

F. Zomer

Q.C.D Fit, $F_2^{c\bar{c}}$ & F_L in H1 (already published topics)

- Fit Program used in H1
 - ➔ contents & numerical precision

- 1993 & 1994 H1 F_2 Fits
 - ➔ difficulties

- $F_2^{c\bar{c}}$ measurement
 - ➔ new informations

- F_L extraction

• Fit program.

- DGLAP eq. solved in x space

→ N.L.L.A kernels (\overline{MS})

- 6 Parton density functions are evolved.

$$\left. \begin{aligned} & \cdot g \\ & \cdot \Sigma = \sum_{i=1}^n (q_i + \bar{q}_i) \\ & \cdot UP^+ = u^+ + c^+ = (u + \bar{u} - \sum_{i=1}^n) + (c + \bar{c} - \sum_{i=1}^n) \\ & \quad (= u^+ \text{ if } n=3) \end{aligned} \right\} F_2^{l^+p}$$

$$\cdot \Delta^+ = u^+ - d^+ = (u + \bar{u}) - (d + \bar{d})$$

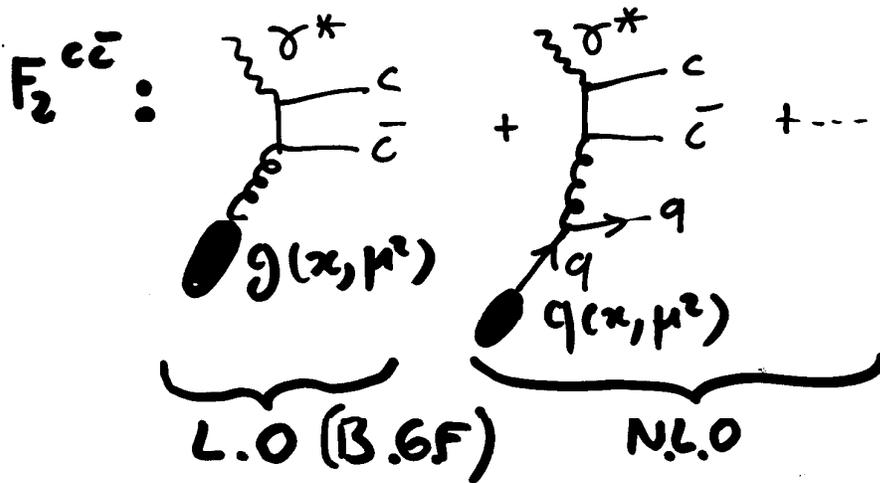
$$\left. \begin{aligned} & \cdot V^+ = u^+ + d^+ = u^v + d^v \\ & \cdot V^- = u^- + d^- = u^v - d^v \end{aligned} \right\} \begin{array}{l} \text{necessary for} \\ \text{HERA } \uparrow Q^2 \\ \text{X-section} \end{array}$$

- P.d.F \otimes L.O Wilson coefficients

→ $F_2^{l^+p}, F_2^{l^+n}, \dots$ For light partons

- HEAVY quarks

- Fixed Flavor Scheme : $n=3$ ("b=0")



(• Massless prescription)

- Numerical details

- x net equidistant in $\ln x$

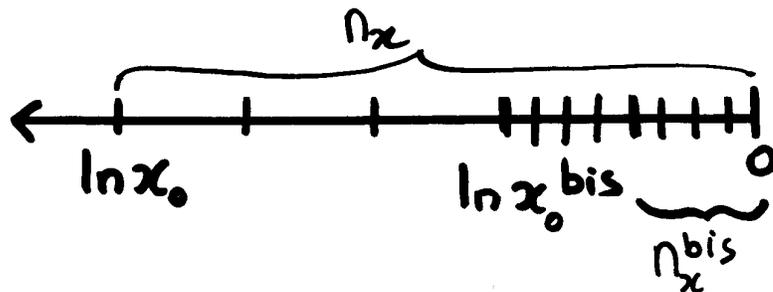
- P.d.F expanded using Lagrange (hat: basis functions \Leftrightarrow linear interpolation of pdf)

➔ DGLAP solution without truncated series.

↳ C.P.U $\propto n_x^2$ (instead of n_x^3)

