

# *Mathematica* in Research.

Wolfram *Seminar*.

Presenter: *Paritosh Mokhasi*.

*paritoshm@wolfram.com*,

Jeff Todd: *jtodd@wolfram.com*,

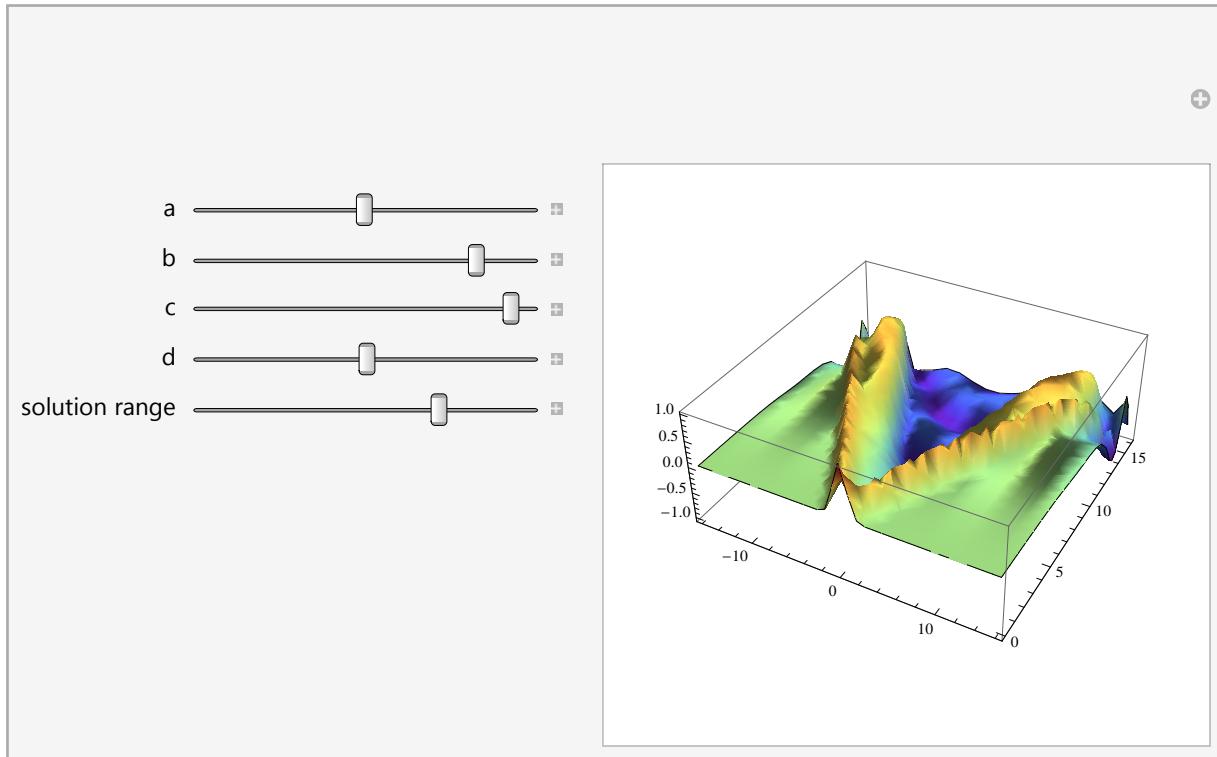
Justin Kehinde: *jkehinde@wolfram.com*

Mon 6 Jun 2011 12:11:01 (GMT -5.)

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*Mathematica presentation - Argonne National Laboratory.*

## What is *Mathematica*?



- ▲ Solve and dynamically visualize solution space of a nonlinear PDE
  - » **Compute & visualize:** wide range of functions for mathematics, science, engineering; automatic algorithm selection; visualize anything!
  - » **Develop:** consistent high-level language; choose the programming paradigm that is best for your computational needs – procedural, functional, rule-based, recursive, object-oriented; advanced development tools
  - » **Performance:** state-of-the-art performance, parallel computation with built-in multicore support, adaptive scalability, precision control
  - » **Data manipulation:** integrate computable data; statistical model analysis; charting and visualization tools for all your data
  - » **Dynamic interactivity:** automated interface construction; create dynamic interfaces quickly and easily; manipulate graphics, math, tables, text, etc.
  - » **Connectivity:** automated import/export; built-in connectivity with databases, spreadsheets, legacy C or Fortran code, Web Services, Java, .NET; web-enabled connectivity

- » **Document & deploy:** interactive document system; write papers/reports/articles/books/homework; output to PDF, HTML, XML; create slide show presentations; dynamic report generation; deploy with *Mathematica* Player

