

# **DIS with Leading Protons in the Forward Proton Spectrometer of H1 at HERA**

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BENNO LIST

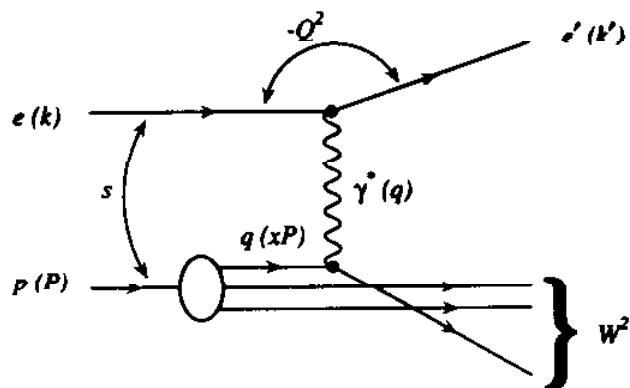
DESY, H1

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Deep Inelastic Scattering and QCD  
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Working Group II: Diffraction

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- Introduction
- Measurement of  $\frac{d^3\sigma(ep \rightarrow e' p' X)}{dx dQ^2 dx_\pi} \propto F_2^{LP(3)}$
- Fits to  $F_2^{LP(3)}$ , Factorization

# Kinematics



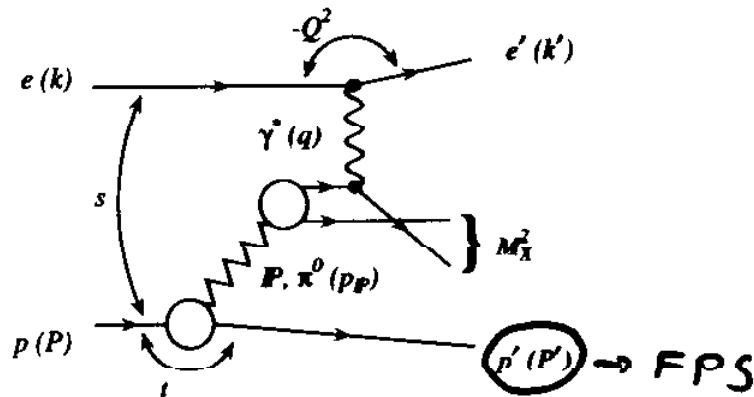
$$x = \frac{Q^2}{2q \cdot P}$$

BJORKEN scaling variable=  
momentum fraction of quark

$$y = \frac{q \cdot P}{k \cdot P}$$

inelasticity

$$Q^2 = x \cdot y \cdot s$$



$$x_\pi = \frac{p_\pi \cdot q}{P \cdot q}$$

= 1 -  $\frac{E'_p}{E_p}$  Momentum fraction of exchange

$$\beta = \frac{Q^2}{2p_\pi \cdot q}$$

Momentum fraction of quark out of "pion"

$$Q^2 = \beta \cdot x_\pi \cdot y \cdot s$$

$$\beta = \frac{x}{x_\pi}$$

Proton energy  $E_p = 820 \text{ GeV}$ , CM energy  $\sqrt{s} = 300 \text{ GeV}$ .

# Cross Section Definition

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Semiinclusive cross section  $\sigma(ep \rightarrow e'p'X)$

for DIS events with protons of  $p_\perp < 200 \text{ MeV}$ .

Measured for  $E'_p = 580 - 740 \text{ GeV}$  ( $x_\pi = 0.1 - 0.3$ ).