- Precision improvement at high- x

➔ Second x -net introduced

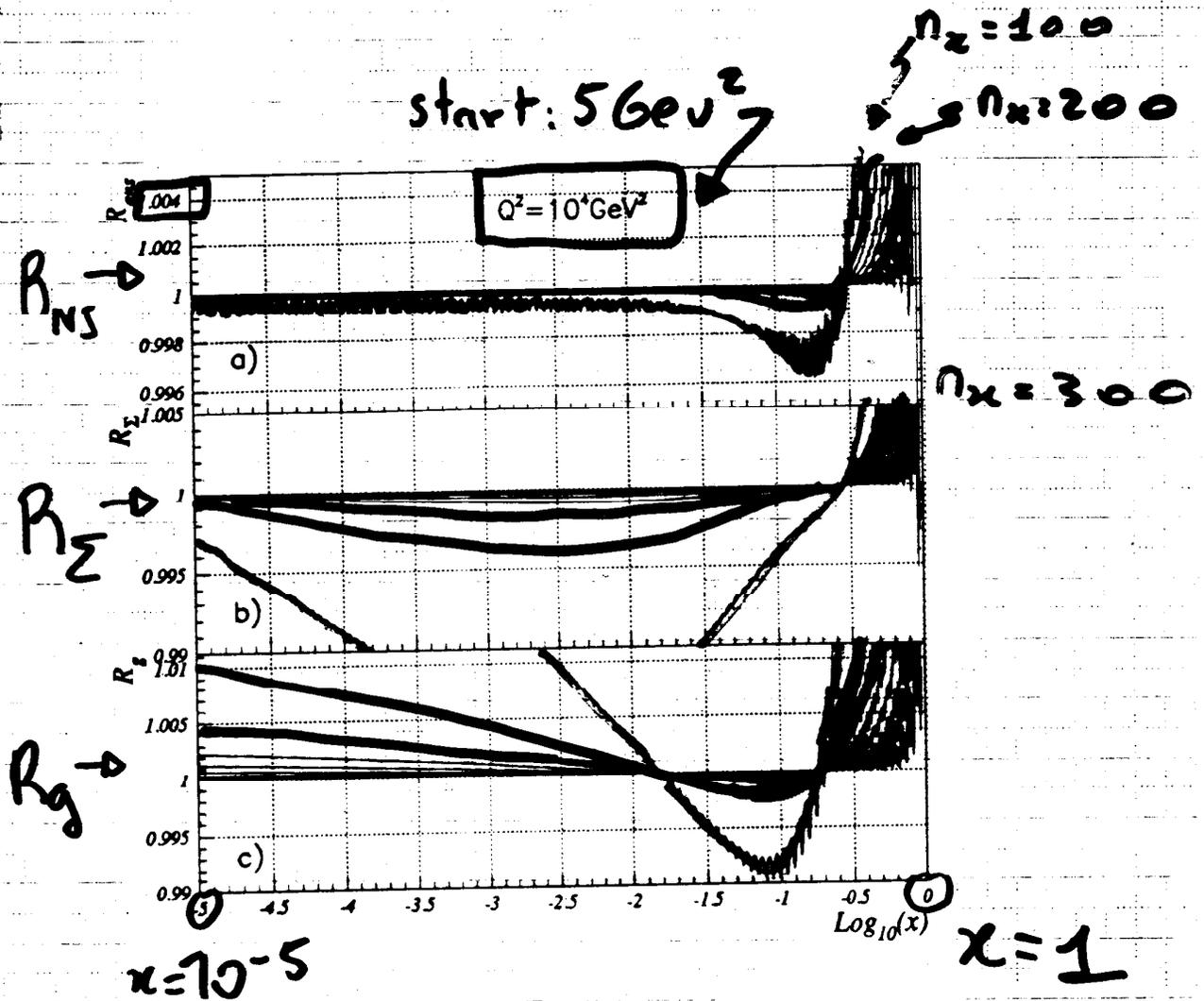


➔ for $x_0 = 10^{-5}$:

$n_x = 50, n_x^{bis} = 6$ → $n_x = 250, n_x^{bis} = 6$
minimum search Final result

$$R_{pdf} = \frac{P.d.f(n_x)}{P.d.f(n_x=900)} \leftarrow \text{less precise}$$

$$R_{pdf} = \frac{P.d.f(n_x=900)}{P.d.f(n_x=900)} \leftarrow \text{"more" precise}$$



$$n_x = 100$$

$$n_x = 200$$

$$n_x = 300$$

$$\frac{\vdots}{n_x = 900} \quad (R_{pdf} \approx 1)$$

• χ^2 definition

$$\chi^2 = \sum_{\text{exp, data}} \left(\frac{F_2^{\text{QCD}} - F_2^{\text{data}}}{\sqrt{\sigma_{\text{stat.}}^2 + \sigma_{\text{uncor.}}^2}} \right)^2 + \sum_i \Delta_i^2 + \sum_{\text{exp}} n_{\text{exp}}^2$$

• With

$\int_{\text{data}} (\Delta_i) = F_2$ relative shift induced by Δ_i standard deviations of the i^{th} syst.

n_{exp} = overall normalization standard deviation

• \Rightarrow IN H1 1993 & 1994 F_2 analysis:

• $\Delta_i \equiv 0$ (BUT $\frac{\partial \chi^2}{\partial \Delta_i} \neq 0 \Rightarrow$ error band)

• n_{exp} : fitted

- Gluon error band

$$\Delta G^{\pm} \Big|_{x_i, Q_i^2} = \left| G(\{P\}) - G(\{P. \pm \Delta P\}) \right|$$