## What's New

Wolfram|Alpha Integration

Core Algorithms

2D and 3D Graphics

Probability and Statistics

Financial Engineering

Image Processing

Control Systems

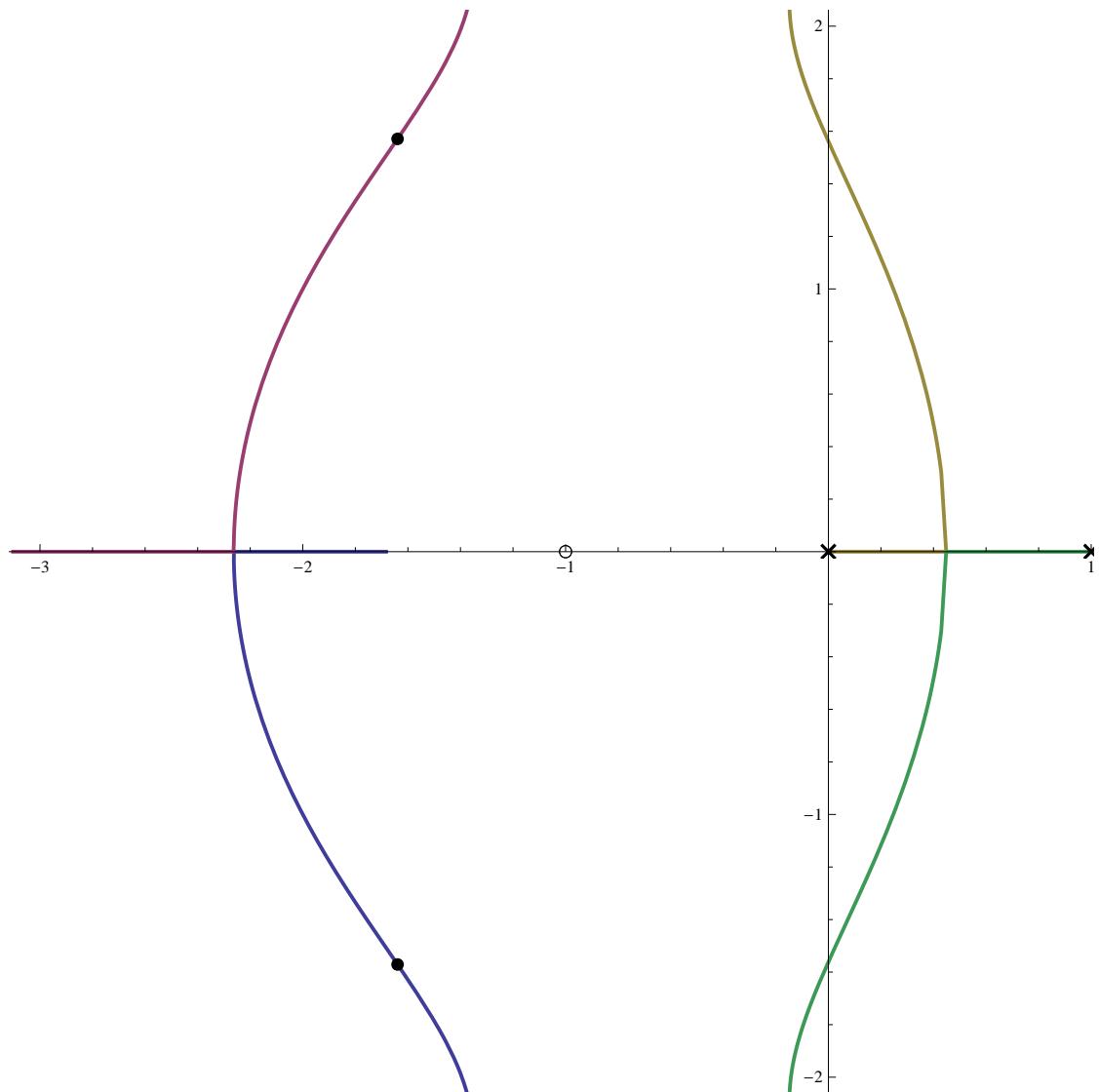
Wavelet Analysis

Graphs and Networks

Programming and Development

# Mathematica: The Numerical Engine

## 1s: Locus Plotting



# Mathematica: The Symbolic Engine

init

Series

Derivative

Integrate

Solve

Minimize

Differential Equations

Untitled-4 \*

Study the phase-space portrait of a dynamical system

```
In[2]:= sol = DSolve[{x'[t] == -2 y[t] + 3 x[t], y'[t] == 15 x[t] - y[t], x[0] == a, y[0] == b}, {x, y}, t]
Out[2]= {{x -> Function[t, -1/13 e^t (-13 a Cos[sqrt[26] t] - sqrt[26] a Sin[sqrt[26] t] + sqrt[26] b Sin[sqrt[26] t])], y -> Function[t, 1/26 e^t (26 b Cos[sqrt[26] t] + 15 sqrt[26] a Sin[sqrt[26] t] - 2 sqrt[26] b Sin[sqrt[26] t])]}}
```

```
In[44]:= Manipulate[rp = {x[t], y[t]} /. sol /. {a -> 1/(13+m), b -> 1/(15+m)};
ParametricPlot[rp, {t, -5, 5}, Evaluate -> True, ImageSize -> 400, PlotStyle -> Thick,
PlotRange -> {{-1, 1}, {-1, 1}}], {{m, 0, "Change Initial Condition"}, 0, 20}]
```

Change Initial Condition

## Linear Algebra

Solve a small  $3 \times 3$  linear system.

```
mat = {{2.0, 3.1, -1.1}, {0.2, -0.29, 3.3}, {-1.5, 4.2, 4.7}}
b = {-1.0, 2.2, 0.5};
{{2., 3.1, -1.1}, {0.2, -0.29, 3.3}, {-1.5, 4.2, 4.7}}
xvec = LinearSolve[mat, b]
```

---

Check the answer.

```
mat.xvec
```

Set up and solve a sparse system (`RandomSparseArray` is defined at the end of this notebook).

```
A = RandomSparseArray[{100000, 100000}];
b = RandomReal[{0, 1}, 100000];
```

`LinearSolve` automatically chooses the appropriate algorithm to use on this sparse system.

```
xvec = LinearSolve[A, b]; // Timing
Norm[A.xvec - b]
Clear[A, xvec, b];
» Fast exact linear algebra
» Applications example - Solving elliptic PDE using finite differences.
```

## Regression

Import the first sheet from a spreadsheet file and plot the data.

```
data = Import["noisydata.xls", {"Data", 1}]
dataplot = ListPlot[data]
```

---

Fit the data to a linear model.

```
fit = LinearModelFit[data, {1, x, x^2, x^3}, x]
```

---

Display the ANOVA table:

```
fit["ANOVATable"]
```

---

Show the fit function together with the data.

```
Show[dataplot,
  Plot[fit[x], {x, -5, 15}, PlotStyle -> Red]]
```

Pulsar example

## Solving Algebraic Equations

This solves a simple quadratic equation with symbolic parameters.

```
Solve[a x2 + b x + c == 0, x]
```

Solve equations involving power series

```
y = 1 + Sum[a[i] xi, {i, 3}] + O[x]4 ;
eqn = D[y, x]2 - y == x ;
Solve[LogicalExpand[eqn]]
```

Whereas **Solve** is set up to give you generic solutions to equations, **Reduce** will give all possible solutions. This example restricts the solutions to the domain of real numbers.

```
Reduce[ $\sqrt[3]{27^{2x-1}} == \sqrt{9^{2x-1}}$ , x, Reals]
```

### » Conditional results

Solve an equation over the reals and get a conditional result:

```
soln = Solve[x2 + y2 == z2 && x + y + 3 z == 1, {x, y}, Reals]
ParametricPlot[{x, y} /. soln, {z, 0, 1}]
```

## Solving Nonlinear Equations

Solving large nonlinear equations with constraints

```
Clear[f, cons, vars, x];
{f, cons, vars} =
{
$$\frac{20 x[2] x[6]}{x[1]^2 x[4] x[5]^2} + \frac{15 x[3] x[4]}{x[1] x[2]^2 x[5] x[7]^{0.5}} +$$


$$\frac{10 x[1] x[4]^2 x[7]^{0.125}}{x[2] x[6]^3} + \frac{25 x[1]^2 x[2]^2 x[5]^{0.5} x[7]}{x[3] x[6]^2},$$


$$\begin{cases} 0.1 \leq x[1] \leq 10, 0.1 \leq x[2] \leq 10, 0.1 \leq x[3] \leq 10, \\ 0.1 \leq x[4] \leq 10, 0.1 \leq x[5] \leq 10, 0.1 \leq x[6] \leq 10, \\ 0.01 \leq x[7] \leq 10, 1 - \frac{0.2 x[3] x[6]^{2/3} x[7]^{0.25}}{x[2] x[4]^{0.5}} - \\ \frac{0.7 x[1]^3 x[2] x[6] x[7]^{0.5}}{x[3]^2} - \frac{0.5 x[1]^{0.5} x[7]}{x[3] x[6]^2} \geq 0, \\ 1 - \frac{3.1 x[2]^{0.5} x[6]^{1/3}}{x[1] x[4]^2 x[5]} - \frac{1.3 x[2] x[6]}{x[1]^{0.5} x[3] x[5]} - \\ \frac{0.8 x[3] x[6]^2}{x[4] x[5]} \geq 0, \\ 1 - \frac{x[2] x[3]^{0.5} x[5]}{x[1]} - \frac{0.1 x[2] x[5]}{x[3]^{0.5} x[6] x[7]^{0.5}} - \\ \frac{2 x[1] x[5] x[7]^{1/3}}{x[3]^{1.5} x[6]} - \frac{0.65 x[3] x[5] x[7]}{x[2]^2 x[6]} \geq 0, \\ 1 - \frac{1}{x[5]^{2/3}} 0.3 x[1]^{0.5} x[2]^2 x[3] x[4]^{1/3} x[7]^{0.25} - \\ \frac{0.2 x[2] x[5]^{0.5} x[7]^{1/3}}{x[1]^2 x[4]} - \frac{0.5 x[4] x[7]^{0.5}}{x[3]^2} - \\ \frac{0.4 x[3] x[5] x[7]^{0.75}}{x[1]^3 x[2]^2} \geq 0, \end{cases}$$

```

$$\begin{aligned}
 & \frac{20 x[2] x[6]}{x[1]^2 x[4] x[5]^2} + \frac{15 x[3] x[4]}{x[1] x[2]^2 x[5] x[7]^{0.5}} + \\
 & \frac{10 x[1] x[4]^2 x[7]^{0.125}}{x[2] x[6]^3} + \frac{25 x[1]^2 x[2]^2 x[5]^{0.5} x[7]}{x[3] x[6]^2} \geq \\
 100, \quad & \frac{20 x[2] x[6]}{x[1]^2 x[4] x[5]^2} + \frac{15 x[3] x[4]}{x[1] x[2]^2 x[5] x[7]^{0.5}} + \\
 & \frac{10 x[1] x[4]^2 x[7]^{0.125}}{x[2] x[6]^3} + \frac{25 x[1]^2 x[2]^2 x[5]^{0.5} x[7]}{x[3] x[6]^2} \leq \\
 & 3000 \}, \{x[1], x[2], x[3], x[4], x[5], x[6], x[7]\};
 \end{aligned}$$

**TraditionalForm[Column@{f, cons}]**

**FindMinimum[{f, cons}, vars] // Timing**

Solving nonlinear equations with multiple minima

Fitting ODE to Noisy Data

Solving Implicit Equations

## Integration and Differentiation

Access a vast array of knowledge, for example, to compute an indefinite integral (easily entered with the Basic Math Assistant palette).

$$\int e^{-t^2} dt$$

Integrate a surface over the region defined by a cone.

```
Integrate[ (x^2 + y^2) Boole[ 0 <= z <= 1 && x^2 + y^2 <= z^2] ,
{ x, -1, 1}, { y, -1, 1}, { z, 0, 1}]
```

You can visualize three-dimensional regions using `RegionPlot3D`.

```
RegionPlot3D[ 0 <= z <= 1 && x^2 + y^2 <= z^2,
{ x, -1, 1}, { y, -1, 1}, { z, 0, 1}]
```

A seemingly simple function whose definite integral is anything but simple.

$$\int_0^\infty \frac{\sin[x^3]}{e^{x/2}} dx$$

» High oscillatory integration

SIAM challenge problem:

```
Plot[ 1/x Cos[ Log[x]/x], { x, 0, 1},
PlotRange -> 15, Filling -> Axis]
```

