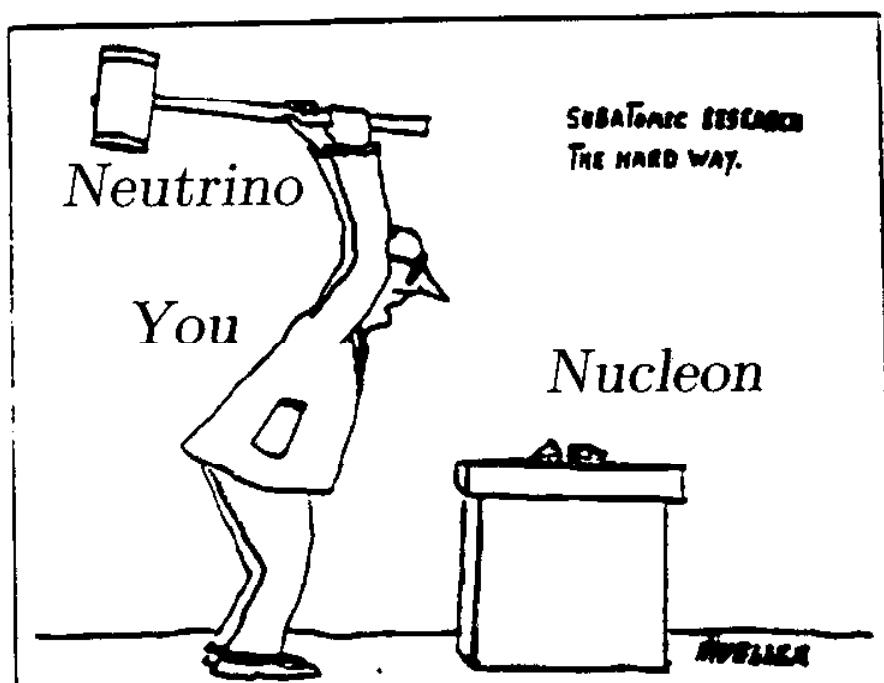


Structure Functions from CCFR

- Introduction
- What Does Neutrino DIS Measure?
 - Structure Functions
 - Charged-Lepton Comparisons
 - $x > 1$
- Future Prospects



DIS 97
Chicago, IL
15 April 1997

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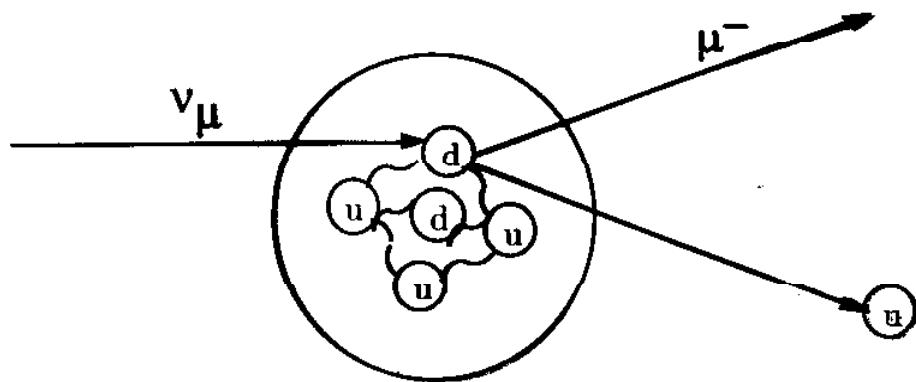
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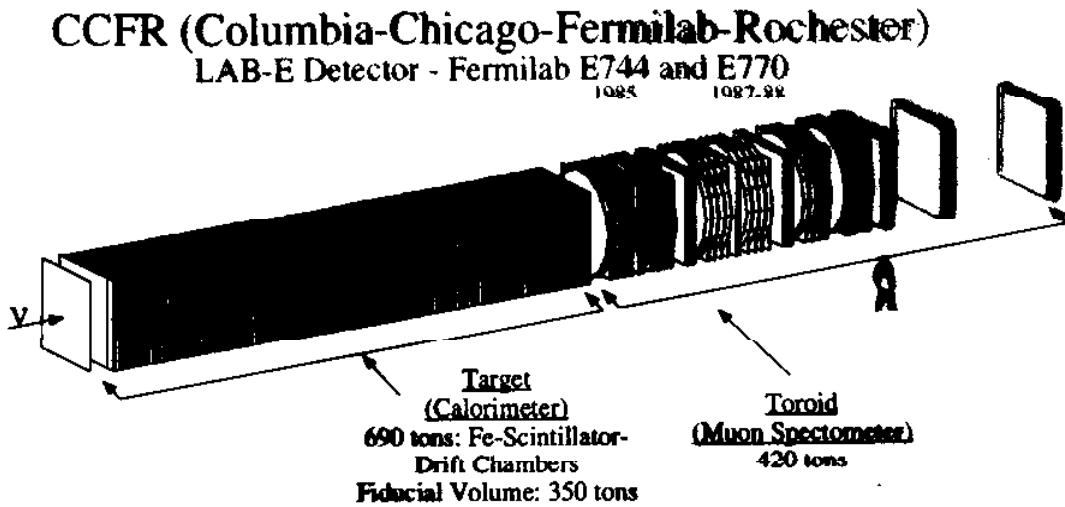
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What Do We Need to Use Neutrinos?



$$\sigma(\nu N) = 0.67 \times 10^{-38} \text{ cm}^2/\text{GeV}$$

- Intense Neutrino Beam
- High Mass Target (hundreds of tons)
- Detector Which Measures Decay Fragments
 - hadron energy
- Something to Measure Muon Momentum



- 950562 ν_μ and 169114 $\bar{\nu}_\mu$ After All Cuts
- $\Delta p_\mu/p_\mu = 0.10$ Independent of Momentum
- $\sigma/E = 0.847/\sqrt{E_{\text{Had}}} + 0.30/E$

How Are the Cross-Sections Expressed?