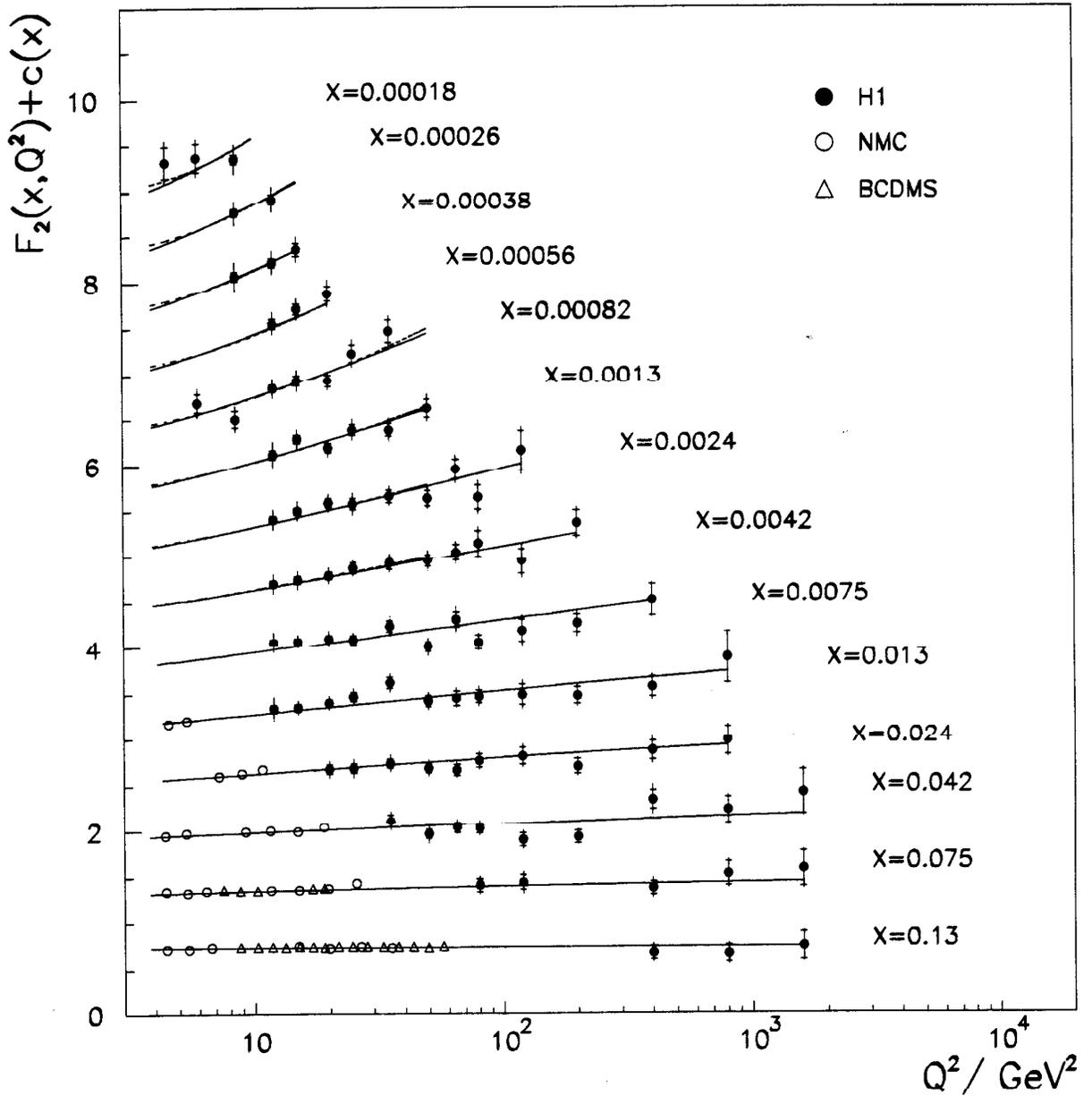
- with

$$\Delta P_i = \frac{[M^{-1} + \Pi^{-1} C C^T \Pi^{-1}] \frac{\partial \vec{G}}{\partial P}}{\sqrt{\frac{\partial \vec{G}}{\partial P} \cdot (\Pi^{-1} + \Pi^{-1} C C^T \Pi^{-1}) \frac{\partial \vec{G}}{\partial P}}}$$

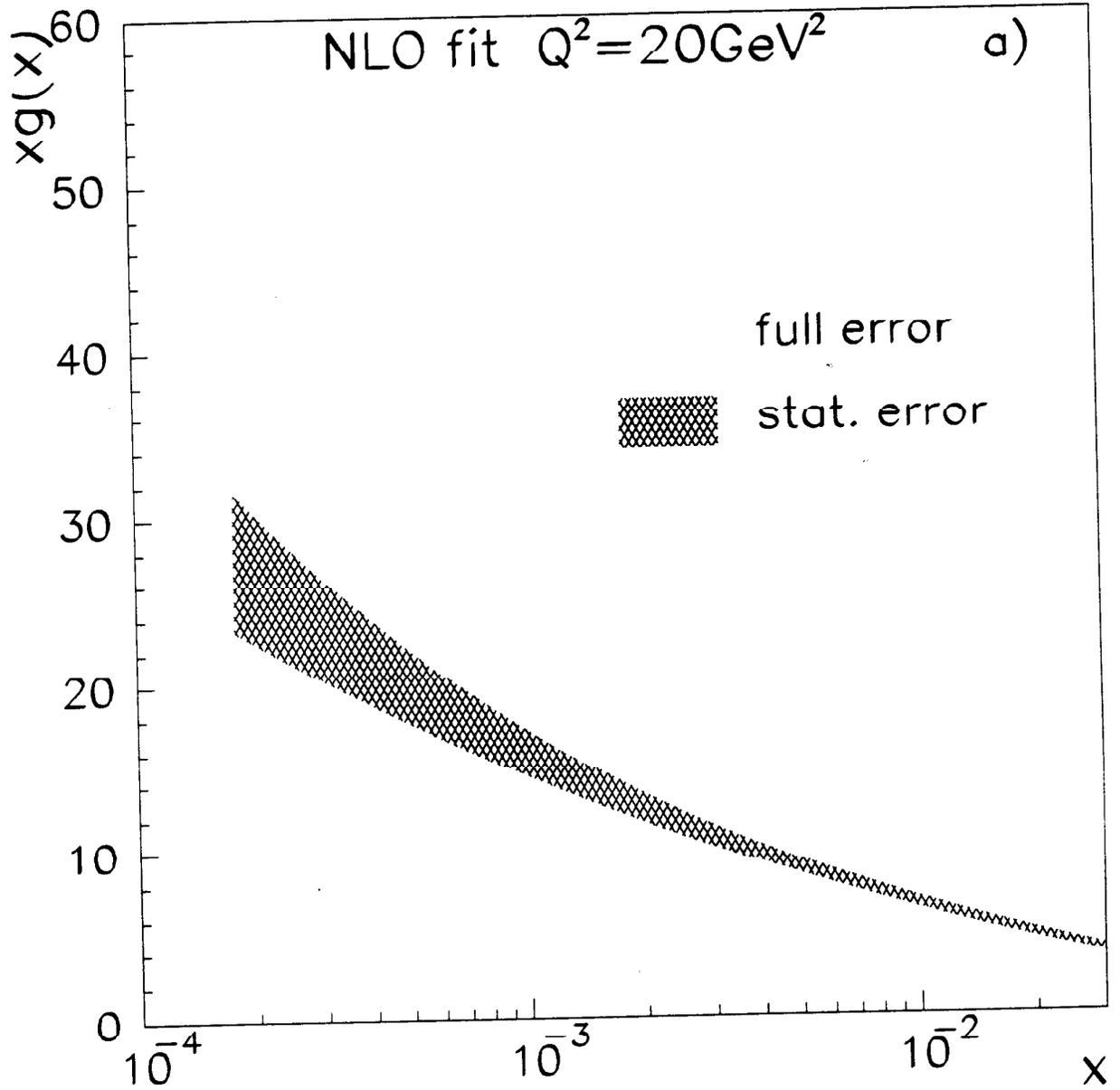
- $M_{ij} = \frac{1}{2} \frac{\partial^2 \chi^2}{\partial P_i \partial P_j}$; $C_{ij} = \frac{1}{2} \frac{\partial^2 \chi^2}{\partial P_i \partial Q_j}$
↳ systematics.