New methods handle highly oscillatory integration problems automatically:

```
NIntegrate[ 1/x Cos[ Log[x]/x], { x, 0, 1}]
```

## Solving Differential Equations

This system of ordinary differential equations give rise to the chaotic map known as the Lorenz attractor.

$$\begin{aligned}x'(t) &= \sigma(y(t) - x(t)) \\y'(t) &= \rho x(t) - y(t) - x(t) z(t) \\z'(t) &= x(t) y(t) - \beta z(t)\end{aligned}$$

This gives the solution for the initial conditions  $x(0) = 0$ ,  $y(0) = 1$  and  $z(0) = 0$ .

```
soln = With[{ $\sigma$  = -3.0,  $\rho$  = 26.5,  $\beta$  = 1.0},
NDSolve[{ $x'$ [t] ==  $\sigma$  ( $x$ [t] -  $y$ [t]),  

 $y'$ [t] == - $x$ [t]  $z$ [t] +  $\rho$   $x$ [t] -  $y$ [t],  

 $z'$ [t] ==  $x$ [t]  $y$ [t] -  $\beta$   $z$ [t],  $x$ [0] ==  $z$ [0] == 0,  $y$ [0] == 1},  

{ $x$ ,  $y$ ,  $z$ }, {t, 0, 200}, MaxSteps  $\rightarrow$   $\infty$ ]

ParametricPlot3D[Evaluate[{ $x$ [t],  $y$ [t],  $z$ [t]} /. soln],  

{t, 0, 200}, ColorFunction  $\rightarrow$   $\left(\text{Hue}\left[\frac{\#4}{210}\right] \&\right)$ ,  

ColorFunctionScaling  $\rightarrow$  False, PlotPoints  $\rightarrow$  250,  

Axes  $\rightarrow$  False, Background  $\rightarrow$  Black,  

BoxRatios  $\rightarrow$  1, ImageSize  $\rightarrow$   $7 \times 72$ ]
```

1D - Heat conduction problem with time dependent boundary conditions

Damped pendulum

Wolfram's 1D- Nonlinear wave equation.

2D modified Burger's problem with periodic boundary conditions on regular domain

Lotka-Volterra with delays

Stochastic Differential Equations example:

## Visualizations

---

Plot the surface  $\cos(x + \sin(y))$  together with the plane  $\frac{x}{6} - \frac{y}{7} - \frac{1}{3}$ .

```
Plot3D[{\Cos[x + Sin[y]], x/6 - y/7 - 1/3},
{x, 0, 2 π}, {y, -π, π}, PlotStyle -> {Red, Blue}]
```

---

Using Textures - Begin with a stream plot:

```
arrows = Rasterize[StreamPlot[
Evaluate[{\Re[(x + I y)^4 - 1], -Im[(x + I y)^4 - 1]}],
{x, 0, 3}, {y, 0, 3}, VectorScale ->
{Automatic, Automatic, Log[#5 + 1] &}, Frame -> False]]
```

---

Layer it onto a 3D plot:

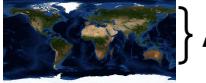
```
Plot3D[Sin[x y], {x, 0, 3}, {y, 0, 3}, Mesh -> None,
PlotStyle -> Texture[arrows]]
```

[More examples](#)

[Combine live video and textures](#)

## Image Processing

A simple demonstration of panning and zooming of a large image. The resizing method is adaptively selected.

```
with[{i = },  
Manipulate[  
ImageResize[  
ImageCrop[i, {300, 300}/zoom, -pts], {300, 300},  
Resampling \[Rule] ControlActive["Nearest", "Lanczos"]],  
{pts, {0, 0}}, {-1, -1}, {1, 1}},  
{zoom, 1}, 1, 10]  
]
```

[Geometric Transformations](#)

[Feature Detection](#)

[Live Image Capture](#)

## Control Systems

*Mathematica* introduces a unifying symbolic representation of transfer function and state space models.

---

Get a state space model from differential equations for coupled damped oscillators:

```
model = StateSpaceModel[
  {2 x2[t] - x3[t] +  $\frac{3 x2'[t]}{2} - \frac{x3'[t]}{2} + x2''[t] == F[t]$ ,
   -x2[t] + x3[t] -  $\frac{x2'[t]}{2} + \frac{x3'[t]}{2} + 2 x3''[t] == 0$ },
  {{x2[t], 0}, {x2'[t], 0}, {x3[t], 0}, {x3'[t], 0}},
  {{F[t], 0}}, {x2[t], x3[t]}, t]
```

---

Convert between state space representation and classical transfer function representation:

**TransferFunctionModel**[**model**]

Immediately ask questions about the system.

---

Can the model be fully controlled with the specified input  $F[t]$ ?

**ControllableModelQ**[**model**]

---

Simulate the model with varying driving frequency:

```
Plot[Evaluate[OutputResponse[model,
  Sin[2^(t/15)]], {t, 0, 100}]], {t, 0, 100}]
```

Analyze the model:

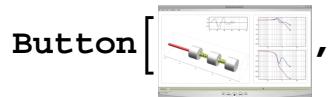
---

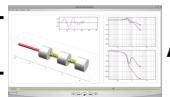
Plot frequency response gain for amplitude and phase:

```
BodePlot[model, GridLines -> Automatic,
  ImageSize -> Medium, GridLinesStyle -> GrayLevel[2/3]]
```

---

Combine with *Mathematica*'s 3D graphics, animate, and export:



```
Button[,  
SystemOpen[FileNameJoin[{NotebookDirectory[],  
"Movies", "SpringMassDamperSystem.mov"}]]]
```

## Wavelets

Wavelets localize noise and features in frequency and time simultaneously, allowing more selective filtering and analysis:

Remove one of two overlapping signals.

Noisy signal.

```
f[x_] := Sin[50 π x] Exp[-100 π (x - 0.5)^2] +
  (Sin[50 π x] + 2 Cos[140 π x]) Exp[-50 π (x - 0.2)^2] +
  2 Sin[150 π x] Exp[-80 π (x - 0.8)^2];
data = Table[f[x], {x, 0., 1, 1/2047}];
ListLinePlot[data, PlotRange → All]
```

Wavelet transform:

```
cwt = ContinuousWaveletTransform[data,
  GaborWavelet[6], {10, 16}, Padding → 0.0,
  SampleRate → 2047, WaveletScale → Automatic]
WaveletScalogram[cwt, ColorFunction → "SolarColors",
  AxesLabel → {"time", "scale"}]
```