- Useful Because Universal and Easily Compared Among Probes:
photons, muons, neutrinos
- “Lagrangian” Representation of What Neutrino Sees:

$$\sigma \propto L_{\mu\nu} W^{\mu\nu}$$

$$W^{\mu\nu} = (-g_{\mu\nu} + \frac{q_\mu q_\nu}{q^2})W_1 + \frac{1}{M}(p_\mu - \frac{p \cdot q}{q^2}q_\mu)(p_\nu - \frac{p \cdot q}{q^2}q_\nu)W_2$$

$$+ i\epsilon_{\mu\nu\alpha\beta} \frac{p^\alpha q^\beta}{2M} W_3$$

with $F_1 = M W_1$, $F_2 = \nu W_2$, $F_3 = \nu W_3$.

- Parton Version of What Neutrino Sees:

$$2x F_1 = xq(x) + x\bar{q}(x)$$

$$F_2 = xq(x) + x\bar{q}(x) + xk(x)$$

$$xF_3 = xq(x) - x\bar{q}(x)$$

(this definition depends on order of QCD calculation.)

- And the Cross-Sections Become

$$\frac{d^2\sigma}{dx dy}|_{\nu,\bar{\nu}} = \frac{G_F^2 M E}{\pi} \left[\left(1 - y - \frac{Mxy}{2E}\right) F_2 + \frac{y^2}{2} 2x F_1 \pm \left(y - \frac{y^2}{2}\right) x F_3 \right]$$

What's So Special About xF_3 ?

- $xF_3 \propto q - \bar{q}$ Independent of Sea
(well, almost)
- xF_3 Is Different for $\nu, \bar{\nu}$

$$xF_3(\nu) = x(u_\nu(x) + d_\nu(x)) + \frac{2}{3} s(v) = x^2$$

$$xF_3(\bar{\nu}) = x(u_{\bar{\nu}}(x) + d_{\bar{\nu}}(x)) + \frac{2}{3} s(v) = s(x)$$

- We report

$$xF_3 \approx \frac{xF_3(\nu) + xF_3(\bar{\nu})}{2}$$

$$= x(u_\nu(x) + d_\nu(x))$$

- Independent of Sea for Evolution Equations.
But ...
- Dependent on AntiNeutrino Statistics

Experimental Method

- Determine the $\bar{\nu}/\nu$ Flux Ratio

$$N(\nu) \propto \int dE \Phi(\nu, E) \times \sigma(\nu, E)$$

$$N(\bar{\nu}) \propto \int dE \Phi(\bar{\nu}, E) \times \sigma(\bar{\nu}, E)$$

- But as $y = E_H/E_\nu \rightarrow 0$

$$\sigma(\nu, E) = \sigma(\bar{\nu}, E) \propto (q + \bar{q})$$

- *The Same!!*

- So

$$\frac{\Phi(\bar{\nu}, E)}{\Phi(\nu, E)} = \frac{\frac{N(\bar{\nu}, E)}{\sigma(\bar{\nu}, E)}}{\frac{N(\nu, E)}{\sigma(\nu, E)}} = \frac{N(\bar{\nu}, E)}{N(\nu, E)}$$

- Which Gives Us the “Relative” Flux
 - Relative $\bar{\nu}/\nu$ vs. Energy
 - Absolute Cross-Section from External Data

Extraction of Structure Functions

- Within an x, Q^2 bin

$$\begin{aligned} N^\nu(x, Q^2) &= A_\nu F_2(x, Q^2) + B_\nu x F_3(x, Q^2) \\ N^\bar{\nu}(x, Q^2) &= A_{\bar{\nu}} F_2(x, Q^2) + B_{\bar{\nu}} x F_3(x, Q^2) \end{aligned}$$

- Where A, B are functions of
 - Relative Flux
 - Measured Kinematic Variables
 - R_{QCD}
- But Changing SFCNS changes Relative Flux,
Through Resolution Smearing
- So Iterate:

$$\Phi \Leftrightarrow F_2, x F_3$$

Department of Corrections

- Physics Model Corrections

$$\text{corr} = \text{corr}^{\text{isoscalar}} \times \text{corr}^{\text{radiative}} \\ \times \text{corr}^{\text{charmmass}} \times \text{corr}^{\text{propagator}}$$

- These do not use external parton distributions — we iterate on F_2, xF_2 until changes are small.
- Use LO Buras-Gaemers model

$$\frac{\sigma(\text{LO, physical Fe target})}{\sigma(\text{LO, bare proton})} \approx \\ \frac{\sigma(\text{NLO, physical Fe target})}{\sigma(\text{NLO, bare proton})}$$

- Strange Sea Correction

So What Do We Report?