⇒ IF Q_i fitted; C does not exist.

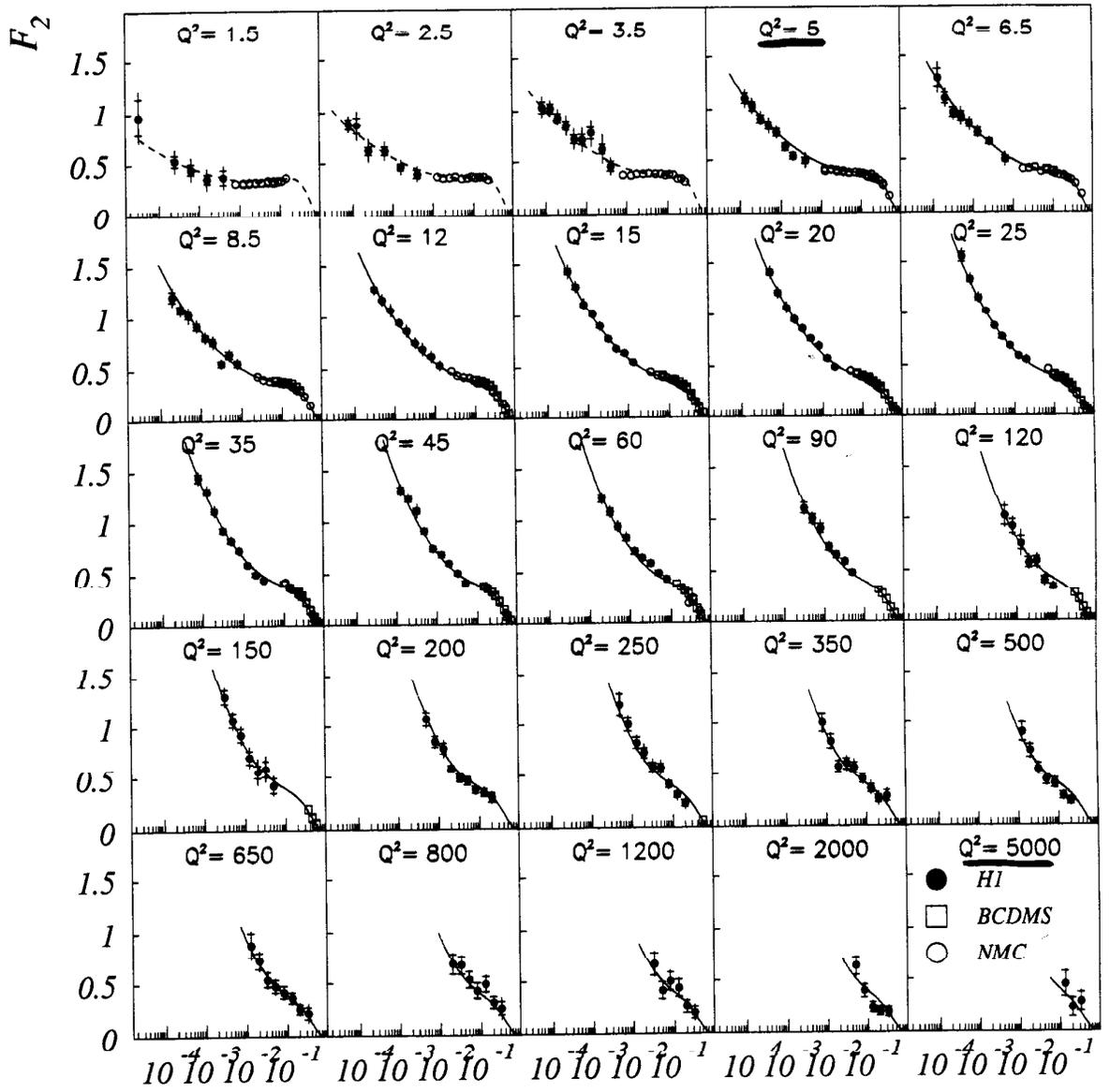
H1 1993 data analysis



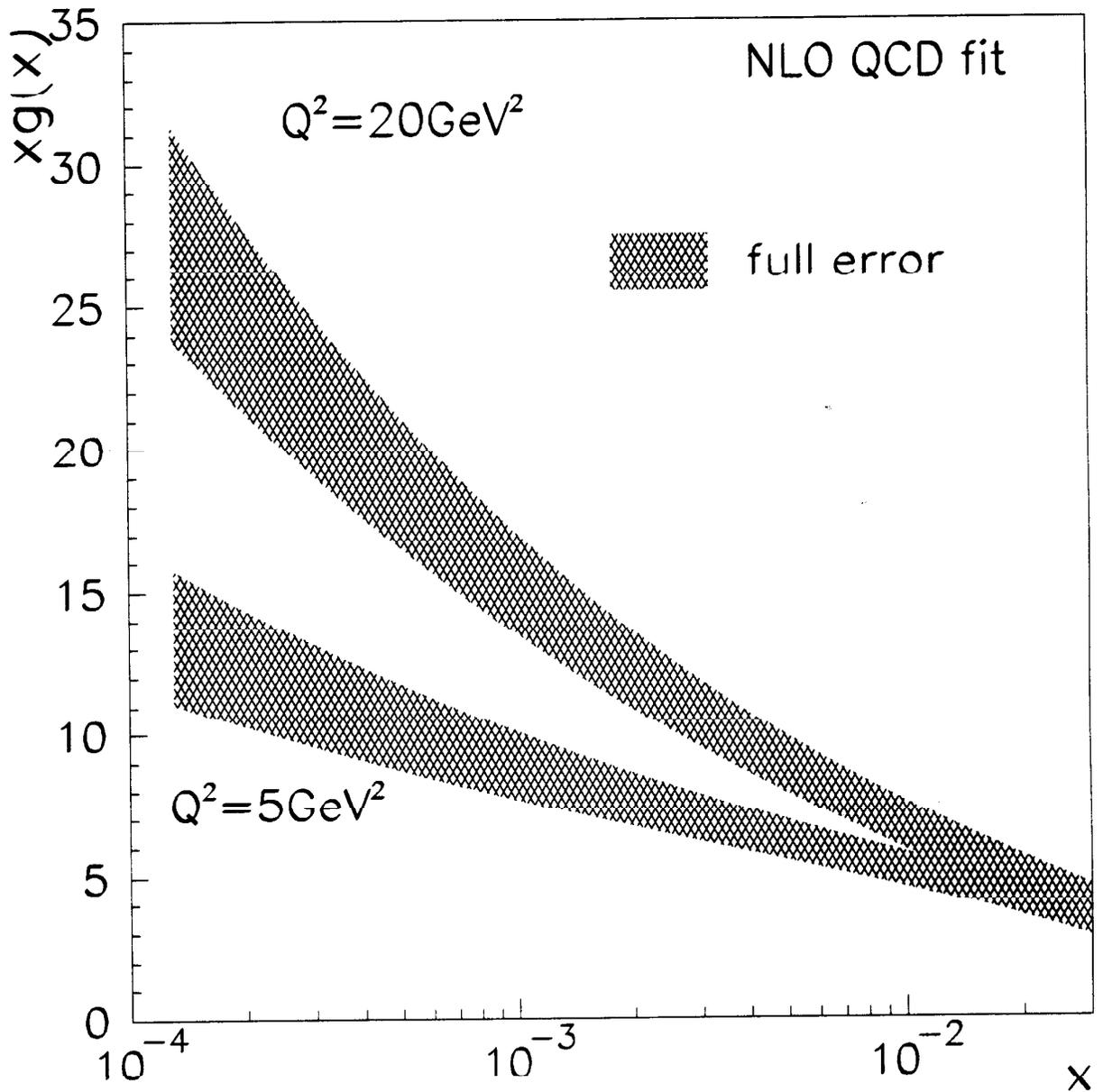
H1 1993 data analysis



H1 1994 data analysis



H1 1994 data analysis



● Difficulties

● 1993 analysis

● F_2^p data only

● xg , $x\Sigma$ & xU^+ parametrized at

$$Q_0^2 = 46 \text{ eV}^2 \quad \left(\Lambda_{\overline{MS}}^{(4)} = 255 \text{ MeV} \right)$$

● with

$$\int_0^1 dx (xg + x\Sigma) = 1$$

$$\int_0^1 dx (xy) = 0.44 \quad \text{at } Q_0^2 \quad \rightarrow \text{(NMC result)}$$

(!) \Rightarrow IF not: $\int_0^1 dx (xy) \rightarrow 0.6 \dots$

- 1994 analysis

- F_2^P & F_2^D data

→ Counting rules on U_V & d_V

- But : $\bar{u} = \bar{d} = 2Q \dots$

(!) → $x g(x, Q_0^2 = 5 \text{ GeV}^2) = 2.24 x^{-0.2} (1-x)^{8.52}$