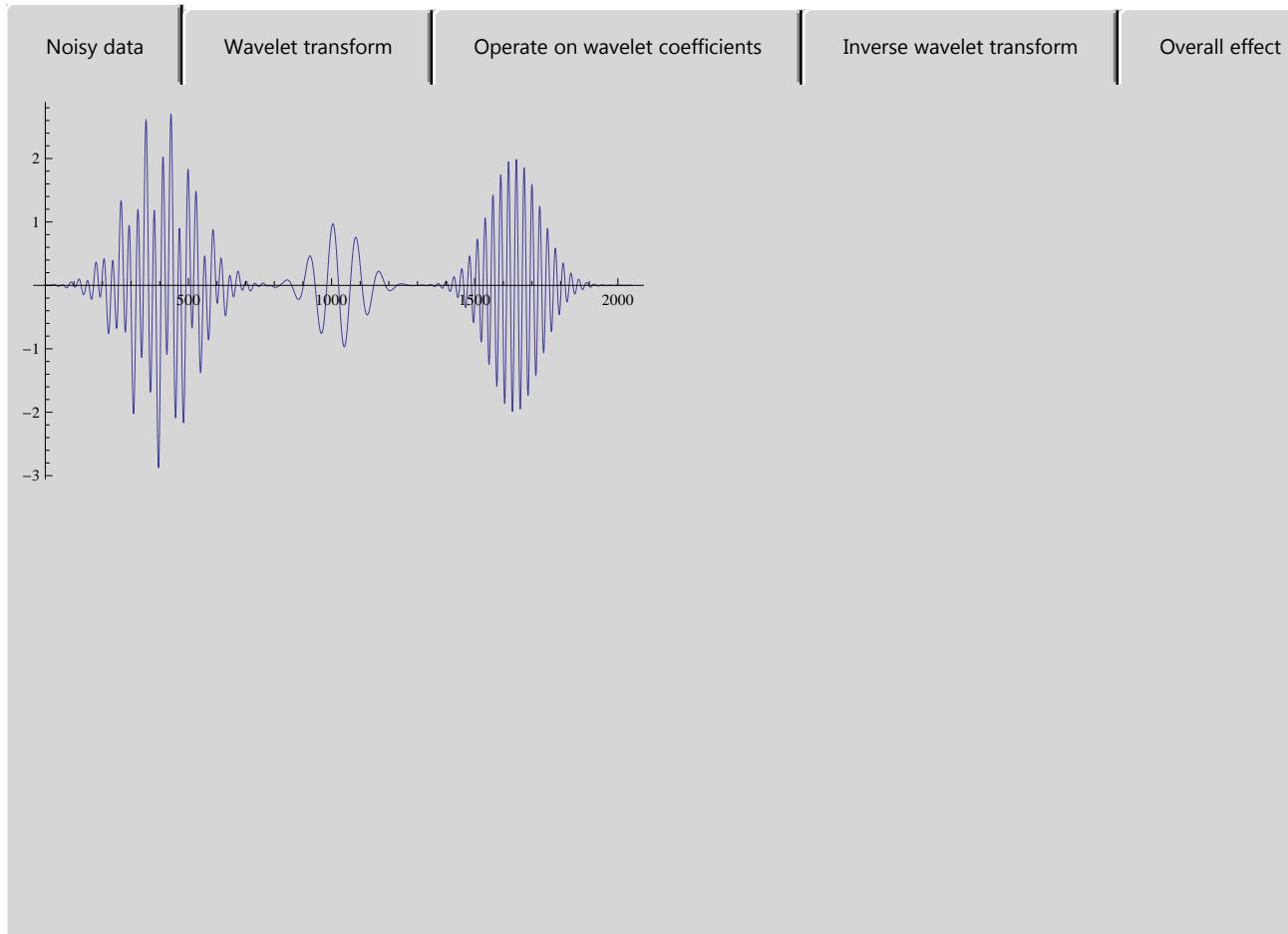
Filter out one feature:

```
vec = ConstantArray[1, Length[data]];
vec[[1 ;; 1000]] := 0.0;
cwtThresh = WaveletMapIndexed[
  #1 vec &, cwt, {{4 | 5, _}, {6, u_ /; u < 8}}];
WaveletScalogram[cwtThresh, ColorFunction → "SolarColors",
  AxesLabel → {"time", "scale"}]
```

Inverse wavelet transform:

```
rdata = InverseContinuousWaveletTransform[cwtThresh];
ListLinePlot[rdata, PlotRange → All]
```

Overall:



De-noising an image

## Import and Export

*Mathematica* aims to support as many standard data formats as possible. With the release of *Mathematica* 8 the number of supported formats rises from 145 to 172.

### New formats:

- » Arrays: `Affymetrix`<sup>†</sup>, `NASACDF`
- » Calendar: `ICS`<sup>†</sup>
- » Fonts: `BDF`<sup>†</sup>
- » Geodesy/geospatial: `ArcGRID`<sup>†</sup>, `KML`, `NDK`<sup>†</sup>, `SurferGrid`, `TLE`<sup>†</sup>
- » Graphics: `EPS`, `VTK`
- » Meterology: `GRIB`<sup>†</sup>
- » Molecular: `CIF`<sup>†</sup>
- » Spreadsheet: `XLSX`
- » Other: `NEXUS`, `JSON`

Full listing of all import and export formats:

**\$ImportFormats**

**\$ExportFormats**

<sup>†</sup> Import only

Import the first sheet of an XLSX file:

```
Import["ExampleData/cities.xlsx", {"Data", 1}]
```

Real-time video processing from a camera:

```
Dynamic[EdgeDetect[CurrentImage[]]]
```

## Programming and Development

*Mathematica's* multiparadigm language and broad range of constructs makes it a perfect choice for constructing programs at all levels.

Rule-based

```
f = Factorial[n]
```

```
f[n_] := n !
```

```
f[n_] := n f[n - 1];
```

```
f[1] = 1
```

Procedural

```
f[n_] :=
```

```
Module[{t = 1}, Do[
  t = t i, {i, n}]; t]
```

```
f[n_] :=
```

```
Module[{t = 1, i},
  For[i = 1, i ≤ n,
    i++, t *= i]; t]
```

List-based

```
f[n_] :=
```

```
Times @@ Range[n]
```

```
f[n_] := Fold[
```

```
Times, 1, Range[n]]
```

Recursive

```
f[n_] := If[n == 1,
```

```
1, n f[n - 1]]
```

Functional	<pre>f = If[#1 == 1, 1,       #1 #0[#1 - 1]] &amp;</pre>
Constructive	<pre>f[n_] := Fold[#2[#1] &amp;, 1, Array[Function[ t, #1 t] &amp;, n]]</pre>
Pattern-based	<pre>f[n_] := First[{1, n} //. {a_, b_ /; b &gt; 0} :&gt; {b a, b - 1}]</pre>
String-based	<pre>f[n_] := StringLength[Fold[ StringJoin[Table[ #1, {#2}]] &amp;, "A", Range[n]]]</pre>
Mathematical	<pre>f[n_] := Gamma[n + 1]</pre>
	<pre>f[n_] := Product[i</pre>

- » Simulating the diffusion model.
- » Theo Jensen walking linkage.

## Programming and Development: Compile

In *Mathematica* 8 the `Compile` function can automatically generate C code, compile it, link dynamically to *Mathematica* at run-time, and run in parallel (multi-threading) when possible.




---

Create a compiled function that runs in native code and in parallel:

```
f = Compile[{{c, _Complex}},
Module[{num = 1}, FixedPoint[(num++; #12 + c) &, 0,
99, SameTest -> (Re[#1]2 + Im[#1]2 ≥ 4 &)] ; num],
CompilationTarget -> "C", RuntimeAttributes -> {Listable},
Parallelization -> True]
```

---

Easily plot 200000 evaluations of the function:

```
ArrayPlot[
f[Table[x + i y, {x, -2, 1/2, 0.005}, {y, -1, 1, 0.005}],
ColorFunction -> "Rainbow"]]
```

---

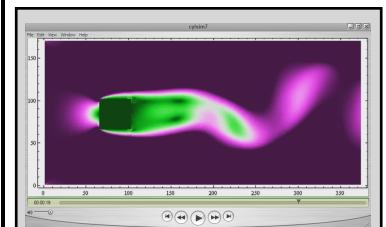
Explore the Mandelbrot set interactively using the natively compiled function:

[Code](#)

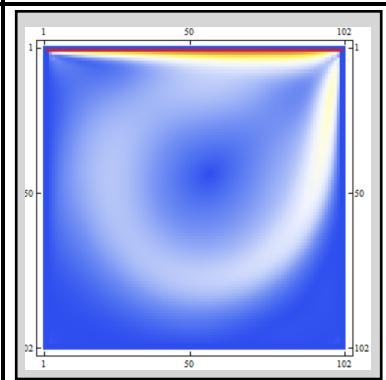
## » Solving the 2D Navier-Stokes Equations.

Generate optimized code for solving fluid problems in 2D using Lattice Boltzmann method

Flow around a 2D Cylinder



Flow in a driven cavity



## » C code generation

## Programming and Development: CUDA and OpenCL Support



- » CUDA is a parallel computing architecture from NVidia
- » Uses GPUs to carry out massively parallel computations
- » OpenCL is a unification of CUDA concepts for GPUs other than those from NVidia
- » Integration with Symbolic C and the C Compiler interface to significantly help develop and execute applications.

Load the CUDA package and get information on the hardware.

```
Needs["CUDALink`"]
CUDAInfoTable[CUDAInformation[]]
```

Lots of CUDA functions:

```
? CUDA`*
```

```
CUDAFluidDynamics[ImageSize → 800]
Image Processing
Linear Algebra
```

## Working with Documents

The screenshot shows a Mathematica notebook window titled "Theory of the Sundial". The notebook is organized into sections:

- Celestial Mechanics**: Contains a section on the motion of the Sun.
- Motion of the Sun**: Describes the eccentricity of Earth's orbit and its effect on the sun-day length. It includes three 3D models of Earth's orbit at different times of the year.
- Calculating the orbit of the sun**: A section with mathematical formulas and code for solving the Kepler problem. It shows the position of the sun relative to the earth over time.
- Analemmas**: A section featuring a user interface for calculating planetary orbits. It includes a dropdown menu for "planet" (set to "Earth"), checkboxes for "choose orbit manually" and "show sun snapshots" (which is checked), and sliders for "axis angle relative to ecliptic" and "orbit eccentricity". To the right is a plot of a planetary orbit with points marked along it.