- F_2, xF_3 for
 - Isoscalar Target
 - No Strange Sea
 - Charm Mass = 0
 - (no slow-rescaling correction)
 - Remove Physical Radiative Corrections
 - Remove Propagator Q^2 Dependence
- Each Correction is Explicitly Given in
Seligman, PhD Thesis
Down to Code – so you can take it out if
you like

`ftp://inearl.news.columbia.edu/pub/~rseligman/afmdiv10s.f77`

Errors

- Statistical

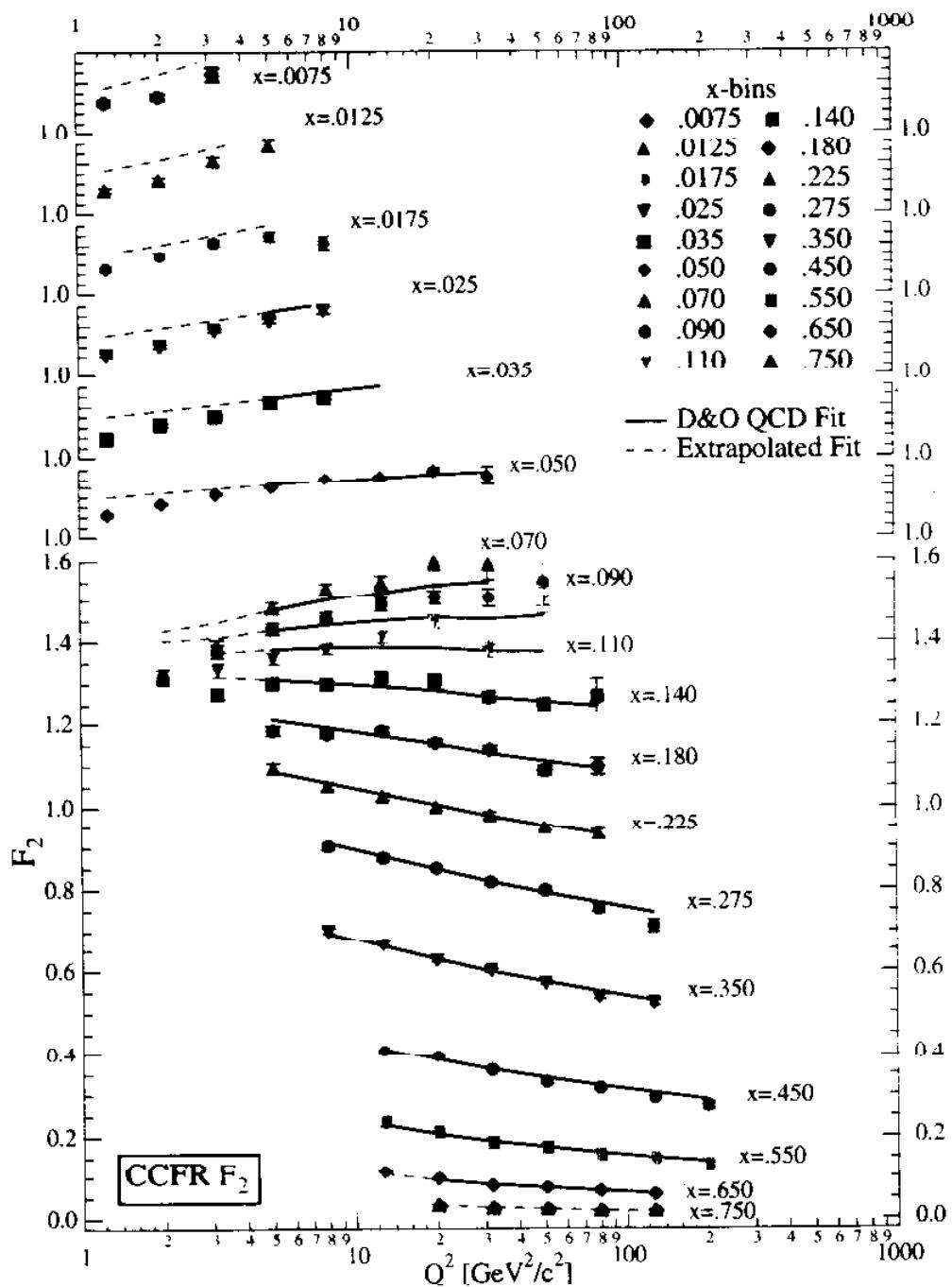
- Since Data Are the Same, ΔF_2 is Correlated with ΔxF_3