Parametrized by semiinclusive structure function  $F_2^{LP(3)}$ :

$$\frac{d^3\sigma(ep \rightarrow e'p'X)}{dx \boxed{dQ^2} dx_\pi} = \frac{4\pi\alpha^2}{\boxed{x} Q^4} \left(1 - y + \frac{y^2}{2}\right) F_2^{LP(3)}(x, Q^2, x_\pi)$$

$$dx = x_\pi \cdot d\beta \quad x = x_\pi \cdot \beta$$

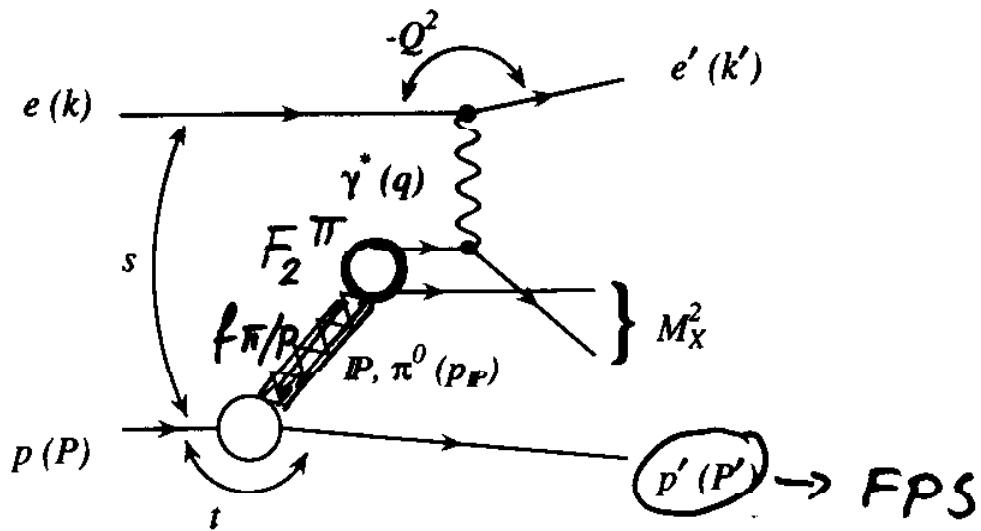
$$\frac{d^3\sigma(ep \rightarrow e'p'X)}{\boxed{d\beta} dQ^2 dx_\pi} = \frac{4\pi\alpha^2}{\boxed{\beta} Q^4} \left(1 - y + \frac{y^2}{2}\right) F_2^{LP(3)}(\beta, Q^2, x_\pi)$$

Cross section unambiguously\* defined on hadron level

Model independent

\*: In the case where  $x_\pi < 0.5$ : there can be only one proton per event with  $E'_p > 0.5E_p$ .

