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# Invisible Gauge Bosons

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**Could there exist  
massless gauge bosons  
other than the photon?**

$U(1)_{B-L}$  is the only global symmetry of the standard model that can be gauged and **unbroken**.

$Z_{B-L}$  coupling to ordinary matter:  $N_n g_z$   
( $N_n =$  number of neutrons)

**To avoid deviations from Newton's law:**

$$g_z \ll \frac{m_n}{M_{\text{Pl}}} \sim 10^{-19}$$

Tests of the equivalence principle:  $g_z < 10^{-24}$

weaker limit if  $B - L$  force is screened by  $\nu$ 's (*Okun, et al*)

*But* even when  $z_q = z_u = z_d = z_l = z_e = 0$

there can still be interactions of the standard model fields with the new massless gauge boson:

**higher-dimensional operators!**

$\gamma'$  couplings to leptons:

$$\frac{1}{M^2} P_{\mu\nu} (\bar{l}_L \sigma^{\mu\nu} F_e H e_R + \text{h.c.})$$

$F_e$ :  $3 \times 3$  matrix in flavor space,  
dimensionless parameters

$\gamma'$  couplings to quarks: similar dimension-6 operators

In the mass eigenstate basis  $F_e \rightarrow F'_e = U_L^e F_e U_R^{e\dagger}$

$U_L^e$  and  $U_R^e$  are the unitary matrices that diagonalize the masses of the electrically-charged leptons.

- Interactions of the mass-eigenstate leptons with  $P^\mu$  (chirality-flip operators  $\sim v_h \approx 174$  GeV) :

$$\frac{v_h}{M^2} P_{\mu\nu} \bar{e}' \sigma^{\mu\nu} (\text{Re}F'_e + i \text{Im}F'_e \gamma_5) e'$$

→ magnetic-like and electric-like dipole moments

$\text{Re}(F'_e)^{ij}$ ,  $\text{Im}(F'_e)^{ij}$  could have any value  $\lesssim 4\pi$ , but:

chirality-flip operators  $\rightarrow$  probably  $|F_e^{ij}| \lesssim |\lambda_e^{ij}|$

$$\Rightarrow |F_e^{ij}| \lesssim \frac{m_\tau}{v_h} \approx 10^{-2}$$

$|F_e^{11}|$  may naturally be below  $m_e/v_h \approx 3 \times 10^{-6}$

**Kinetic mixing of  $U(1)_Y \times U(1)_z$  gauge bosons:**

$c_0 B^{\mu\nu} F_{\mu\nu}$       **dimension-four operator!**

*Holdom 1985:*

**Kinetic terms can be diagonalized and canonically normalized by a  $SL(2, R)$  transformation.**

**Global  $SO(2)$  symmetry: linear combination of  $U(1)$  fields that couples to hypercharge is the real  $B^\mu$ .**

**Orthogonal combination (“paraphoton” =  $\gamma'$ ) does not have any renormalizable couplings to standard model fields.**

*Conclusion:*

*kinetic mixing has no effect on the standard model fields other than a renormalization of the hypercharge gauge coupling.*

## Bosonic interactions of the paraphoton:

$$\frac{1}{M^2} H^\dagger H (c_1 B_{\mu\nu} + \tilde{c}_1 \tilde{B}_{\mu\nu} + c_2 P_{\mu\nu} + \tilde{c}_2 \tilde{P}_{\mu\nu}) P^{\mu\nu}$$

- renormalize the  $U(1)$  gauge couplings
- include vertices with two  $U(1)$  gauge bosons and Higgs bosons.

*These are all operators of  $d \leq 6$  involving both  $\gamma'$  and SM fields*

# Primordial Nucleosynthesis

Constraints on any new particles with mass below several MeV.