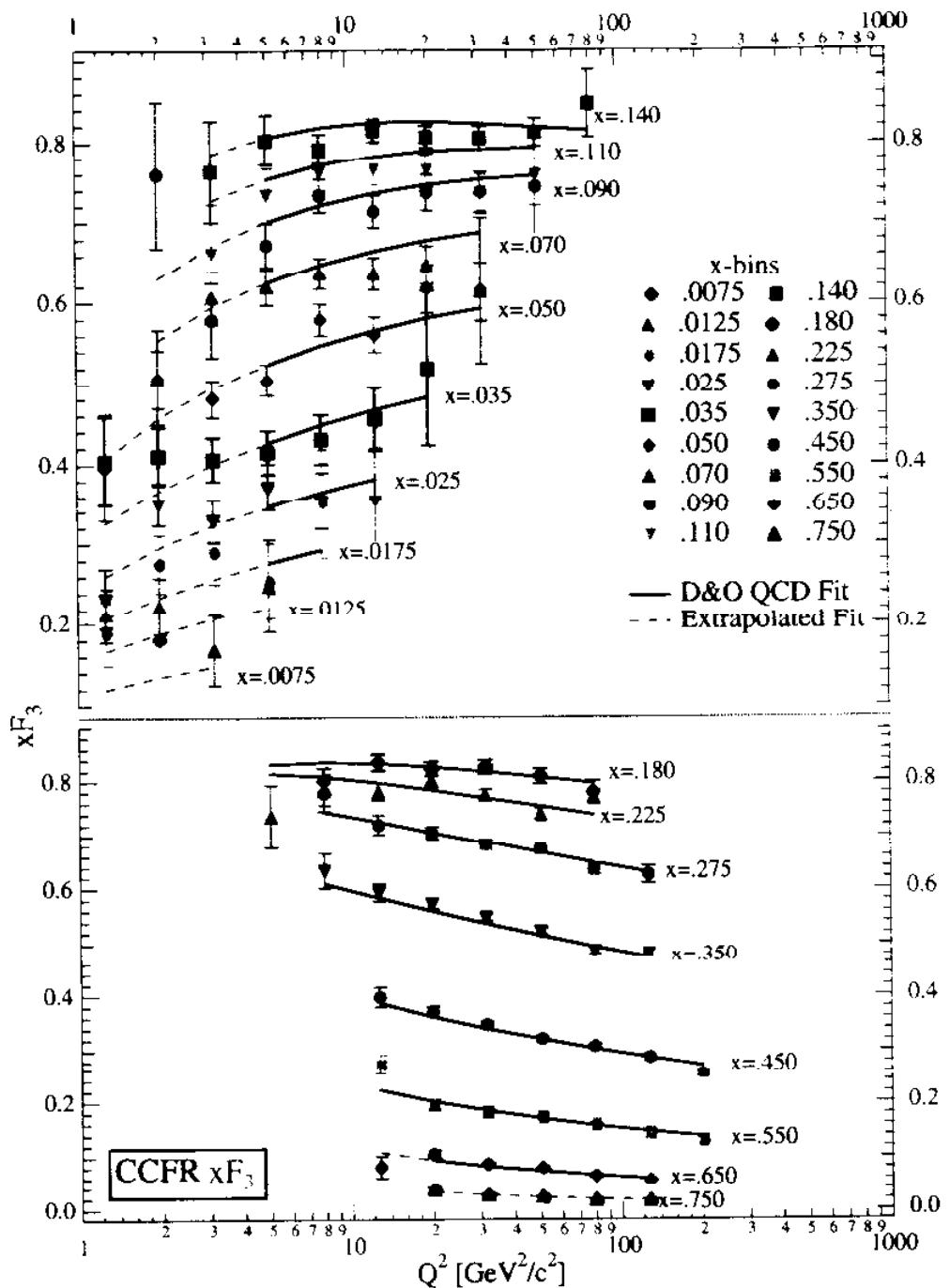
- Systematic

Treated as Additional Term in χ^2

- Hadron Energy Calibration
 - or more specifically, E_{Had}/p_μ
- Flux Extraction
 - quality of fits to $\sigma_\nu = \sigma_{\bar{\nu}}$ at $y = 0$
- Buras-Gaemers Model Parameterization
 - fits poorly at low x
- R_{QCD}, m_c , strange sea, . . .

	$\Delta \Lambda_{\overline{\text{MS}}} (\text{MeV})$
Statistical	42
Calibration/Energy Scale	64
Flux	21
Cross-Section	31
Buras-Gaemers “Model”	41
Remaining	21