|| inconsistent
with prompt σ data ||

- Question

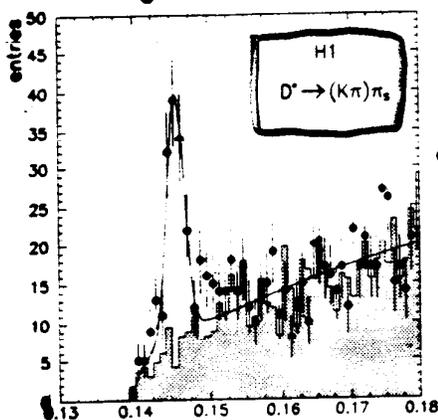
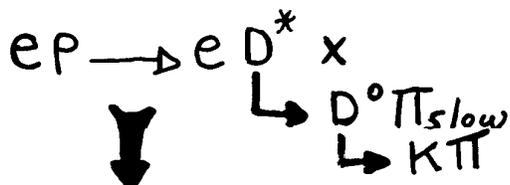
- Can we "blindly" parametrize xg , $x\Sigma$, xU^+ , $x\Delta^+$ and extract q_s ?

- can we still use the F.F.N.S for heavy(s) quark(s)?

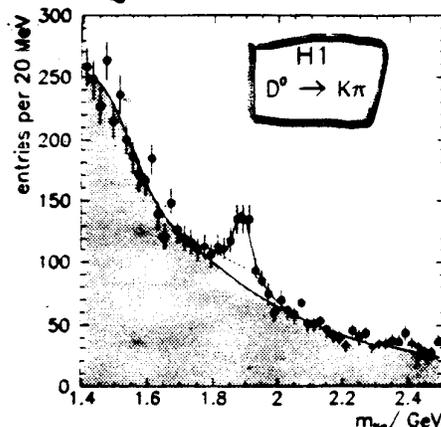
• $F_2^{c\bar{c}}$ •

• Measurement: $10 \text{ GeV}^2 \leq Q^2 \leq 100 \text{ GeV}^2$
 $y_e < 0.53$

• Signature



$\sigma_{\text{int}} = 2.7 \text{ pb}^{-1}$



$(m_{K\pi\pi} - m_{K\pi}) / \text{GeV}$

$m_{K\pi} / \text{GeV}$

$$\frac{d\sigma}{dx dQ^2}(ep \rightarrow e D x)$$

$$\Downarrow (P(c \rightarrow D) \times \text{Br})$$

$$\frac{d\sigma}{dx dQ^2}(ep \rightarrow e c \bar{c} x) \Rightarrow F_2^{c\bar{c}}(x, Q^2)$$

