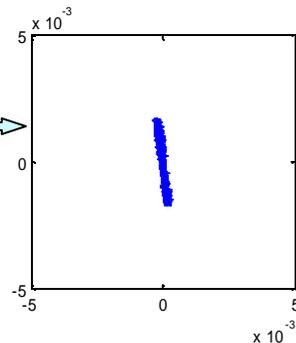
Right after 1st quad

Right before 2nd Quad



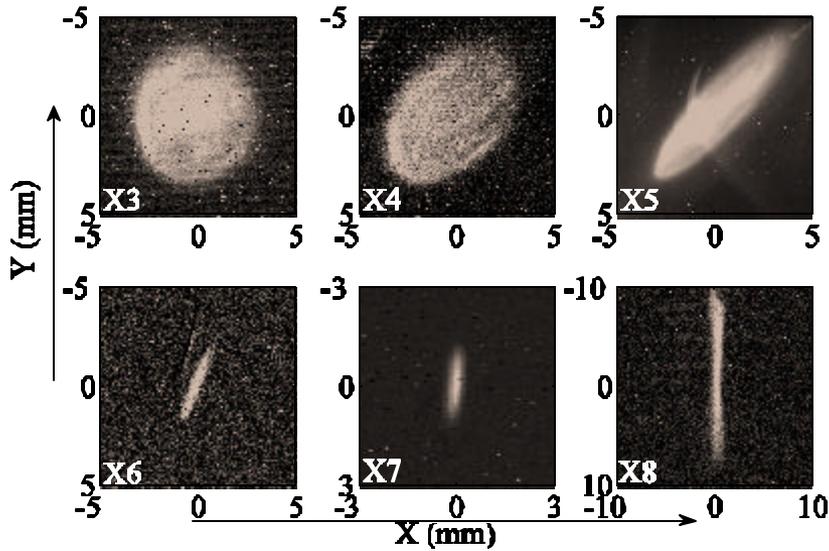
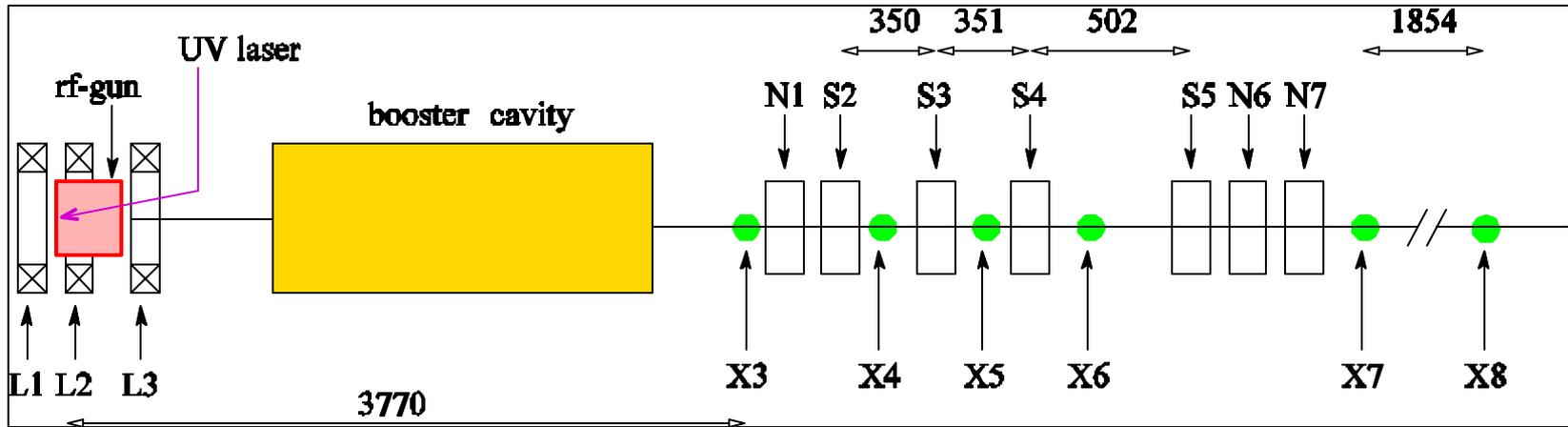
Right after 2nd Quad