F_2 

xF_3 

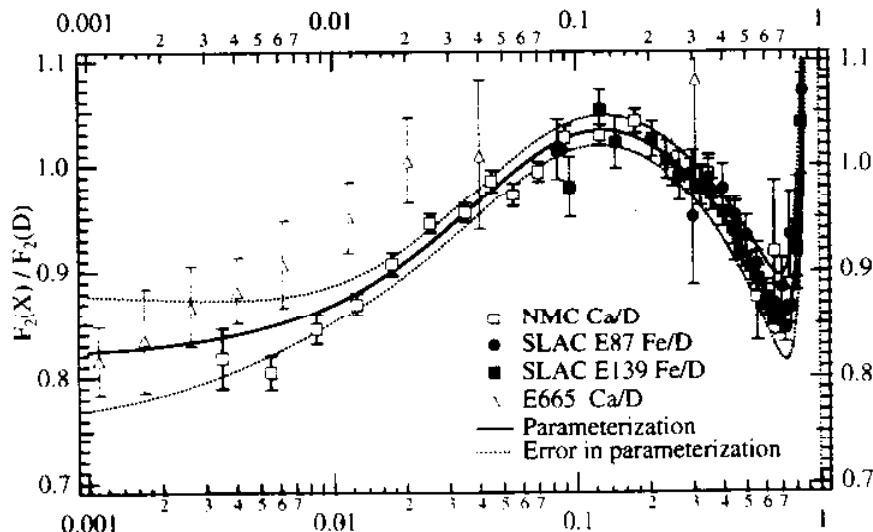
Comparison to Charged Lepton Experiment

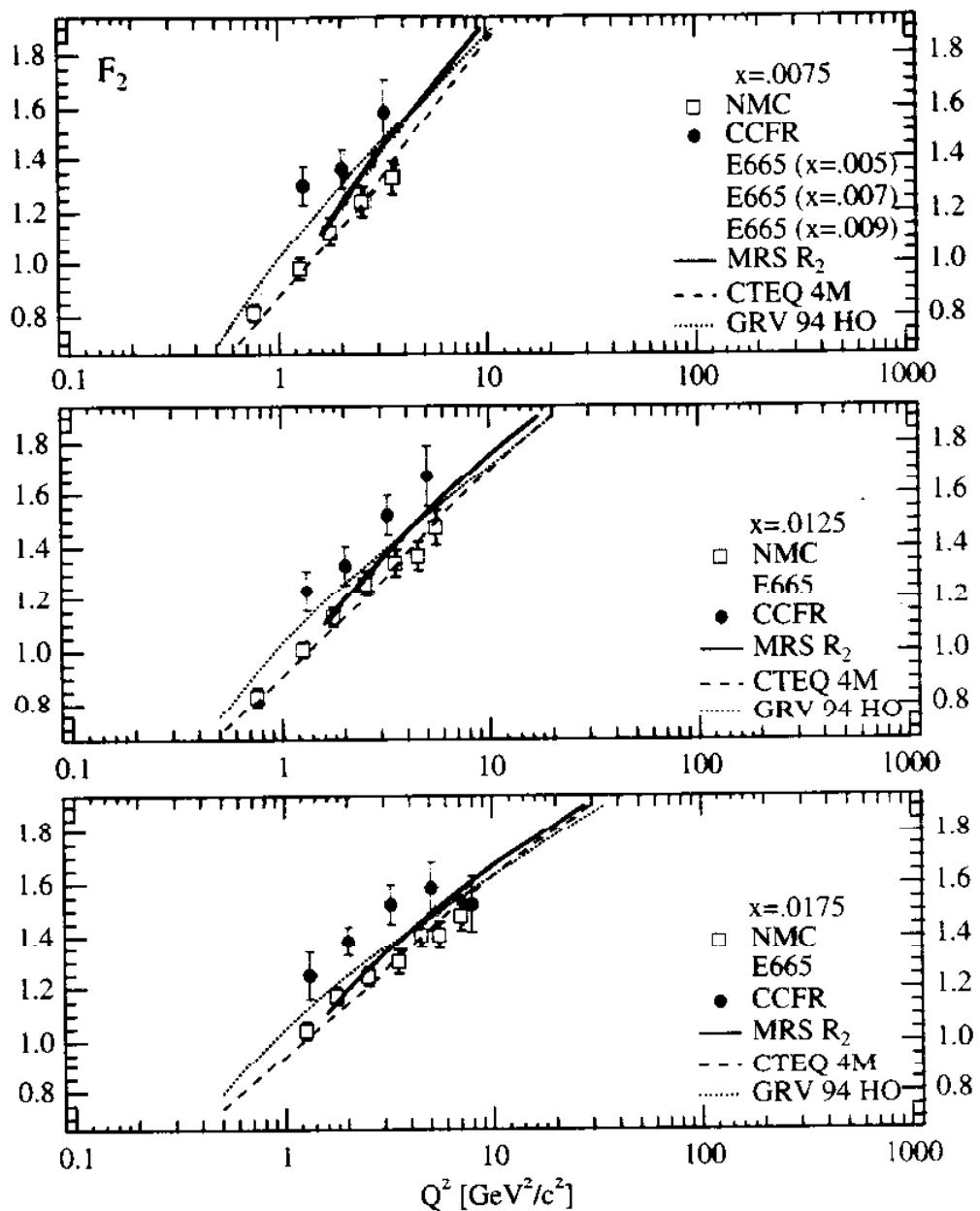
- Heavy Target Correction
- “5/18”ths Rule

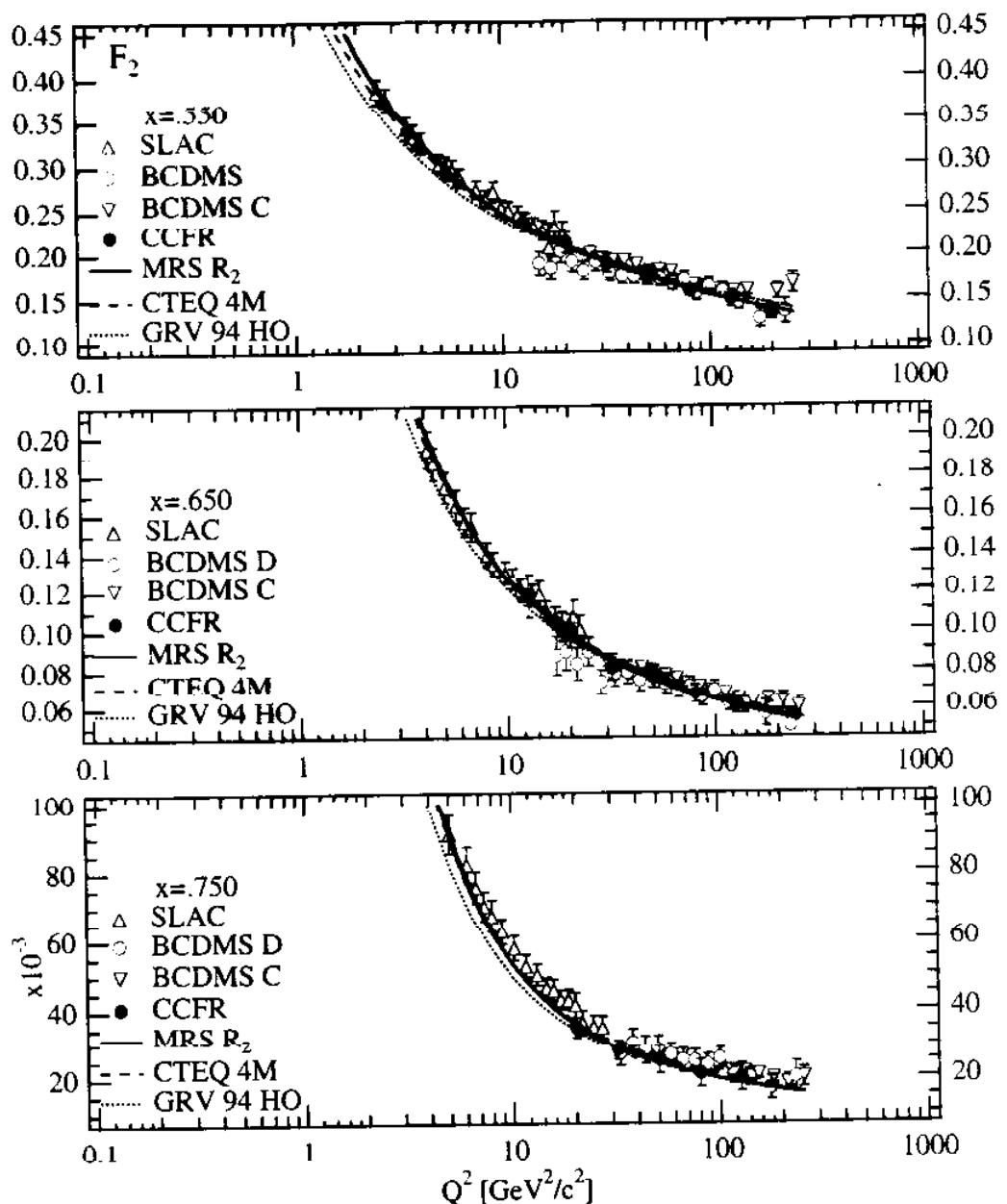
$$\frac{F_2^{\text{lepton}}}{F_2^\nu} = \frac{5}{18} \left[1 - \frac{3}{5} \left(\frac{s + s - c - \bar{c}}{q + \bar{q}} \right) \right]$$