Interaction rate of  $\gamma'$  with SM fields:  $\Gamma_s \approx \frac{c^2 m_e^2 T^3}{M^4}$

$$c \equiv F_e' \frac{v_h}{m_e}$$

Expansion rate of the universe:  $H \approx \frac{T^2}{M_{\text{Pl}}} \left( \frac{2\pi^3}{45} g_*(T) \right)^{1/2}$

At the freeze-out temperature,  $T_D$ :  $\Gamma_s = H$

$$\Rightarrow \frac{M}{\sqrt{c}} \approx 1.5 \text{ TeV} \times [g_*(T_D)]^{-1/8} \left( \frac{T_D}{1 \text{ GeV}} \right)^{1/4}$$

Number of degrees of freedom contributed by  $\gamma'$  during nucleosynthesis, for  $T_D > T_{\text{BBN}} \approx 1 \text{ MeV}$ :

$$\Delta g_*(T_{\text{BBN}}) = 2 \left[ \frac{g_*(T_{\text{BBN}})}{g_*(T_D)} \right]^{4/3}$$

$$\Delta g_*^{\text{max}} = \frac{7}{8} \Delta N^{\text{max}} \quad \longrightarrow \quad g_*(T_D) > \frac{20.0}{(\Delta N_\nu^{\text{max}})^{3/4}}$$

At the  $2\sigma$  level,  $\Delta N_\nu^{\text{max}} \approx 0.6 \quad \longrightarrow \quad g_*(T_D) > 30$

$T_D > T_{\text{QCD}} \approx 150 - 180 \text{ MeV}$

(for  $T_D \gtrsim T_{\text{QCD}}$ :  $g_* = 247/4$ )

$$\frac{M}{\sqrt{c}} \gtrsim 0.5 \text{ TeV}$$

# Star cooling

Effective coupling of  $\gamma'$  to electrons:  $g_{\gamma'e} = \frac{c}{M^2} m_e^2$

Red giant stars:

$$g_{\gamma'e} < 2.5 \times 10^{-13} \quad \Rightarrow \quad \frac{M}{\sqrt{c}} \gtrsim 1.2 \text{ TeV}$$

For supernovae:  $\nu$  emission rate  $\gg$   $\gamma'$  emission rate  
 $\Rightarrow$  no useful bound on electron- $\gamma'$  coupling  
(strong bound on quark- $\gamma'$  couplings)

# Flavor-changing neutral currents

Chirality-flip transition:  $\Gamma(\mu \rightarrow e\gamma') = c_{e\mu}^2 \frac{m_\mu^5}{8\pi M^4}$

Standard model:  $\Gamma(\mu \rightarrow e\nu\bar{\nu}) = \frac{m_\mu^5 G_F^2}{192\pi^3} \approx 3.2 \times 10^{-10} \text{eV}$

$$\text{Br}(\mu \rightarrow e\gamma') < 3 \times 10^{-4} \quad \Rightarrow \quad \frac{M}{\sqrt{c_{e\mu}}} \gtrsim 8 \text{ TeV}$$

	$l_L$	$e_R$	$N_L$	$N_R$	$H$	$\phi$
$SU(2)_W$	2	1	1	1	2	1
$U(1)_Y$	-1	-2	0	0	+1	-2
$U(1)_D$	0	0	+1	+1	0	-1

Yukawa interaction:  $\lambda_\phi^j \bar{e}_R^j N_L \phi + \text{h.c.}$

Contribution to the  $iP_{\mu\nu} \bar{e}_R \gamma^\mu \partial^\nu e_R$  operator ( $\sim P_{\mu\nu} \bar{l}_L \sigma^{\mu\nu} e_R H$ ):

The image shows two Feynman diagrams for the triangle loop contribution to the operator. The first diagram has external lines labeled  $e_R$  and  $e_R$  at the bottom, and  $\phi$  and  $\phi$  at the top. The internal lines are labeled  $N$ . The second diagram has external lines labeled  $e_R$  and  $e_R$  at the bottom, and  $N$  and  $N$  at the top. The internal lines are labeled  $\bar{\phi}$ . To the right of the diagrams is the equation  $\Rightarrow C_e^{ij} = \frac{\lambda_\phi^i \lambda_\phi^{*j} g_p}{192\pi^2}$ .

## Conclusions

New massless gauge boson may couple to quarks and leptons via dimension-6 operators suppressed by the TeV scale!

The lightest particle charged under the new  $U(1)$  is a good dark matter candidate.

Look for paraphotons at the Tevatron (coupling to top-quark), LHC, LC, ...