Right before 3rd quad

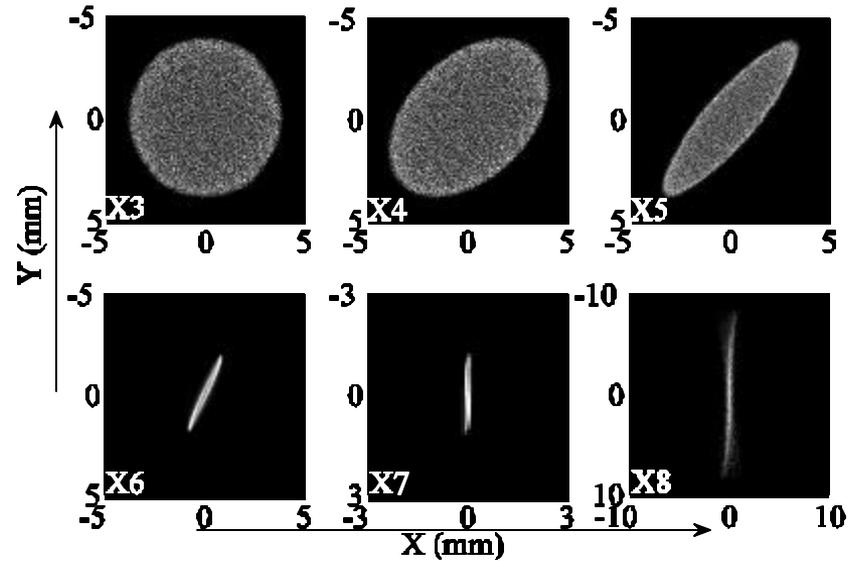


Right after 3rd quad

Removal of angular momentum and generating a flat beam



experiment



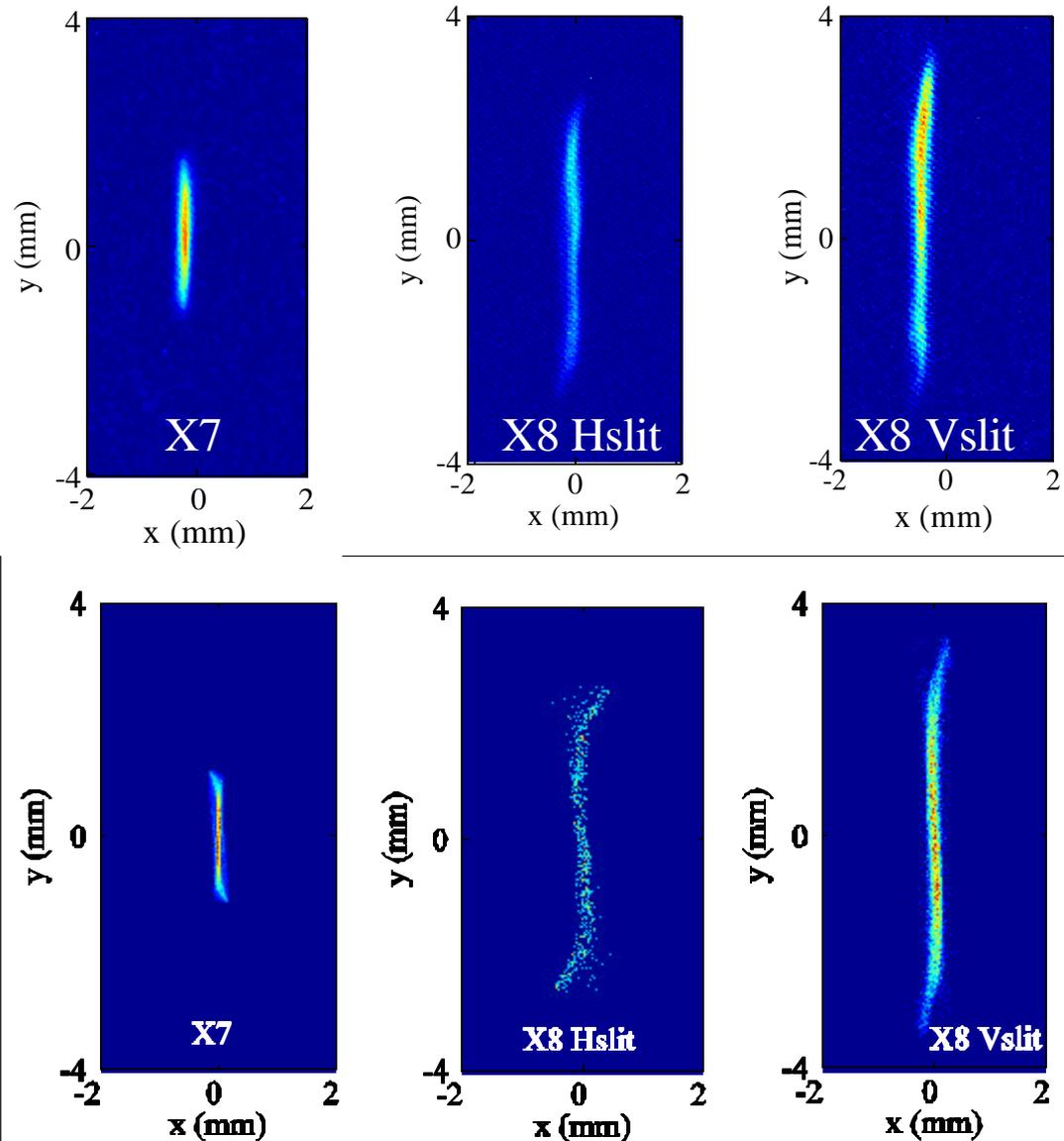
simulation

Flat-beam experiment