# Pion Exchange



Proton emits **virtual pion**

Momentum fraction  $x_\pi = 1 - E'_p/E_p$  measured by FPS

$\beta = x/x_\pi$  momentum fraction of quark out of pion

Flux factor  $f_{\pi/p}(x_\pi, t)$

Pion structure function  $F_2^\pi(\beta, Q^2)$

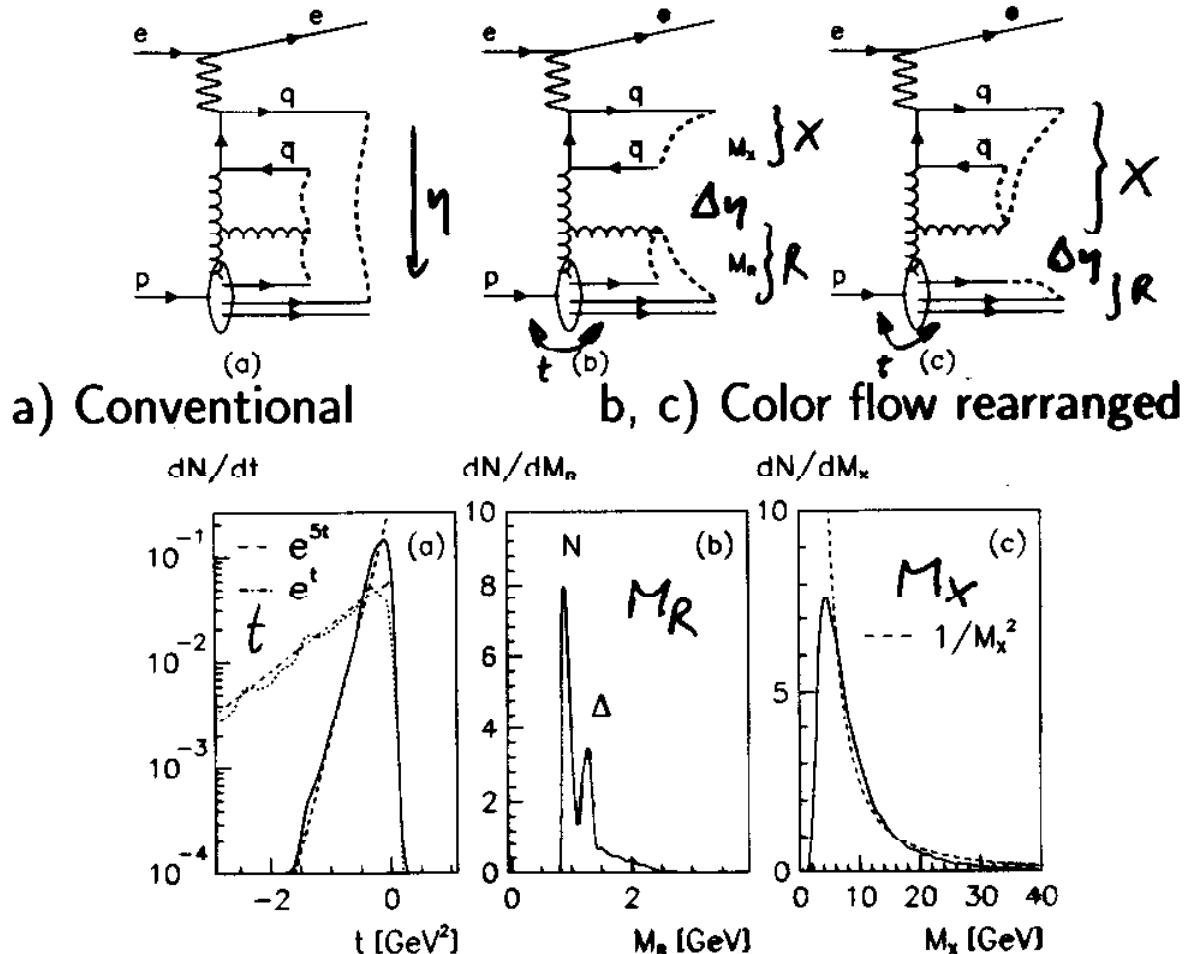
$$\begin{aligned} \frac{d^3\sigma(ep \rightarrow e'p'X)}{d\beta dQ^2 dx_\pi} &= \frac{4\pi\alpha^2}{\beta Q^4} \left(1 - y + \frac{y^2}{2}\right) F_2^{LP(3)}(\beta, Q^2, x_\pi) \\ &= f_{\pi/p}(x_\pi) \frac{d^2\sigma(e\pi \rightarrow e'X)}{d\beta dQ^2} \\ &= f_{\pi/p}(x_\pi) \frac{4\pi\alpha^2}{\beta Q^4} \left(1 - y + \frac{y^2}{2}\right) F_2^\pi(\beta, Q^2) \end{aligned}$$

Expect factorization

$$F_2^{LP(3)}(\beta, Q^2, x_\pi) = F_2^\pi(\beta, Q^2) \cdot \underbrace{\int_t^1 f_{\pi/p}(x_\pi, t) dt}_{f_{\pi/p}(x_\pi)}$$

# Soft Color Interactions

Generator: LEPTO (6.3)



- a)  $t$  spectrum:  $d\sigma/dt \propto e^{bt}$   
 b) Mass of proton remnant      c) central system

Soft color interactions + new seaquark treatment model

- Diffractive events (pomeron exchange)
- Diffractive proton dissociation
- Meson exchange ( $\pi^0, \pi^+, K, \dots$ )

Figures from: A. EDIN, G. INGELMAN & J. RATHSMAN: DESY 96-060.