$(R=0)$

• Massless Versus Massive Prescription

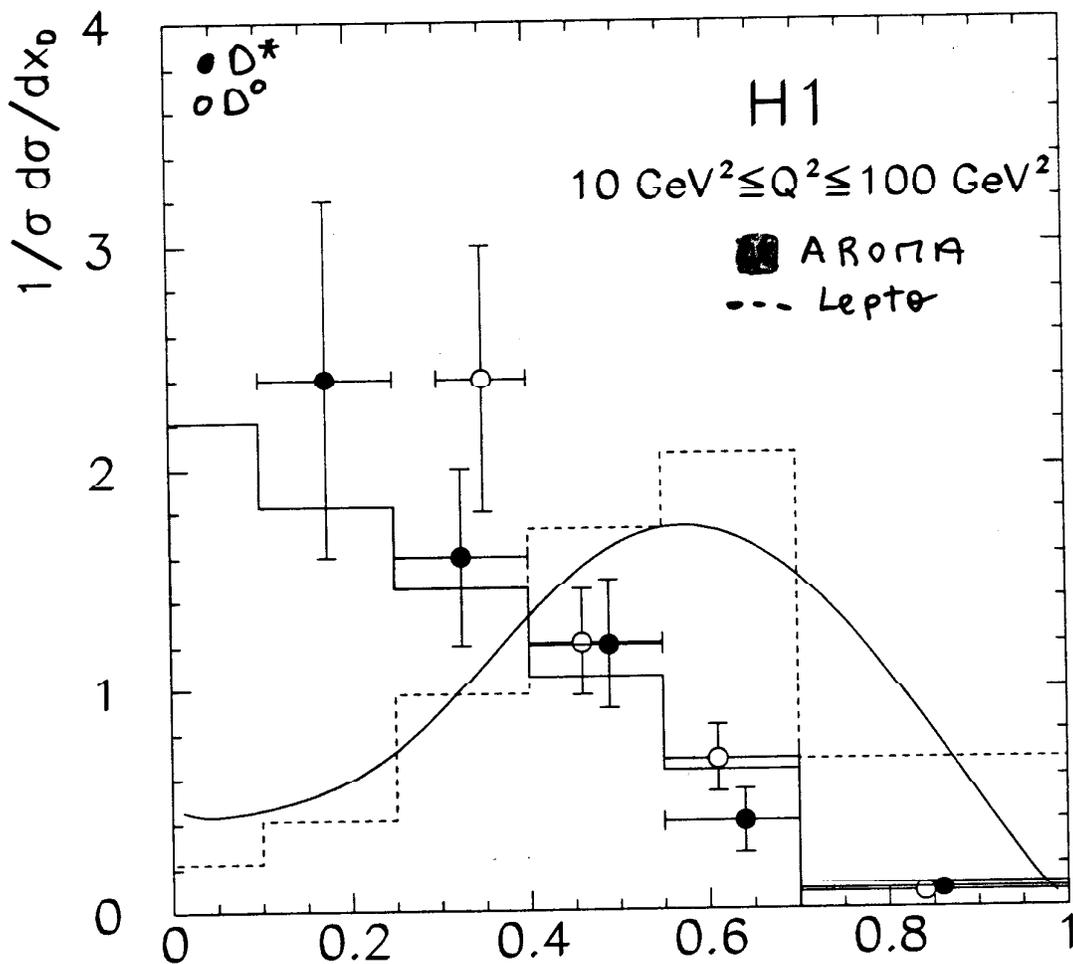
\downarrow LEPTO $\pi.C$ (massless $\pi E + P.S.$)

 \downarrow ARONIA $\pi.C$ (L.O.B.G.F + P.S.)

\rightarrow Fit: $\frac{1}{\sigma} \frac{d\sigma}{dx_0} = (1-\epsilon) \frac{1}{\sigma} \frac{d\sigma}{dx_0} \Big|_{BGF} + \epsilon \frac{1}{\sigma} \frac{d\sigma}{dx_0} \Big|_{\text{massless}}$

to Fragmentation distribution

\rightarrow $\epsilon < 5\%$ @ 95% C.L.