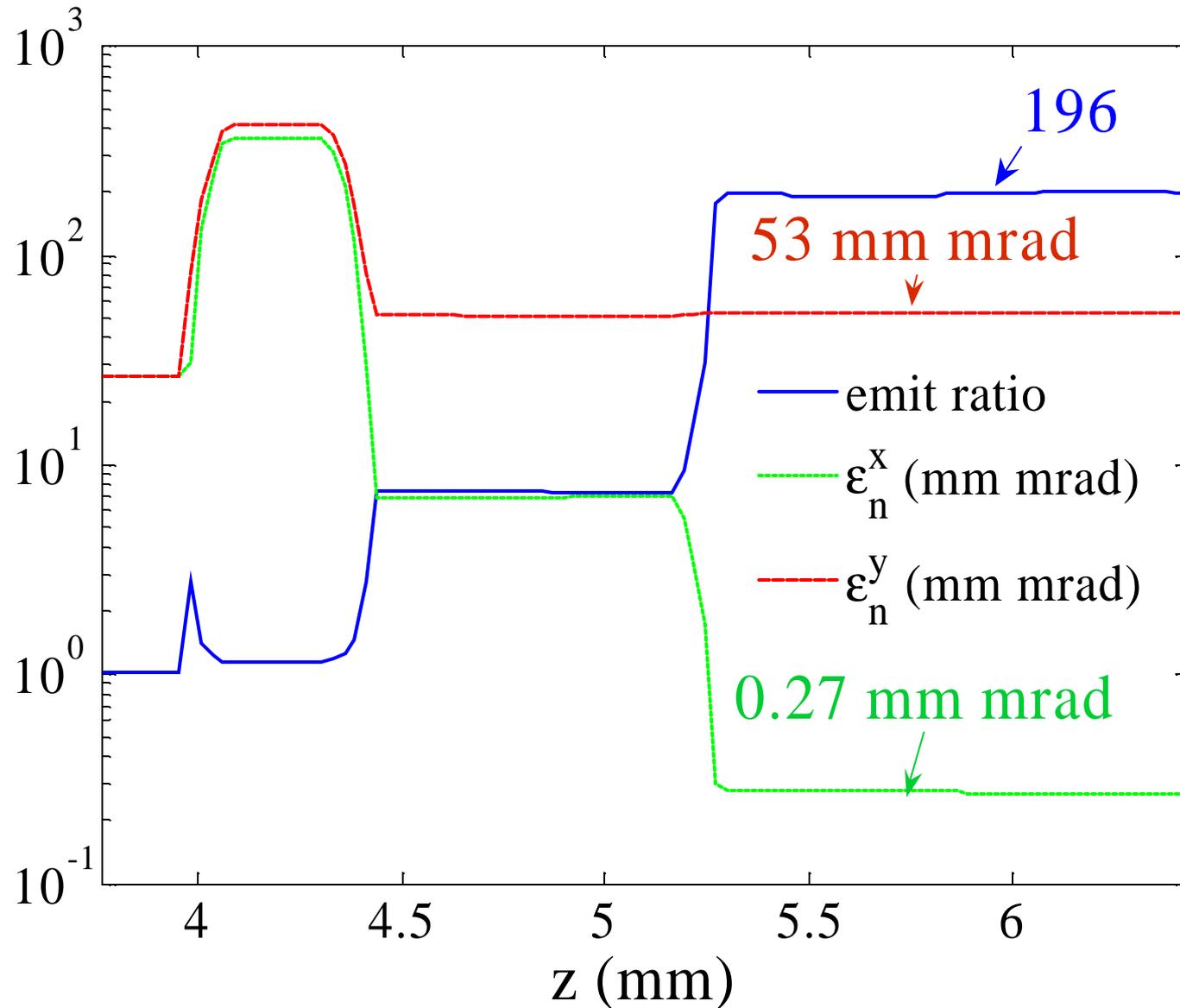
Solenoid setting:
main=195A,
buck=0A,
secondary=75A

Laser $s = 0.97$ mm
 $s_t = 3$ ps

$E = 15.8$ MeV
 $Q = 0.50 \pm 0.05$ nC



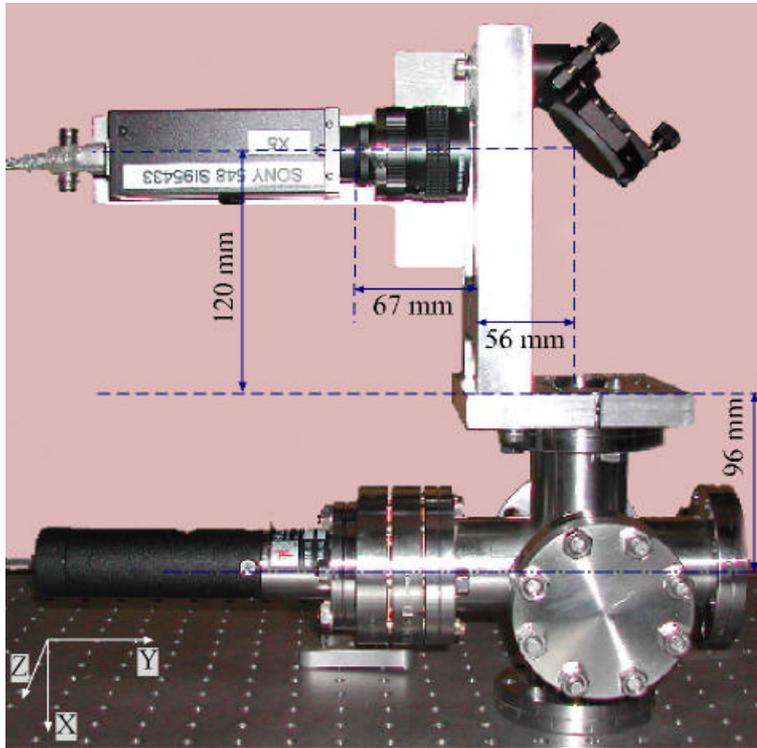
ASTRA Simulation with experimental conditions