Annotations on the right side of the window explain various features:

- Cell brackets show document structure
- Closed cell hides code
- Include annotations
- Edit and re-run code at any time
- Everything in a notebook is immediately editable, interactive, and printable

- » “Good science is good observation” - James Cameron.
- » homework assignment from computational physics course.
- » Making teaching material for students.
- » Making interactive material.

position

---

number of teeth

tooth contact angle

tooth deport

---

show construction lines

```
gearpict[11, 20°, 1, 0.4, 0, True]
```

## Connection Technologies

*Mathematica* can connect to external applications like databases, spreadsheets, or legacy C or Fortran. These external applications can then be manipulated within *Mathematica* as symbolic expressions (see the guide to Calling External Programs).

- » **Wolfram Workbench:** provides typical features of a state-of-the-art integrated development environment (IDE), customized and specialized for *Mathematica* and other Wolfram technologies (see [www.wolfram.com/products/workbench](http://www.wolfram.com/products/workbench)).
- » **J/Link™:** *Mathematica* ships with a well-developed link to Java that allows you to interactively work with a Java runtime, accessing anything that the runtime can work with (see the Java Interface guide).
- » **webMathematica™:** *webMathematica* allows you to show results on the web, and more importantly to allow others to directly interact with your computations (see examples at [www.wolfram.com](http://www.wolfram.com)).
- » **DatabaseLink:** *DatabaseLink* is a *Mathematica* application that provides a set of tools allowing convenient integration of *Mathematica* with database management systems. With *DatabaseLink* you can use all *Mathematica*'s numeric/symbolic/programming/visualization capabilities with data taken from SQL database applications (see the guide to Database Connectivity).
- » **Web Services Link:** The web services client for *Mathematica* allows users to call operations that are based on other platforms or languages that are not immediately accessible to *Mathematica* (see the reference InstallService).
- » **.Net/Link™:** *.Net/Link* integrates *Mathematica* and Microsoft's .NET platform; call .NET from *Mathematica* in a completely transparent way; use and control the *Mathematica* kernel from a .NET program (see the guide to .NET Interface).

## Mathematica Community

There is a vast *Mathematica* community that has built up around the world and that can be tapped in a variety of ways.

- » Wolfram Demonstrations Project: [demonstrations.wolfram.com](http://demonstrations.wolfram.com)
- » Applications packages such as *Rayica* or *Neural Networks*
- » Hundreds of books
- » Web resources such as Wolfram Library Archive and *MathWorld*<sup>TM</sup>
- » Training offered by Wolfram Education Group
- » Forums and user groups such as MathGroup
- » Conferences such as the annual International *Mathematica* User Conference or the International *Mathematica* Symposium

## Initializations

### » General

```
$DataDirectory = FileNameJoin[
  {NotebookDirectory[], "DataAndNotebooks"}];
AppendTo[$Path, $DataDirectory];
```

### » RandomSparseArray

```
RandomSparseArray[{n_, m_}] := SparseArray[{
  Band[{1, 1}] :> RandomReal[],
  Band[{1, 2}] :> RandomReal[],
  Band[{2, 1}] :> RandomReal[],
  Band[{n - 1, 1}, {n, 2}] :> RandomReal[1, {2, 2}],
  Band[{1, n - 1}, {2, n}] :> RandomReal[1, {2, 2}]
}, {n, m}]
```

DisplayPictureCell

```
DisplayPictureCell[expr_] := CellPrint[
  TextCell[expr, "Picture", ShowStringCharacters → False]]
```

DisplayOption and TTDisplayOption

```
DisplayOption[a_List] :=
  StringJoin[Riffle[DisplayOption /@ a, " "]];
DisplayOption[a_String] :=
  StringTrim[StringJoin[StringSplit[a,
    z : RegularExpression["[A-Z]"] :> " " <> z]]];
TTDisplayOption[expr_] := Tooltip[
  Style[DisplayOption[expr], FontFamily → "Times"],
  Labeled[Grid[List /@ FinancialDerivative[expr],
    Alignment → Left], Style["Parameters", Bold], Top]];
SetOptions[EvaluationNotebook[],
  StyleDefinitions → Notebook[{Cell[CellGroupData[
```

```
{Cell[TextData[{"Style Definitions for \n",  
    StyleBox["Wolfram Seminars",  
        FontSlant → "Italic"]}], "Subtitle"],  
Cell[StyleData[StyleDefinitions → "Default.nb"]],  
Cell[StyleData[StyleDefinitions →  
    "StyleMenuClear.nb"]], Cell[CellGroupData[  
{Cell["Style Environment Definitions",  
    "Section"], Cell[StyleData[All,  
        "SlideShow", StyleDefinitions →  
            StyleData[All, "Presentation"]],  
    PageWidth → WindowWidth, DockedCells → Cell[  
        BoxData[GridBox[{ {TooltipBox[ButtonBox[  
            StyleBox[RowBox[{" ", "□", " "}],  
                FontSize → 20, GrayLevel[0.7`]],  
            Appearance → None, ButtonFunction :>  
                (FEPrivate`NotebookToggleFullScreen[]; {}),  
            Evaluator → None], DynamicBox[  
                FEPrivate`FrontEndResource[  
                    "SlideshowToolbarText",  
                    "TooltipToggleFullScreen"]]],  
        StyleBox[RowBox[{ TooltipBox[  
            ButtonBox[StyleBox[  
                RowBox[{" ", "‹", " "}],  
                    FontSize → 25, GrayLevel[0.7`]],  
                ButtonData → "ScrollPageFirst",  
                Appearance → None], DynamicBox[  
                    FEPrivate`FrontEndResource[  
                        "SlideshowToolbarText",  
                        "TooltipFirstSlide"]]],  
        "", TooltipBox[ButtonBox[  
            StyleBox[RowBox[{" ", "‹", " "}],  
                FontSize → 25, GrayLevel[  
                    0.7`]], ButtonData →
```

```
"ScrollPagePrevious",
Appearance → None], DynamicBox[
FEPrivate`FrontEndResource[
"SlideshowToolbarText",
"TooltipPreviousSlide"]]],
"", TooltipBox[ButtonBox[
StyleBox[RowBox[{" ", ">", " "}],
FontSize → 25, GrayLevel[0.7]],
ButtonData → "ScrollPageNext",
Appearance → None], DynamicBox[
FEPrivate`FrontEndResource[
"SlideshowToolbarText",
"TooltipNextSlide"]]],
"", TooltipBox[ButtonBox[
StyleBox[RowBox[{" ", ">", " "}],
FontSize → 25, GrayLevel[0.7]],
ButtonData → "ScrollPageLast",
Appearance → None], DynamicBox[
FEPrivate`FrontEndResource[
"SlideshowToolbarText",
"TooltipLastSlide"]]],
ButtonBoxOptions → {Alignment →
{Automatic, FEPrivate`If[
FEPrivate`$OperatingSystem ===
"Unix", -0.4`, -0.5`]}},
Appearance → "Palette",
ButtonFunction :>
(FEPrivate`FrontEndExecute[
FrontEnd`FrontEndToken[
FrontEnd`ButtonNotebook[],
#1]] &), Evaluator → None,
FrameMargins → 0, ImageMargins →
0, ImageSize → Medium}],
DynamicModuleBox[{cells$$ = {}},
```

```

tagFind$$ = False}, TagBox[
DynamicBox[PopupMenuBox[Dynamic[0,
With[{nb$ = ButtonNotebook[]}],
SelectionMove[nb$, Before,
Notebook, AutoScroll → False];
If[tagFind$$, Do[NotebookFind[
nb$, "SlideShowHeader", Next,
CellTags, AutoScroll → False],
{#1}], Do[NotebookFind[nb$,
"SlideShowNavigationBar",
Next, CellStyle, AutoScroll →
False], {#1}]]]; SelectionMove[
nb$, After, Cell, AutoScroll →
False]; NotebookWrite[nb$,
Cell["", Deletable → True,
ShowCellBracket → False],
All]; NotebookDelete[nb$];
SelectionMove[nb$, If[
tagFind$$, Previous, Next],
Cell]] &], cells$$,
StyleBox[RowBox[{DynamicBox[
CurrentValue[{"CounterValue",
"SlideShowNavigationBar"}]],
DynamicBox[
FEPrivate`FrontEndResource[
"SlideshowToolbarText",
"SlideshowToolbarCounterText"
]],
DynamicBox[CurrentValue[
{"MaxCounterValue",
"SlideShowNavigationBar"}]]}]
,
"ControlStyle"], Appearance →
None, ImageSize → Automatic],