—note this is *exact* in DIS scheme
 —use CTEQ4D, determined in DIS
 (and CTEQ charm sea)

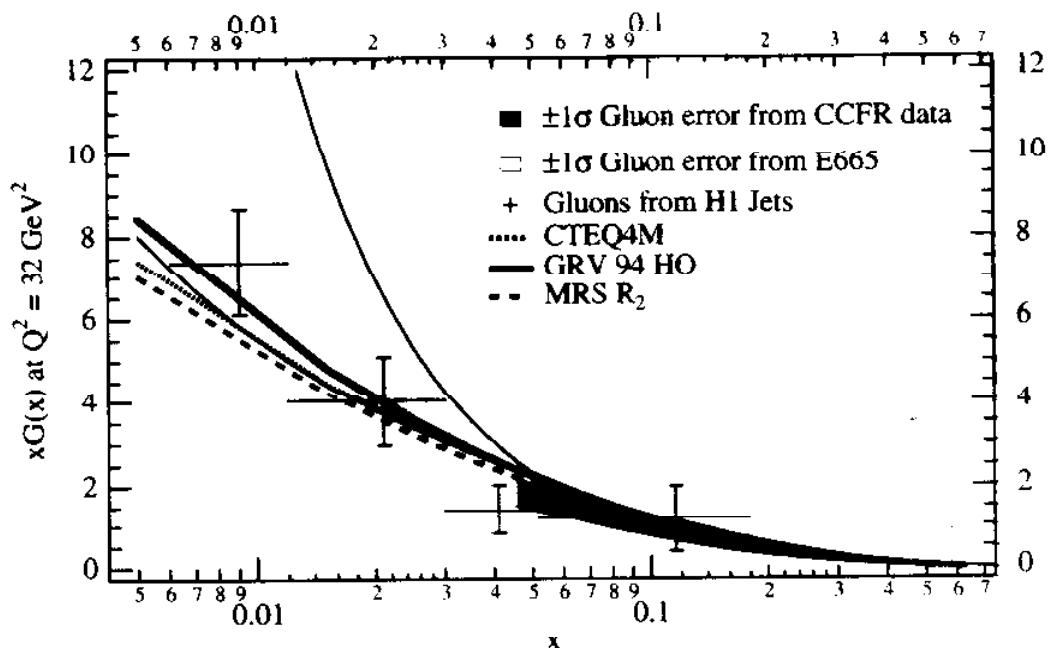
- Deviation at low- x , not Understood
- Small Deviation from SLAC/BCDMS at $x = 0.75$, probably Fermi motion





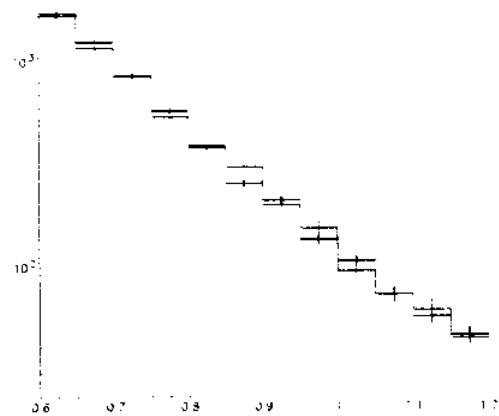
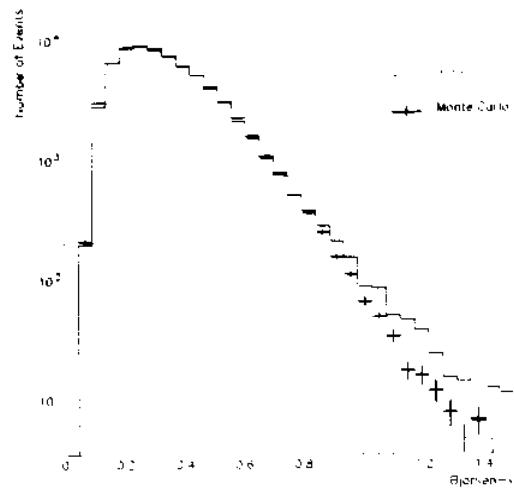


Gluon Distribution



- Cut so that $x > 0.045$ (best fit)
- Evolved or Extracted at $Q^2 = 32 \text{ GeV}^2$
- E665 Evolved from $Q^2 = 8 \text{ GeV}^2$

Collective Effects and $x > 1$



- Difference is Collective Effects from
*Strikman and Frankfurt, Phys. Rep. 160, 25(1988), Nikiforov
Phys. Rev. C22 700, (1980)*
- $s = 7.7 \pm 0.6$ CCFR Prelim (M. Vakili)
- SlacE133 $s = 7.8$, BCDMS $S = 16.5 \pm 0.5$