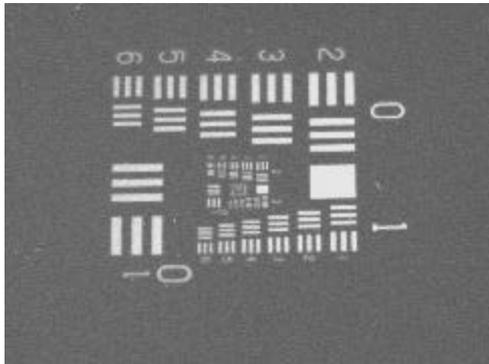
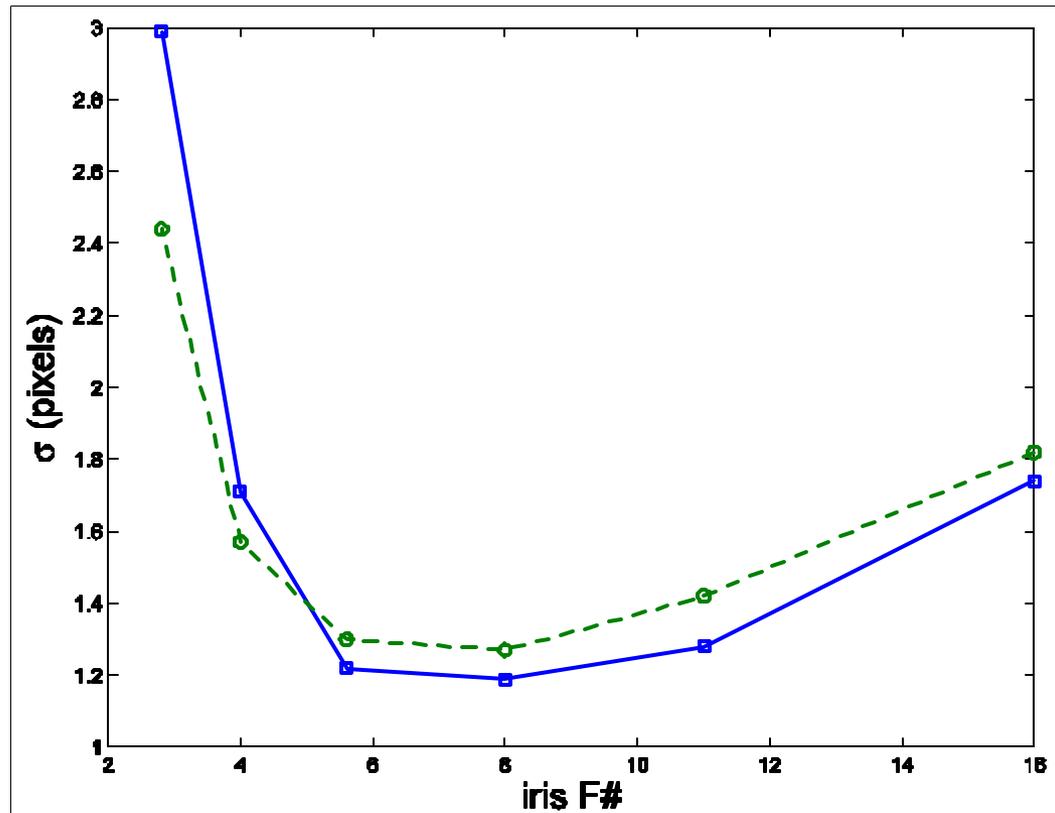
Compare measurement with simulation

	Experiment		Simulation
	90%	95%	(ASTRA)
rms_cathode(mm)		0.97	0.97
B_cathode(Gauss)		898	898
I_Quad1 (A)		-1.97	-1.98
I_Quad2 (A)		2.56	2.58
I_Quad3 (A)		-4.55	-5.08
rms_X7y (mm)	0.58±0.01	0.63±0.01	0.77
rms_X7x (mm)	0.084±0.001	0.095±0.001	0.058
rms_X8_hslit (mm)	1.57±0.01	1.68±0.01	1.50
rms_X8_vslit (mm)	0.12±0.01	0.13±0.01	0.11
Lcath (mm mrad)		24.5±0.7	
Lmech (mm mrad)		26.6±0.5	
Emit-uncorrelated (mm mrad)		5.1±0.7	
e ₊ (mm mrad)		53.8±0.9	
e ₋ (mm mrad)		0.49±0.13	
ex (mm mrad)	<u>0.39±0.02</u>	<u>0.49±0.02</u>	<u>0.27</u>
ey (mm mrad)	35.2±0.5	41.0±0.5	53
ey/ex	90±5	83±4	196
(ex · ey) ^{0.5}	3.7	4.5	3.8 mm mrad