```

```
ImageSizeCache → {50.`,  
{6.`, 18.`}}], EventHandlerTag[  
{"MouseDown" :> Module[{cnt$, nb$ =  
InputNotebook[]}, cells$$ =  
{}; cnt$ = Apply[(NotebookFind[  
nb$, #1, All, #2, AutoScroll →  
False]; CurrentValue[nb$,  
{"CellCount", True}]) &,  
{{"SlideShowNavigationBar",  
CellStyle},  
 {"SlideShowHeader",  
CellTags}}, {1}]; cnt$ =  
(If[tagFind$$ = #1 == 0,  
#2, #1] &) @@ cnt$;  
SelectionMove[nb$, Before,  
Notebook, AutoScroll → False];  
If[tagFind$$, cells$$ =  
(#1 → "Slide " <> ToString[  
#1] &) /@ Range[cnt$],  
Do[NotebookFind[nb$,  
"SlideShowNavigationBar",  
Next, CellStyle, AutoScroll →  
False]; SelectionMove[nb$,  
Next, Cell, AutoScroll →  
False]; AppendTo[cells$$,  
NotebookRead[nb$] /.  
s_StyleSheet :> With[{ss = Join[  
Take[s, 1], DeleteCases[Rest[  
s], _String | _[FontColor,  
_]]]}, ss /; True]], {cnt$}];  
cells$$ = Replace[cells$$[[  
All, 1]], {BoxData[c_] :> c,  
TextData[c_] :> RowBox[  
If[ListQ[c], c, {c}]]}, 1];
```

```

    cells$$ = Thread[Range[
      cnt$] \[Rule] cells$$]],

PassEventsDown \[Rule] True,
EvaluationOrder \[Rule] Before,
PassEventsDown \[Rule] Automatic,
PassEventsUp \[Rule] True}]],

DynamicModuleValues \[Rule] {}}],

AutoDelete \[Rule] False, GridBoxItemSize \[Rule]
{ "Columns" \[Rule] {Automatic,
Fit, Automatic}}]],

"DockedCell", CellDynamicExpression \[Rule]
If[CurrentValue[EvaluationNotebook[],

{TaggingRules,
"DisableController"}] ===
True, Null, (FrontEndExecute[
FrontEnd`FrontEndToken[
FrontEnd`InputNotebook[], #1]] &) [
Switch[ControllerState["Apple IR",
{"B1", "B2"}],
{True, _}, "ScrollPagePrevious",
{_, True}, "ScrollPageNext",
_, None]]], Magnification \[Rule] 0.75`],

ScrollingOptions \[Rule] {"PagewiseDisplay" \[Rule] True,
"VerticalScrollRange" \[Rule] Fit},
ShowGroupOpener \[Rule] False, MenuSortingValue \[Rule]
1300], Cell[StyleData["DockedCell"],
Editable \[Rule] False, Evaluator \[Rule] "Local",
PageWidth \[Rule] WindowWidth, CellFrame \[Rule]
{{0, 0}, {0, 0}}, ShowSelection \[Rule] True,
CellMargins \[Rule] {{0, 0}, {0, 0}},
CellElementSpacings \[Rule] {"ClosedCellHeight" \[Rule]
0, "ClosedGroupTopMargin" \[Rule] 0},
DynamicUpdating \[Rule] True, CellFrameMargins \[Rule]
{{0, 0}, {0, 4}}, ContextMenu \[Rule] None,