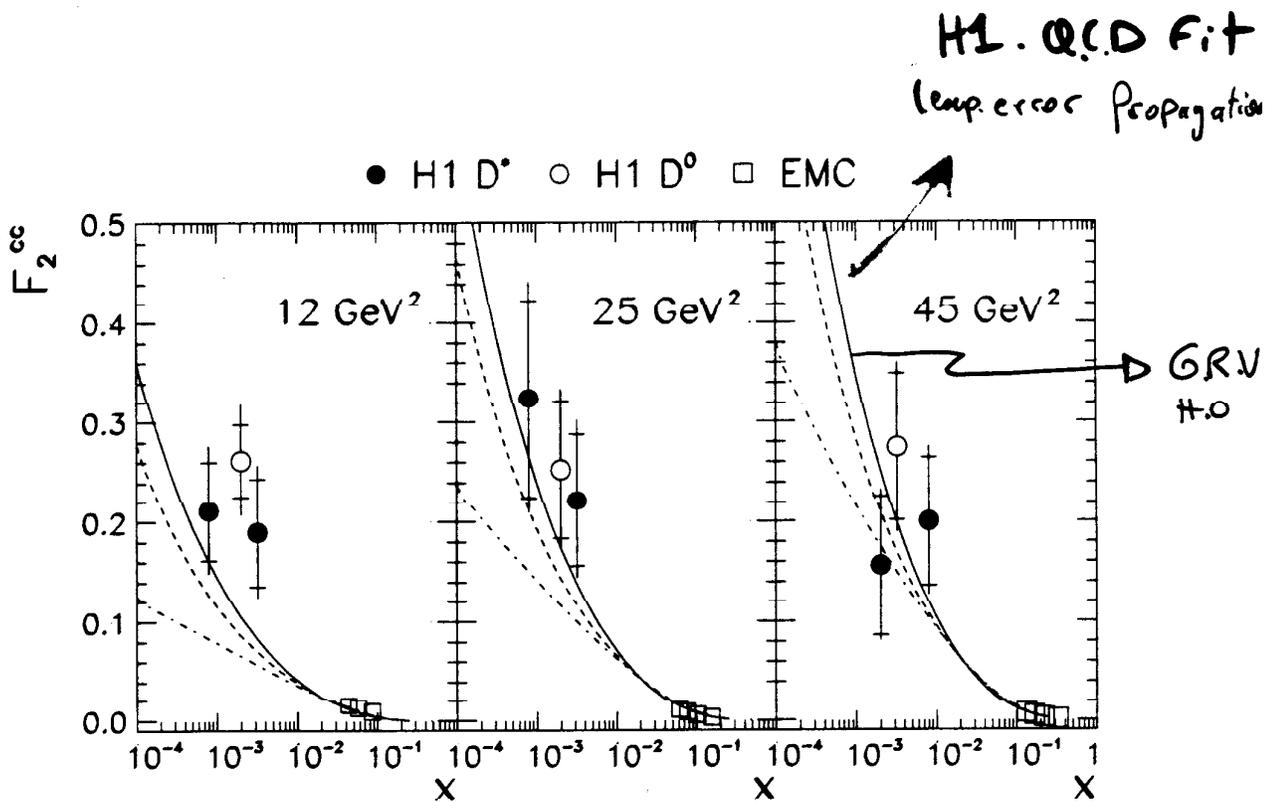


$x_0 = \frac{|p_0^*|}{|p_p^*|}$

• \Rightarrow comparison with p.g.f using

B. G. F (NLO) process :

• $m_c = 1.5 \text{ GeV}$; $\mu_{\text{BCF}}^2 = Q^2 + m_c^2$



$\Rightarrow \left\langle \frac{F_2^{c\bar{c}}}{F_2} \right\rangle = 23.7\% \pm 2.1\% \Big|_{\text{stat.}} \pm 4.1\% \Big|_{\text{syst.}}$

• F_L extraction •

• DIS X-section:

$$K \frac{d\sigma}{dx dQ^2} = F_2 - \frac{y^2}{Y_+} F_L$$

• with

$$K = \frac{Q^2 x}{2\pi\alpha_{em}^2 Y_+} ; Y_+ = 2(1-y) + y^2$$

• idea: if "we know" F_2 at high y

$$\Rightarrow F_L \text{ determined from } \frac{d\sigma}{dx dQ^2}$$

\Rightarrow NEW X-section measurement:

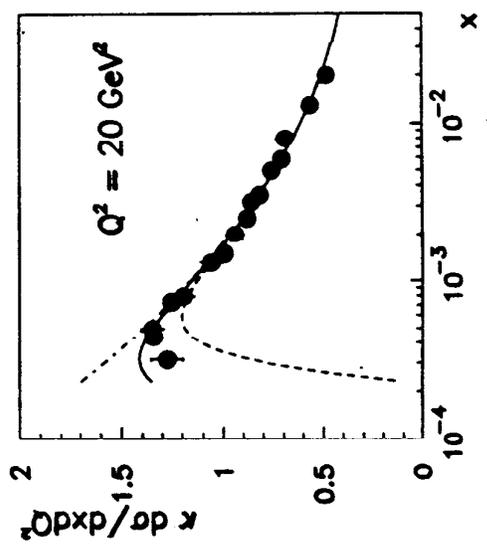
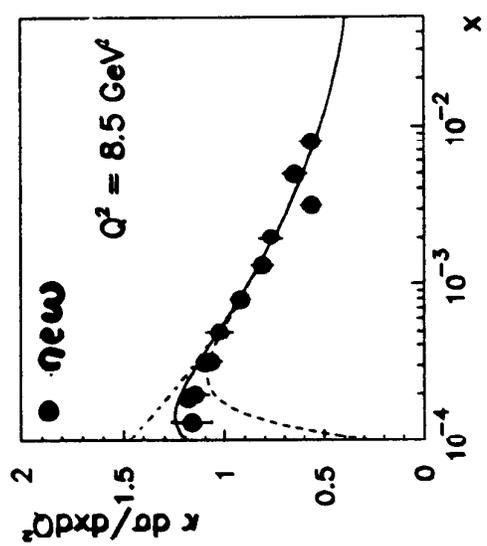
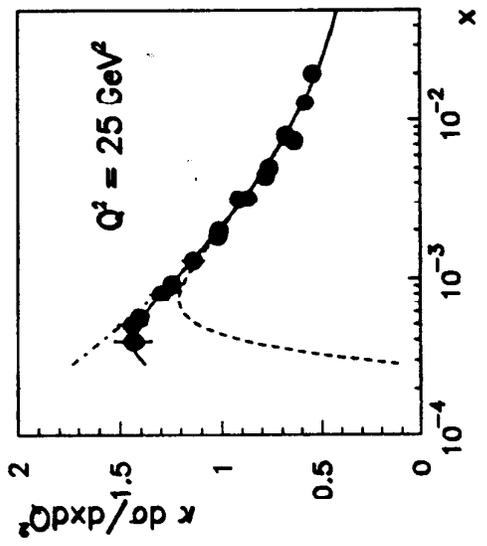
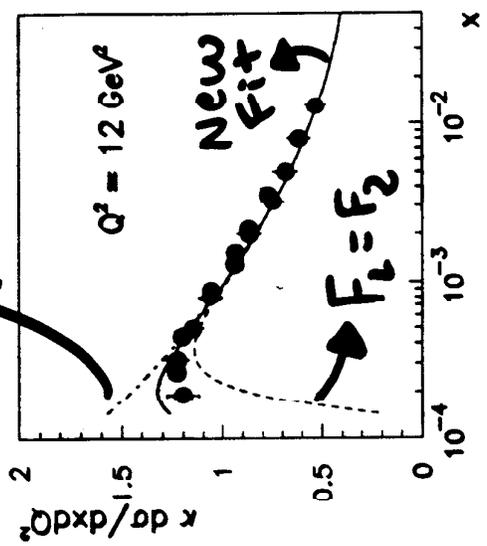
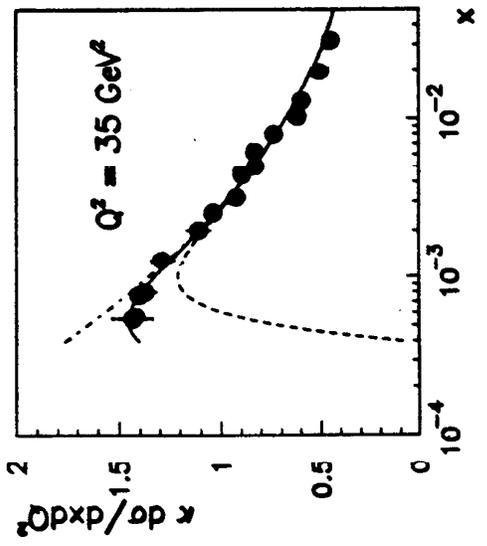
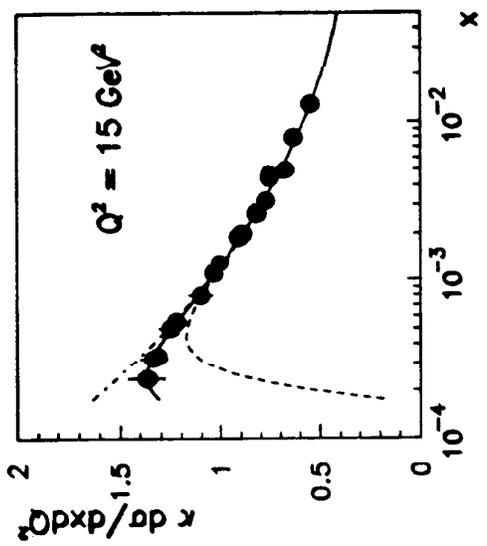
high y & small x