Camera resolution



Calibration: $29 \mu\text{m}/\text{pixel}$
Resolution: $[35 \sim 50] \mu\text{m}$



Upper limit of the “true” flat beam emittances

$$\mathbf{S}_0 = \sqrt{\mathbf{S}^2 - \mathbf{S}_{res}^2}$$

upper limit of
true rms size

directly
measured

best measured
camera resolution

	90%	95%
rms_X7y (mm)	0.58±0.01	0.63±0.01
rms_X7x (mm)	0.076±0.001	0.088±0.001
rms_X8_hslit (mm)	1.57±0.01	1.68±0.01
rms_X8_vslit (mm)	0.11±0.01	0.11±0.01
e _x (mm mrad)	<u>0.32±0.02</u>	<u>0.41±0.02</u>
e _y (mm mrad)	35.2±0.5	41.0±0.5
e _y /e _x	<u>110±7</u>	<u>100±5</u>
$\sqrt{\mathbf{e}_x \mathbf{e}_y}$ (mm mrad)	3.35	4.1

summary

- experimental investigation of angular-momentum-dominated electron beams was carried out.
- The result of flat-beam emittance measurements:
 - at 0.5 nC, normalized emittance of **0.4 mm mrad** was measured;
 - emittance ratio of **100** was achieved.

acknowledgements

Univ. of Chicago
Kwang-je Kim

FNPL:

flat beam: Helen Edwards, Don Edwards, Philippe Piot

laser: Jianliang Li, Rodion Tikhoplav, Jamie Santucci, Nick Barov

vacuum: Wade Muranyi, Brian Degraff, Mike Heinz, Rocky Rauchmiller

rf: Markus hüning, Peter Prieto, Rene Padilla, John Reid, Tim Berenc

controls: Mike Kucera, Jason Wennerberg

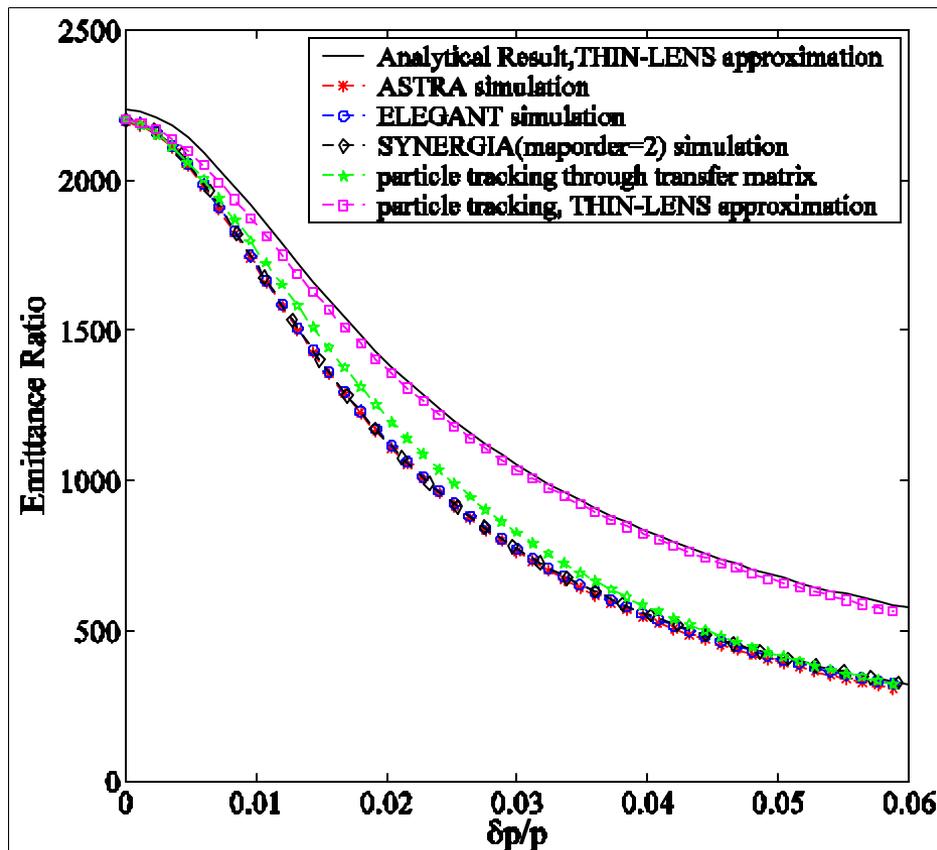
Collaborating institutes:

Court Bohn (NIU), Klaus Flöttmann (DESY), Steve Lidia (LBNL)

Chromatic effects

q? $q_0(1 - \delta + \delta^2)$, transfer matrix? $M(q_1, q_2, q_3, d_2, d_3) \approx M_0 + \delta\Delta_1 + \delta^2\Delta_2$,