```

```
ComponentwiseContextMenu → { } ,
ShowStringCharacters → False ,
LineBreakWithin → False , Magnification → 1 ,
Background → GrayLevel[0.97`] ,
TooltipBoxOptions →
{ TooltipDelay → Automatic } ] } ,
Open] ] , Cell[CellGroupData[
{Cell["Styles for Headings", "Section"] ,
Cell[CellGroupData[{Cell[StyleData["Title"] ,
MenuSortingValue → 1, MenuCommandKey →
"1", FontFamily → "Georgia", FontSize →
36, FontWeight → Plain, FontColor →
RGBColor[0.796078`, 0.0705882`, 0]], ,
Cell[StyleData["Title", "Presentation"] ,
CellMargins → {{90, 100}, {10, 100}}, ,
FontSize → 54], Cell[StyleData["Title",
"SlideShow"]}], Closed]]], Cell[
CellGroupData[{Cell[StyleData["Subtitle"] ,
MenuSortingValue → 100, MenuCommandKey →
"2", FontFamily → "Georgia", FontSize →
24, FontWeight → "Plain", FontSlant →
"Italic"], Cell[StyleData["Subtitle",
"Presentation"], CellMargins →
{{90, 100}, {100, 20}}, FontSize → 32], ,
Cell[StyleData["Subtitle", "SlideShow"]]}], ,
Closed]]], Cell[CellGroupData[
{Cell[StyleData["Subsubtitle"] ,
MenuSortingValue → 200, MenuCommandKey →
"3", FontFamily → "Georgia", FontSize →
20, FontWeight → "Plain", FontSlant →
"Italic", FontColor → GrayLevel[0.2`]], ,
Cell[StyleData["Subsubtitle",
"Presentation"], CellMargins →
{{90, 20}, {2, 120}}, LineSpacing →
```

```
{1.25` , 1} , FontSize → 26] , Cell[  
  StyleData["Subsubtitle", "SlideShow"]]],  
 Closed]], Cell[CellGroupData[  
  {Cell[StyleData["DateSection"],  
    CellMargins → {{30, 0}, {12, 24}},  
    ShowStringCharacters → False], Cell[  
      StyleData["DateSection", "Presentation"],  
      CellMargins → {{90, 20}, {2, 36}},  
      ShowStringCharacters → False, FontSize →  
      21], Cell[StyleData["DateSection",  
      "SlideShow"]]}, Closed]]},  
 Closed]], Cell[CellGroupData[  
  {Cell["Styles for Sections", "Section"], Cell[  
    CellGroupData[{Cell[StyleData["Chapter"],  
      CellMargins → {{27, Inherited}, {8, 34}},  
      CounterIncrements → {"Chapter"},  
      MenuSortingValue → 2410, FontFamily →  
      "Georgia", FontSize → 28, FontColor →  
      RGBColor[0.811765`, 0.117647`,  
      0.145098`], CellTags → "Chapter"],  
      Cell[StyleData["Chapter", "Presentation"],  
      CellFrame → None, CellMargins →  
      {{80, 60}, {20, 30}}, FontSize → 36],  
      Cell[StyleData["Chapter",  
      "SlideShow"]]}, Closed]],  
  Cell[CellGroupData[{Cell[StyleData[  
    "LargeChapter", StyleDefinitions →  
    StyleData["Chapter"]], CellMargins →  
    {{27, Inherited}, {8, 34}},  
    MenuSortingValue → 2430, FontFamily →  
    "Georgia", FontSize → 30,  
    FontColor → RGBColor[0.811765`,  
    0.117647`, 0.145098`]],  
    Cell[StyleData["LargeChapter",
```

```
"Presentation"], CellMargins ->
{{100, 100}, {10, 150}}, FontSize -> 54],
Cell[StyleData["LargeChapter",
"SlideShow"]], Closed]], Cell[
CellGroupData[{Cell[StyleData["Section"],
CellFrame -> 0, MenuSortingValue -> 1200,
MenuCommandKey -> "4", FontFamily ->
"Georgia", FontSize -> 24, FontWeight ->
Plain, FontColor -> RGBColor[
0.811765`, 0.117647`, 0.145098`]],
Cell[StyleData["Section", "Presentation"],
CellFrame -> None, CellMargins ->
{{80, 14}, {30, 30}}, FontFamily ->
"Georgia", FontSize -> 34, FontWeight ->
Plain, FontColor -> RGBColor[0.811765`,
0.117647`, 0.145098`]], Cell[StyleData[
"Section", "SlideShow"]]}, Open]],
Cell[CellGroupData[{Cell[StyleData[
"Subsection"], CellDingbat -> "»",
CellGroupingRules -> {"SectionGrouping",
40}, MenuSortingValue -> 1300,
MenuCommandKey -> "5", FontFamily ->
"Georgia", FontSize -> 22, FontWeight ->
Plain, FontColor -> GrayLevel[0.25`]],
Cell[StyleData["Subsection",
"Presentation"], CellMargins ->
{{80, 60}, {12, 20}}, FontSize -> 25],
Cell[StyleData["Subsection",
"SlideShow"]]}, Closed]], Cell[CellGroupData[{Cell[StyleData[
"Subsubsection"], CellDingbat ->
"»", MenuSortingValue -> 1400,
MenuCommandKey -> "6", FontFamily ->
"Georgia", FontSize -> 20, FontWeight ->
```

```

Plain, FontColor → GrayLevel[0.3`]],
Cell[StyleData["Subsubsection",
  "Presentation"], CellMargins →
{{88, 60}, {0, 12}}, FontSize → 22],
Cell[StyleData["Subsubsection",
  "SlideShow"]}], Closed]],
Cell[CellGroupData[{Cell[StyleData[
  "MoreExamplesSection",
  StyleDefinitions →
  StyleData["Subsubsection"]],
CellDingbat → None, ShowGroupOpener →
True, CellGroupingRules →
{"SectionGrouping", 45},
MenuSortingValue → 2100, FontColor →
RGBColor[0.636862`, 0.0564706`, 0.`]],
Cell[StyleData["MoreExamplesSection",
  "Presentation"], CellMargins →
{{88, 60}, {20, 12}}], Cell[StyleData[
  "MoreExamplesSection", "SlideShow"],
CellMargins → {{88, 60}, {20, 12}},
WholeCellGroupOpener → True]], Closed]]},
Closed]], Cell[CellGroupData[
{Cell["Styles for Text", "Section"],
Cell[CellGroupData[
{Cell[StyleData["Text"], MenuSortingValue →
2000, MenuCommandKey → "7", FontFamily →
"Georgia", FontSize → 18],
Cell[StyleData["Text", "Presentation"],
CellMargins → {{80, 20}, {12, 12}},
LineSpacing → {1.25`, 1}, FontFamily →
"Georgia", FontSize → 20],
Cell[StyleData["Text", "SlideShow"]]}],
Closed]], Cell[CellGroupData[
{Cell[StyleData["MathCaption"]]
```

```
MenuSortingValue → 2010, MenuCommandKey →
  "8", FontFamily → "Georgia", FontSize →
  18, FontColor → GrayLevel[0]], Cell[
  StyleData["MathCaption", "Presentation"], 
  CellMargins → {{120, 12}, {6, 34}}, 
  LineSpacing → {1.25` , 1}, FontSize → 20], 
  Cell[StyleData["MathCaption",
    "SlideShow"]}], Closed]], 
Cell[CellGroupData[{Cell[StyleData[
    "IntegrationMathCaption",
    StyleDefinitions →
      StyleData["MathCaption"]],
    CellMargins → {{0, 12}, {2, 24}}, 
    CellFrameMargins → {{0, 0}, {0, 3}}, 
    CellFrameLabels → {{PaneBox[
      FrameBox[StyleBox["Integration",
        FontFamily → "Helvetica", FontSize →
        9, FontColor → GrayLevel[1],
        FontWeight → Plain], Background →
        RGBColor[0.811765` , 0.117647` ,
        0.145098` ], BoxFrame → 0,
        FrameStyle → None, FrameMargins →
        {{3, 3}, {1, 1}}], ImageSize → 56,
        Alignment → Left, FrameMargins → 0],
      None}, {None, None}]}, Cell[
  StyleData["IntegrationMathCaption",
    "Presentation"], CellMargins →
    {{30, 12}, {12, 12}}, CellFrameMargins →
    {{10, 0}, {0, 5}}, FontSize → 20], 
  Cell[StyleData["IntegrationMathCaption",
    "SlideShow"], CellMargins →
    {{30, 12}, {12, 12}}, CellFrameMargins →
    {{10, 0}, {0, 5}}]], Closed]], 
Cell[CellGroupData[{Cell[StyleData[
```

```

"AutomationMathCaption",
StyleDefinitions → StyleData[
  "IntegrationMathCaption"]], 
CellMargins → {{0, 12}, {2, 24}},
CellFrameMargins → {{0, 0}, {0, 3}},
CellFrameLabels → {{PaneBox[
  FrameBox[StyleBox["Automation",
    FontFamily → "Helvetica", FontSize →
      9, FontColor → GrayLevel[1],
    FontWeight → Plain], Background →
    RGBColor[0.811765`, 0.117647`,
      0.145098`], BoxFrame → 0,
  FrameStyle → None, FrameMargins →
    {{3, 3}, {1, 1}}], ImageSize → 56,
  Alignment → Left, FrameMargins → 0],
  None}, {None, None}}}],
Cell[StyleData["AutomationMathCaption",
  "Presentation"], CellMargins →
{{30, 12}, {12, 12}}, FontSize → 20],
Cell[StyleData["AutomationMathCaption",
  "SlideShow"], CellMargins →
{{30, 12}, {12, 12}}]], Closed]],
Cell[CellGroupData[{Cell[StyleData[
  "Comment", StyleDefinitions →
    StyleData["Text"]], CellMargins →
{{0, 12}, {2, 24}}, CellFrameMargins →
{{0, 0}, {0, 3}}, CellFrameLabels →
{{PaneBox[FrameBox[StyleBox["Comment",
    FontFamily → "Helvetica", FontSize →
      9, FontColor → GrayLevel[1],
    FontWeight → Plain], Background →
    RGBColor[1.`, 0.647059`, 0],
  BoxFrame → 1, FrameStyle → RGBColor[
    1.`, 0.647059`, 0], FrameMargins →
    {{0, 0}, {0, 0}}], ImageSize → 56,
  Alignment → Left, FrameMargins → 0],
  None}, {None, None}}]}]
```

```
    {{3, 3}, {1, 1}}]], ImageSize -> 56,
    Alignment -> Left, FrameMargins -> 0],
    None}, {None, None}},

MenuSortingValue -> 2200, FontSize ->
14], Cell[StyleData["Comment",
"Presentation"], CellMargins ->
{{30, 12}, {12, 12}}, FontSize -> 16],
Cell[StyleData["Comment", "Slideshow"],
CellMargins -> {{30, 12}, {12, 12}},
FontSize -> 16]}, Closed]],

Cell[CellGroupData[{Cell[StyleData[
"DisplayFormula"], CellMargins ->
{{60, Inherited}, {Inherited,
Inherited}}], DefaultFormatType ->
DefaultInputFormatType,
HyphenationOptions ->
{"HyphenationCharacter" -> ":"},
LanguageCategory -> "Formula",
ScriptLevel -> 0, SingleLetterItalics ->
True, MenuSortingValue ->
1700, UnderoverscriptBoxOptions ->
{LimitsPositioning -> True},
StripStyleOnPaste -> True], Cell[StyleData[
"DisplayFormula", "Presentation"],