'S' from different sources:

$$F_2(x, Q^2) = F_2^f(0.75 \dot{+} Q^2) \cdot \exp[S(x - 0.75)]$$

$S \approx 8 - 9$ FNCM Strikman & Frankfurt
Phys. Rep. 160 1988 325

$S \approx 7 - 8$ Al ($e e'$) SLAC E133
S. Rock

$S \approx 6$ Nikiforov
Phys. Rev. C22 1980 700

$S = 16.5 \pm 0.5$ BCDMS μC
Z. Phys. C63 29-36 1994

$S = 7.7 \pm 0.6$ CCFR preliminary

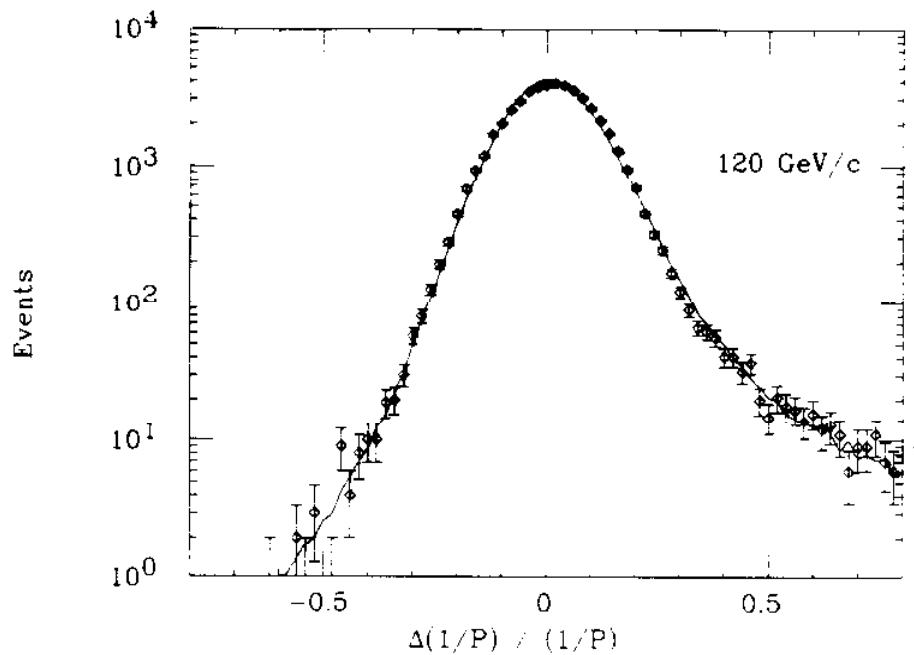
Conclusions

- New νN DIS Structure Function Determination
- Improved Systematic Errors on Muon Calibration \Rightarrow Changed Results
- Charged-Lepton Discrepancy
- $x > 1$ Results

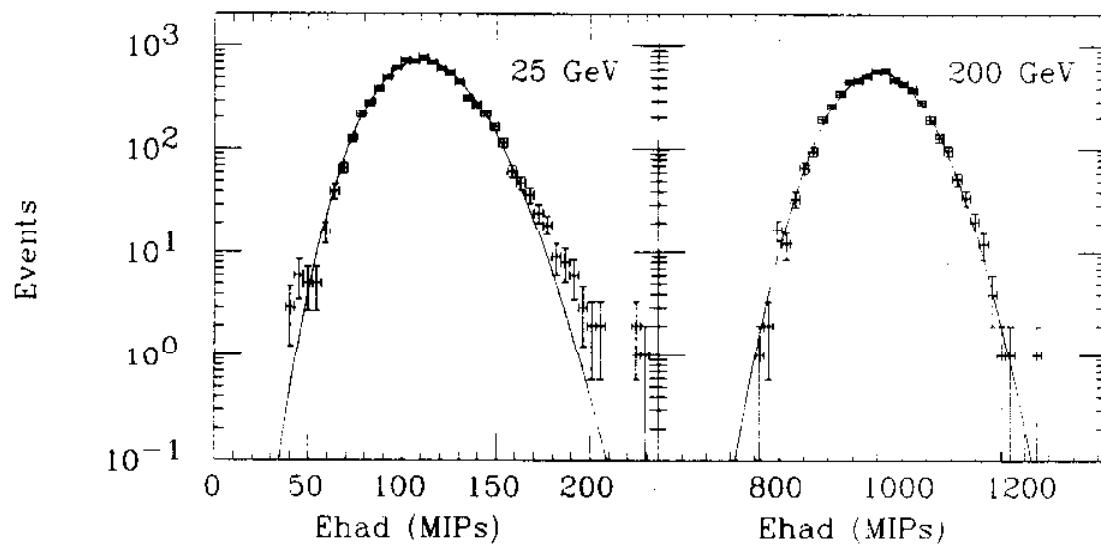
Future Prospects

- NuTeV in Data-Taking Now
- Same Statistical Power as This Data
- Improved Calibration $\times 3$ Reduction in Systematic Error from Muon Calibration
- Better $\alpha_S, \Lambda_{\bar{M}S}$