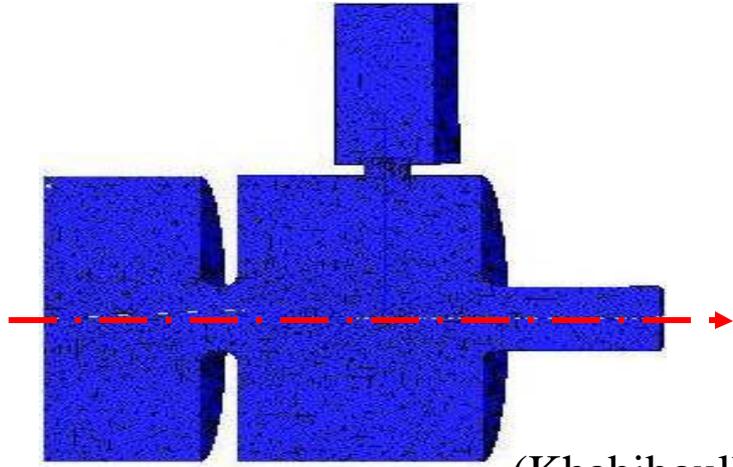
$$\varepsilon_{x,y} = \sqrt{(\varepsilon_{eff} \mp \mathcal{L})^2 + \langle \delta^2 \rangle^2 [|\Delta_{11 \text{ or } 22}| + (\varepsilon_{eff} \mp \mathcal{L})^2 \text{Tr}(T \Delta_{11 \text{ or } 22}^\dagger)]}.$$



thermal emittance = 1 mm
mrad.

space charge force is turned
off.

RF asymmetry caused by gun RF coupler kick

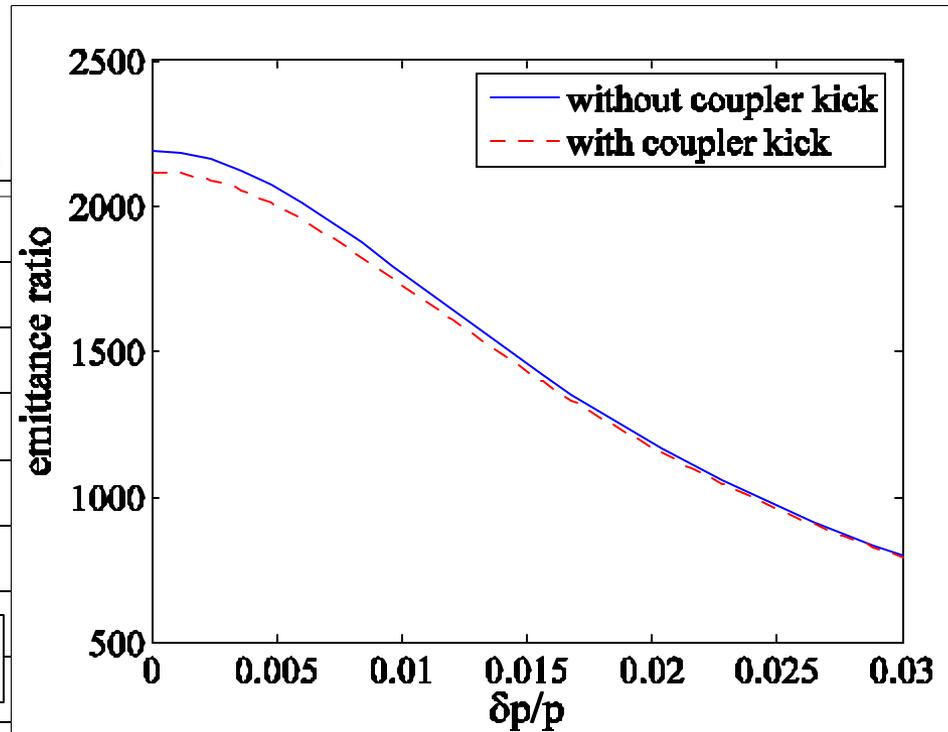
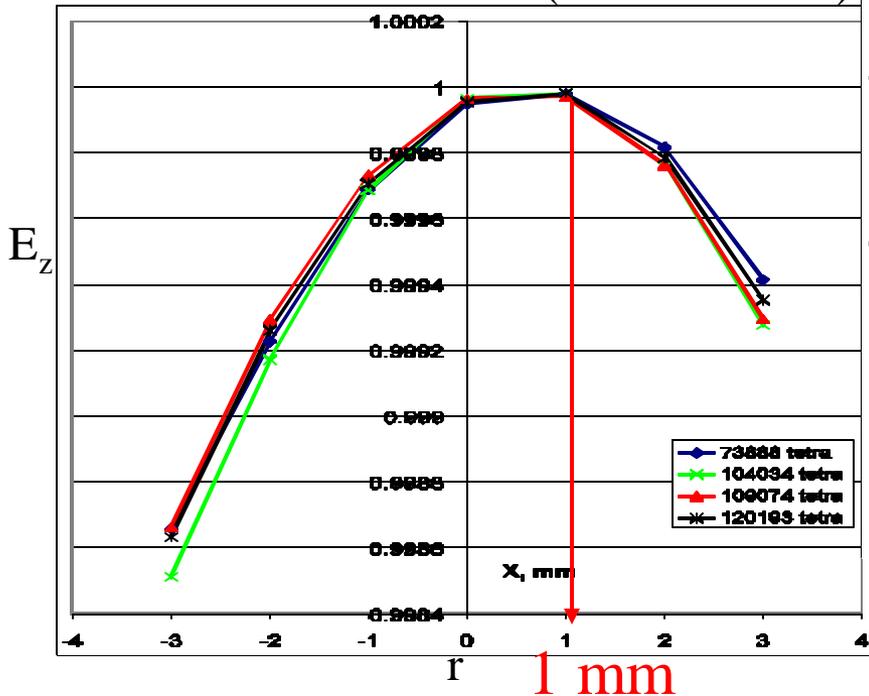