CellMargins -> {{120, Inherited},
{1.75` Inherited, 1.75` Inherited}},
LineSpacing -> {1, 5}, FontFamily ->
"Georgia", FontSize -> 20],
Cell[StyleData["DisplayFormula",
"SlideShow"]}], Closed]]}, Open]],

Cell[CellGroupData[{Cell["Styles for Items",
"Section"],

Cell[CellGroupData[{Cell[StyleData["Item"],
CellDingbat -> "» ", LineSpacing ->
```

```
{1.5` , 0} , MenuSortingValue → 2700 ,
FontFamily → "Georgia" , FontSize →
18 , FontColor → GrayLevel[0.2`]] ,
Cell[StyleData["Item", "Presentation"] ,
CellMargins → {{116, 20}, {12, 12}} ,
FontFamily → "Georgia" , FontSize → 20] ,
Cell[StyleData["Item", "SlideShow"]]],

Closed]], Cell[CellGroupData[
{Cell[StyleData["ItemParagraph"] ,
MenuSortingValue → 2710 , FontFamily →
"Georgia" , FontSize → 18 , FontColor →
GrayLevel[0.2`]] , Cell[StyleData[
"ItemParagraph", "Presentation"] ,
CellMargins → {{120, 90}, {12, 12}} ,
LineSpacing → {1.25` , 0} , FontFamily →
"Georgia" , FontSize → 20] ,
Cell[StyleData["ItemParagraph",
"SlideShow"]]], Closed]],

Cell[CellGroupData[{Cell[StyleData[
"ItemNumbered"] , LineSpacing →
{1.5` , 0} , MenuSortingValue → 2720 ,
FontFamily → "Georgia" , FontSize →
18 , FontColor → GrayLevel[0.25`]] ,
Cell[StyleData["ItemNumbered",
"Presentation"] , CellMargins →
{{116, 20}, {12, 12}} , FontFamily →
"Georgia" , FontSize → 20] ,
Cell[StyleData["ItemNumbered",
"SlideShow"]]], Closed]],

Cell[CellGroupData[{Cell[StyleData[
"Subitem"] , CellDingbat →
"» " , LineSpacing → {1.5` , 0} ,
MenuSortingValue → 2730 , FontFamily →
"Georgia" , FontSize → 16 , FontColor →
```

```
GrayLevel[0.3`]], Cell[StyleData[
  "Subitem", "Presentation"],
CellMargins → {{136, 20}, {10, 10}},
FontFamily → "Georgia", FontSize → 21],
Cell[StyleData["Subitem",
  "SlideShow"]}], Closed]],
Cell[CellGroupData[{Cell[StyleData[
  "SubitemParagraph"], LineSpacing →
{1.5`, 0}, MenuSortingValue → 2740,
FontFamily → "Georgia", FontSize →
16, FontColor → GrayLevel[0.3`]],
Cell[StyleData["SubitemParagraph",
  "Presentation"], CellMargins →
{{136, 90}, {10, 8}}, FontFamily →
"Georgia", FontSize → 18],
Cell[StyleData["SubitemParagraph",
  "SlideShow"]}], Closed]],
Cell[CellGroupData[{Cell[StyleData[
  "SubitemNumbered"], LineSpacing →
{1.5`, 0}, MenuSortingValue → 2750,
FontFamily → "Georgia", FontSize →
16, FontColor → GrayLevel[0.3`]],
Cell[StyleData["SubitemNumbered",
  "Presentation"], CellMargins →
{{136, 20}, {10, 10}}, FontFamily →
"Georgia", FontSize → 18],
Cell[StyleData["SubitemNumbered",
  "SlideShow"]}], Closed]]},
Closed]], Cell[CellGroupData[{Cell["Styles for Input and Output",
  "Section"],
Cell[CellGroupData[{Cell[StyleData[
  "Input"], MenuSortingValue → 2020,
MenuCommandKey → "9", FontSize → 18],
```

```
Cell[StyleData["Input", "Presentation"],
  CellMargins → {{120, 10}, {7, 12}},
  FontSize → 18], Cell[StyleData[
  "Input", "SlideShow"]]], Closed]],
Cell[CellGroupData[{Cell[StyleData[
  "CellLabel"], CellLabelMargins →
  {{12, Inherited}, {Inherited,
    Inherited}}}, LanguageCategory → None,
  StyleMenuListing → None, FontFamily →
  "Helvetica", FontSize → 9, FontColor →
  RGBColor[0.269993`, 0.308507`, 0.6`]],
  Cell[StyleData["CellLabel",
  "Presentation"], CellMargins →
  {{12, Inherited}, {1.5` Inherited,
    1.5` Inherited}}}, FontSize → 12],
  Cell[StyleData["CellLabel", "SlideShow"],
  CellMargins → {{12, Inherited},
    {1.5` Inherited, 1.5` Inherited}},
  FontSize → 12]], Closed]],
Cell[CellGroupData[{Cell[StyleData[
  "WolframAlphaShort"], FontSize → 18],
  Cell[StyleData["WolframAlphaShort",
  "Presentation"], CellMargins →
  {{120, 10}, {7, 12}}, FontSize → 18],
  Cell[StyleData["WolframAlphaShort",
  "SlideShow"]]], Closed]],
Cell[CellGroupData[{Cell[StyleData[
  "WolframAlphaShortInput"],
  FontSize → 18], Cell[StyleData[
  "WolframAlphaShortInput",
  "Presentation"], CellMargins →
  {{120, 10}, {7, 12}}, FontSize → 18],
  Cell[StyleData["WolframAlphaShortInput",
  "SlideShow"]]], Closed]]]
```

```
Cell[CellGroupData[{Cell[StyleData[
    "WolframAlphaLong"], FontFamily ->
    "Helvetica", FontSize -> 18],
  Cell[StyleData["WolframAlphaLong",
    "Presentation"], CellMargins ->
    {{120, 10}, {7, 12}}, FontSize -> 18],
  Cell[StyleData["WolframAlphaLong",
    "SlideShow"]}], Closed]],
Cell[CellGroupData[{Cell[StyleData[
    "WolframAlphaLongInput"], FontSize -> 18],
  Cell[StyleData["WolframAlphaLongInput",
    "Presentation"], CellMargins ->
    {{120, 10}, {7, 12}}, FontSize -> 18],
  Cell[StyleData["WolframAlphaLongInput",
    "SlideShow"]}], Closed]],
Cell[CellGroupData[{Cell[StyleData[
    "Output"], MenuSortingValue ->
    2030, FontSize -> 18], Cell[StyleData[
    "Output", "Presentation"], CellMargins ->
    {{120, 10}, {7, 12}}, FontSize -> 18],
  Cell[StyleData["Output", "SlideShow"]}], Closed]], Cell[CellGroupData[
{Cell[StyleData["Print"], FontSize -> 18],
  Cell[StyleData["Print", "Presentation"],
    CellMargins -> {{120, 10}, {7, 12}},
    FontSize -> 18], Cell[StyleData[
    "Print", "SlideShow"]}], Closed]],
Cell[StyleData["MSG"], FontSize -> 16}],
Closed]], Cell[CellGroupData[
{Cell["Styles of Links", "Section"],
  Cell[StyleData["Link", "SlideShow"],
    FontSize -> 21],
  Cell[StyleData["SearchLink",
    StyleDefinitions -> StyleData["Link"]]]],
```

```
Cell[StyleData["FunctionLink"]],  
Closed]], Cell[CellGroupData[  
{Cell["Special Styles", "Section"],  
Cell[CellGroupData[  
{Cell[StyleData["Picture"],  
CellMargins -> {{100, 100}, {20, 20}},  
ShowStringCharacters -> False,  
MenuSortingValue -> 5000, Magnification ->  
1], Cell[StyleData["Picture",  
"Presentation"], CellMargins ->  
{{100, 100}, {20, 20}}, Magnification ->  
1], Cell[StyleData["Picture",  
"SlideShow"]]}, Closed]],  
Cell[CellGroupData[{Cell[StyleData[  
"PictureCaption", StyleDefinitions ->  
StyleData["Text"]], CellDingbat -> "▲",  
CellMargins -> {{114, 100}, {15, 4}},  
ShowStringCharacters -> False,  
MenuSortingValue -> 5100, FontSize ->  
14, FontColor -> GrayLevel[0.3`]],  
Cell[StyleData["PictureCaption",  
"Presentation"], CellMargins ->  
{{114, 100}, {20, 4}}, FontSize -> 16],  
Cell[StyleData["PictureCaption",  
"SlideShow"], CellMargins -> {{114, 100},  
{20, 4}}, FontSize -> 16]}, Closed]],  
Cell[CellGroupData[{Cell[StyleData[  
"OverviewTitle"], CellFrame -> None,  
CellMargins -> {{100, 100}, {20, 60}},  
FontFamily -> "Calibri", FontSize ->  
24, FontWeight -> "Bold", FontColor ->  
GrayLevel[0.4`]], Cell[StyleData[  
"OverviewTitle", "Presentation"],  
CellFrame -> None, CellMargins ->
```

```
 {{100, 100}, {20, 60}], FontFamily ->
  "Calibri", FontSize -> 24, FontWeight ->
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Cell[StyleData["OverviewTitle",
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CellMargins -> {{120, 100}, {10, 10}},
FontFamily -> "Georgia", FontSize -> 22,
FontWeight -> Plain, FontColor -> RGBColor[
  0.811765`, 0.117647`, 0.145098`],
ReturnCreatesNewCell -> True], 

Cell[StyleData["OverviewSection",
  "Presentation"], CellFrame -> None,
CellMargins -> {{120, 100}, {10, 10}},
FontFamily -> "Georgia", FontSize -> 22,
FontWeight -> Plain, FontColor -> RGBColor[
  0.811765`, 0.117647`, 0.145098`],
ReturnCreatesNewCell -> True], 

Cell[StyleData["OverviewSection",
  "SlideShow"], CellFrame -> None,
CellMargins -> {{120, 100}, {10, 10}},
FontFamily -> "Georgia", FontSize -> 22,
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  0.811765`, 0.117647`, 0.145098`],
ReturnCreatesNewCell -> True]}, Open]],

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  {{90, 90}, {15, 0}}, FontSize -> 24],
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  "SlideShow"]}], Closed]],
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  FontSize -> 12,
  FontColor -> GrayLevel[1],
  ButtonBoxOptions ->
  {Background -> RGBColor[0.811765`, 0.117647`,
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  Cell[StyleData["Program",
  "SlideShow"], CellMargins -> {{116, 48},
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  ShowCellBracket ->
  Automatic, CellMargins -> {{24, 10},
    {6, 6}}, CellBracketOptions -> {"Color" ->
    RGBColor[0.786999`, 0.0386053`,
      0.0571756`]}, CellFrameLabels ->
    {{Cell[TextData[{"Edit:"}], FontFamily ->
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      FontWeight -> "Bold", CellBaseline ->
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  Hyphenation -> True, LineSpacing -> {1, 3},
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(64-bit) (February 23, 2011)",
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