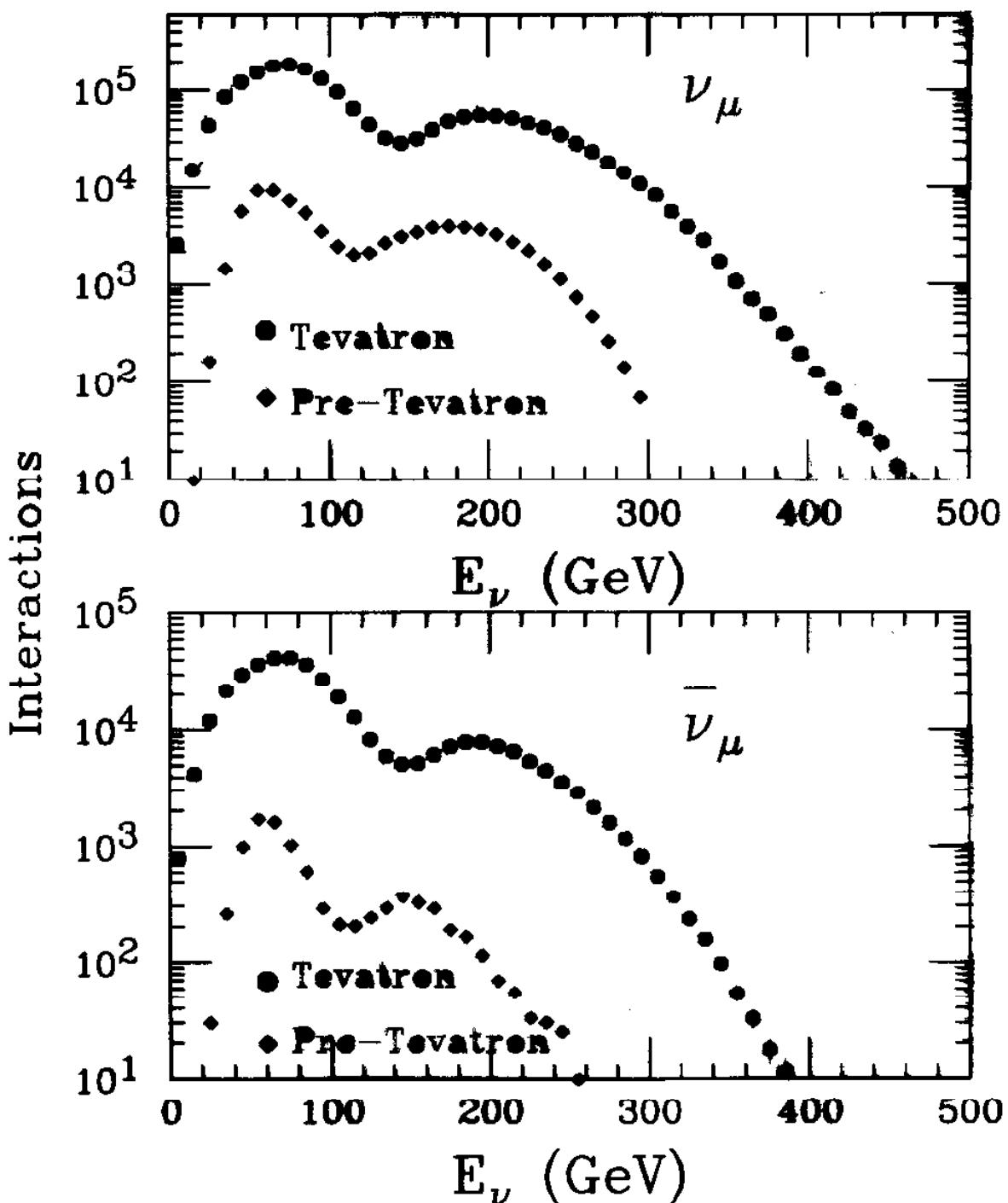
Muon Momentum Resolution



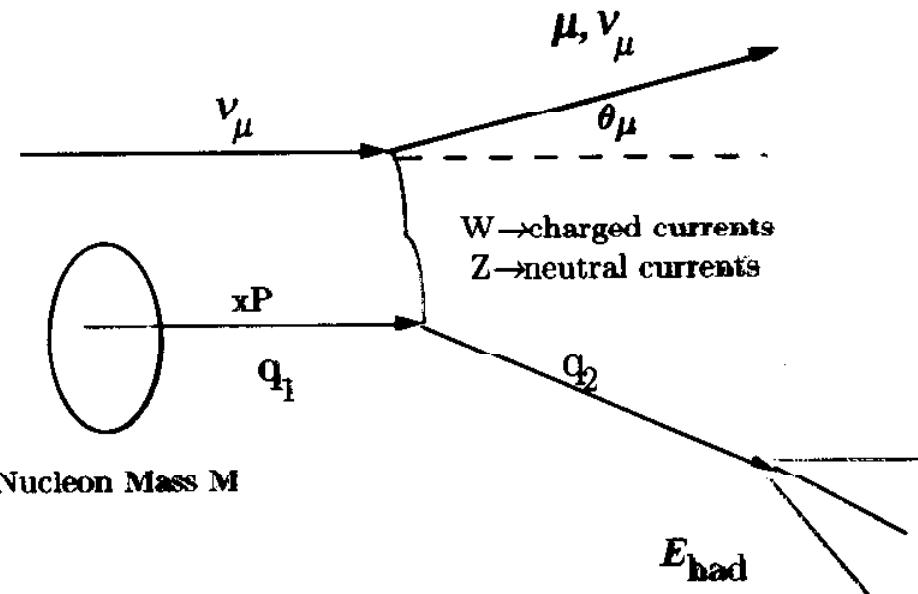
Hadron Energy Resolution



Neutrino Energy Spectrum: Tevatron vs. Pre-Tevatron



What Does A Neutrino Interaction Look Like to a Theorist?



Kinematic Variables:

$$y = E_{\text{had}}/E_\nu$$

— inelasticity

$$Q^2 = 4E_\nu E_\mu \sin^2 \frac{\theta}{2}$$

$= (4 - \text{momentum transfer})^2$

$$x = \frac{Q^2}{2ME_{\text{had}}}$$

$= \text{fractional momentum of struck quark}$