(Khabiboulline)

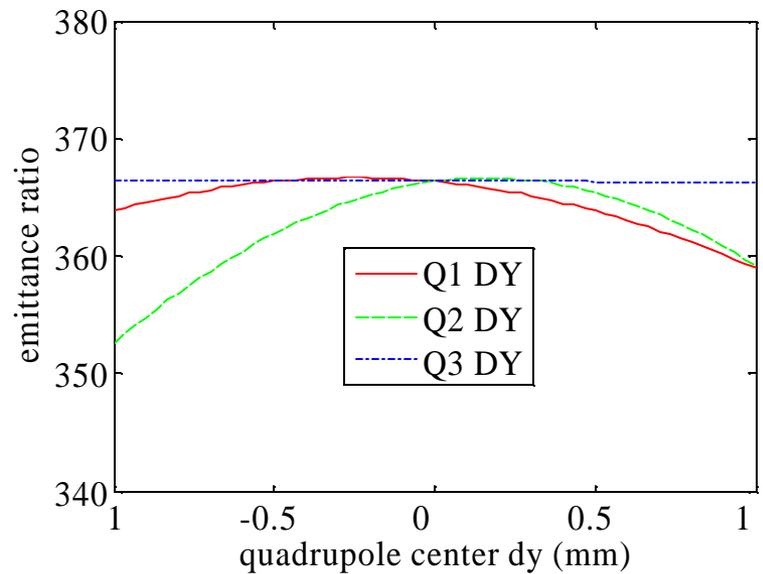
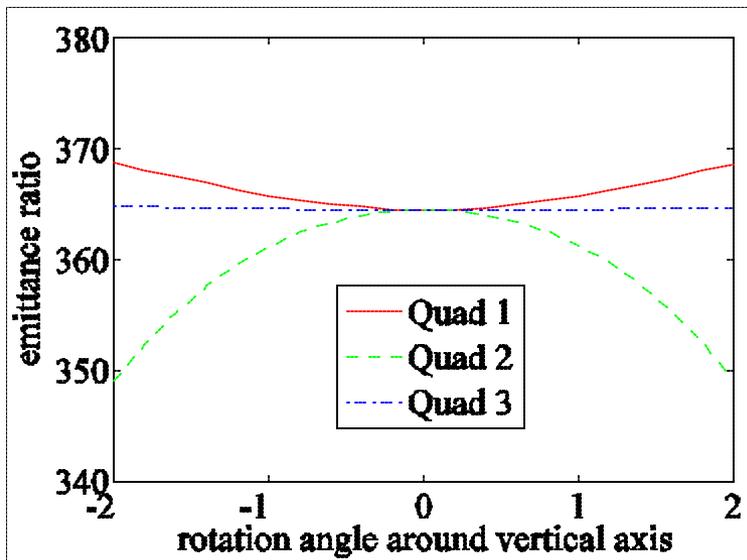
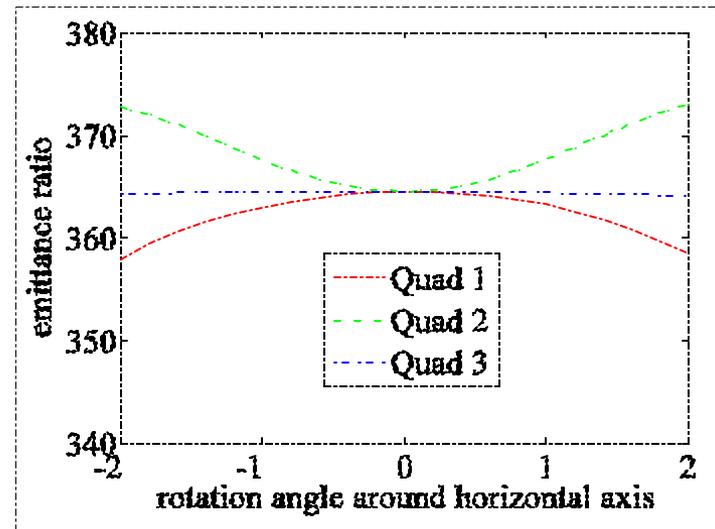
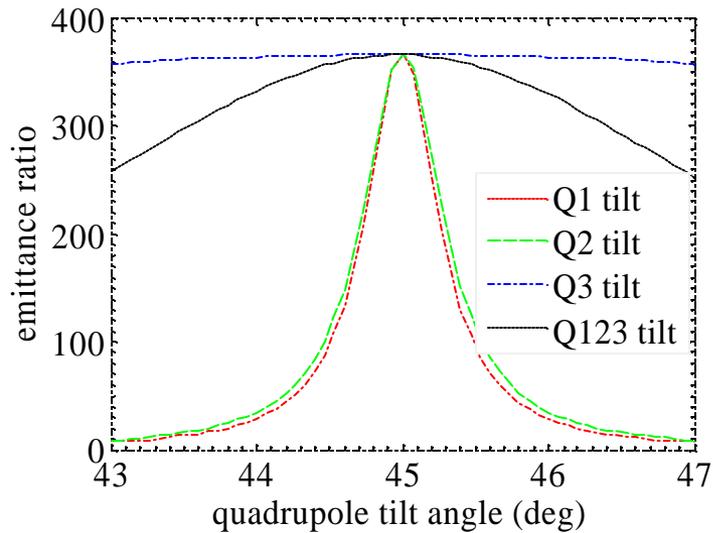
Accelerating mode center is shifted