$$0.6 < y < 0.78 \quad 1.3 \cdot 10^{-4} \leq x \leq 5.5 \cdot 10^{-4}$$

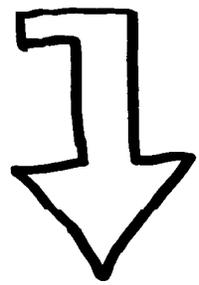
$$(8.5 \text{ GeV}^2 \leq Q^2 \leq 35 \text{ GeV}^2)$$

\Rightarrow New F_2 Fit (repeat 1994 analysis)

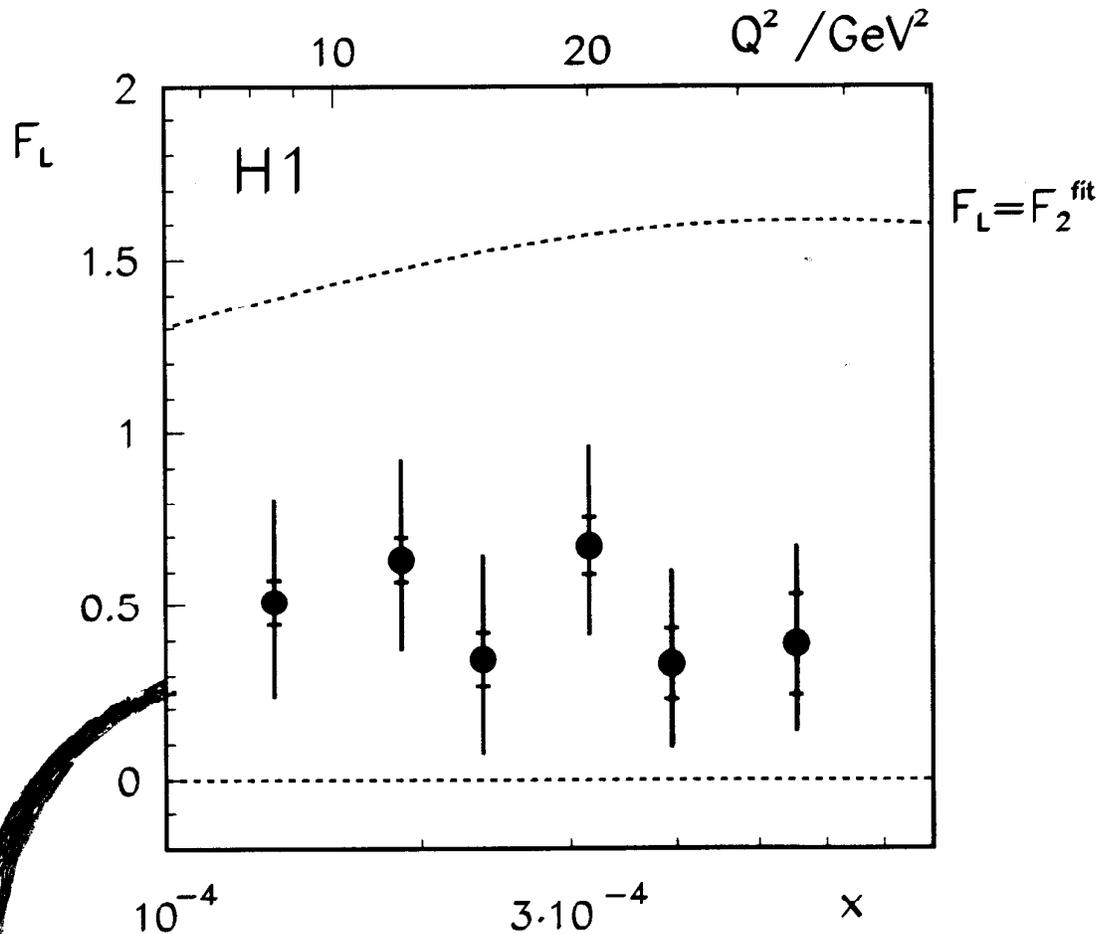
using $\left\{ \begin{array}{l} H1 \\ BCMS \end{array} \right. F_2$ at $y < 0.35$



- Extrapolation of new F_2 fit at high y



(+ syst. studies on extrapolation)



Cross-section Fit excluding our new high y measurement & using N.L.O F_L calculation

• Summary •

• F_2 fit :

- up to now : - QCD test ;
- gluon extraction with experimental error band

- near future : α_s extraction , BUT :

Do we need other observable?

• F_2^c :

- very promising observable

⇒ more statistic required

⇒ work is going on!

• F_2 :

- "new" method ⇒ consistency test of DGLAP.

⇒ NEW measure is being performed

⇒ lower Q^2 & higher y domain