? time-dependent dipole kick

? vertical emittance growth



Quadrupole alignment: rotation and displacement around each axis



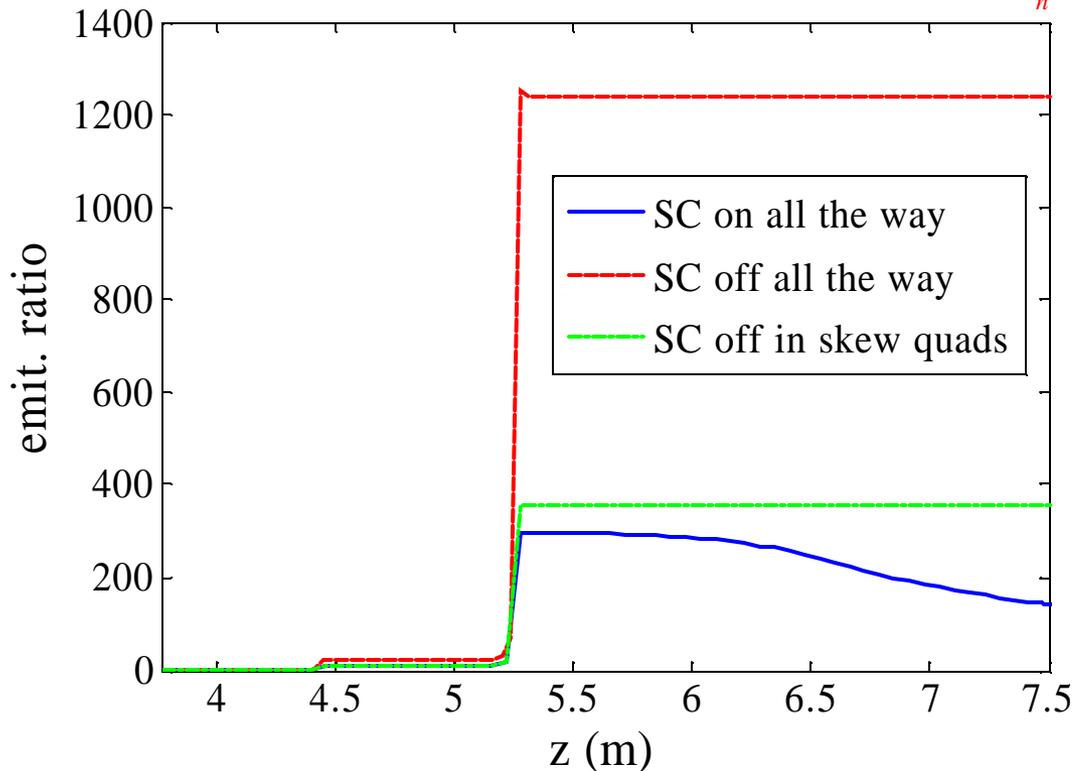
Space-charge effects in rf gun

Space charge in the rf gun is the main limiting factor in flat-beam generation.

$$\mathbf{e}_n^{sc} \approx \sqrt{\left(b \frac{I}{I_0} \frac{1}{16\sqrt{2}} \right)^2 + \mathbf{e}_n^2}$$

$$\mathbf{e}_n = 1 \mu\text{m} \Rightarrow \mathbf{e}_n^{sc} = 3.5 \mu\text{m}$$

$$\mathbf{e}_n^- = 0.02 \mu\text{m} \Rightarrow \mathbf{e}_n^{-,sc} = 0.30 \mu\text{m}$$



emittance ratio decreases from 10^3 to 10^2 as a result of the non-linear space-charge effects in the rf gun area.

Upper limit of the “true” flat beam emittances

$$\mathbf{S}_0 = \sqrt{\mathbf{S}^2 - \mathbf{S}_{res}^2}$$

upper limit of true rms size

directly measured

best measured camera resolution

	95%	-dispersion at 95%	simulation
rms_X7x (mm)	0.088±0.001	0.065±0.001	0.058
rms_X8_vslit (mm)	0.11±0.01	0.11±0.01	0.11
e_x (mm mrad)	<u>0.41±0.02</u>	<u>0.30±0.02</u>	0.27
$\sqrt{e_x e_y}$	<u>4.1±0.1</u>	<u>3.5±0.1</u>	3.8
e_y/e_x	<u>100±5</u>	<u>137±15</u>	196