# The H1 Forward Proton Spectrometer

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**Objective:**

Measure protons with  $E'_p > 400 \text{ GeV}$ ,  $\theta_p < 1 \text{ mrad}$

⇒ Detectors close ( $\approx 4 \text{ mm}$ ) to proton beam

HERA magnets act as magnetic spectrometer

⇒ Energy measurement by measuring offset and tilt of proton trajectory w.r.t. circulating beam at 85 m

## Forward Proton Spectrometer

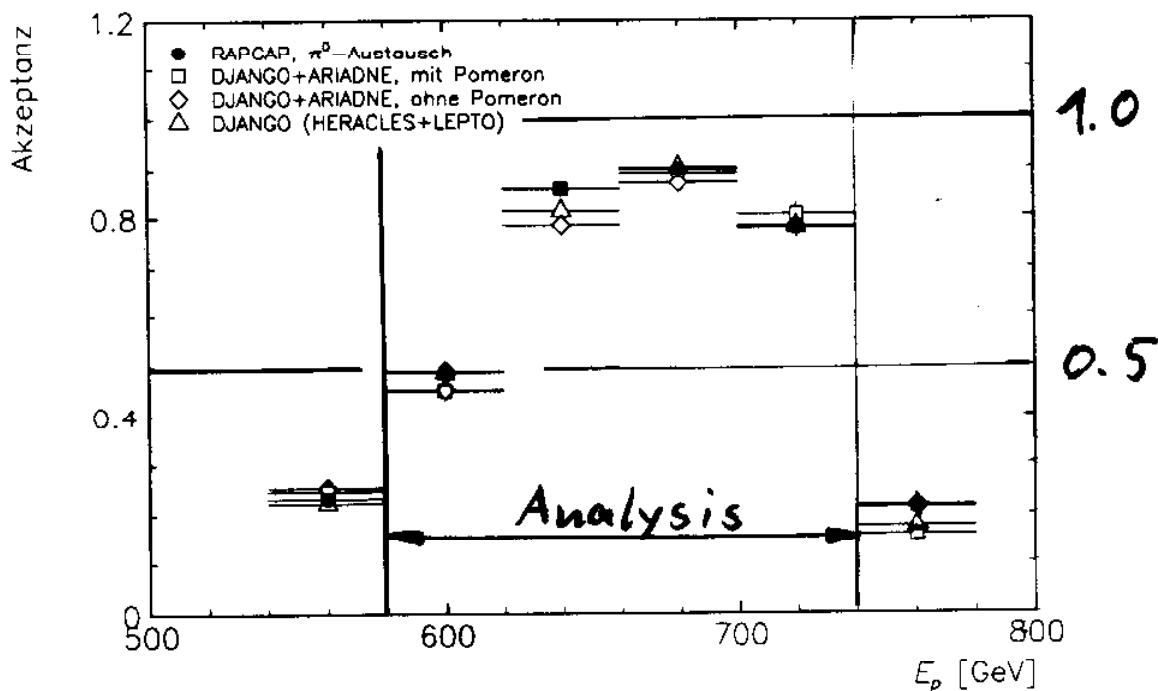
- Detectors in plunger vessels ("Roman Pots")
- Scintillating fiber hodoscopes
- Readout by multi channel photomultipliers
- 2 stations at 81 and 90 m
- Position resolution  $\approx 0.1 \text{ mm}$

**Energy Resolution:**  $\Delta E'_p = 6 \text{ GeV}$  at  $E'_p = 700 \text{ GeV}$

# Acceptance of the H1 FPS

### Acceptance:

## Fraction of protons with $p_T < 200$ MeV in fiducial region



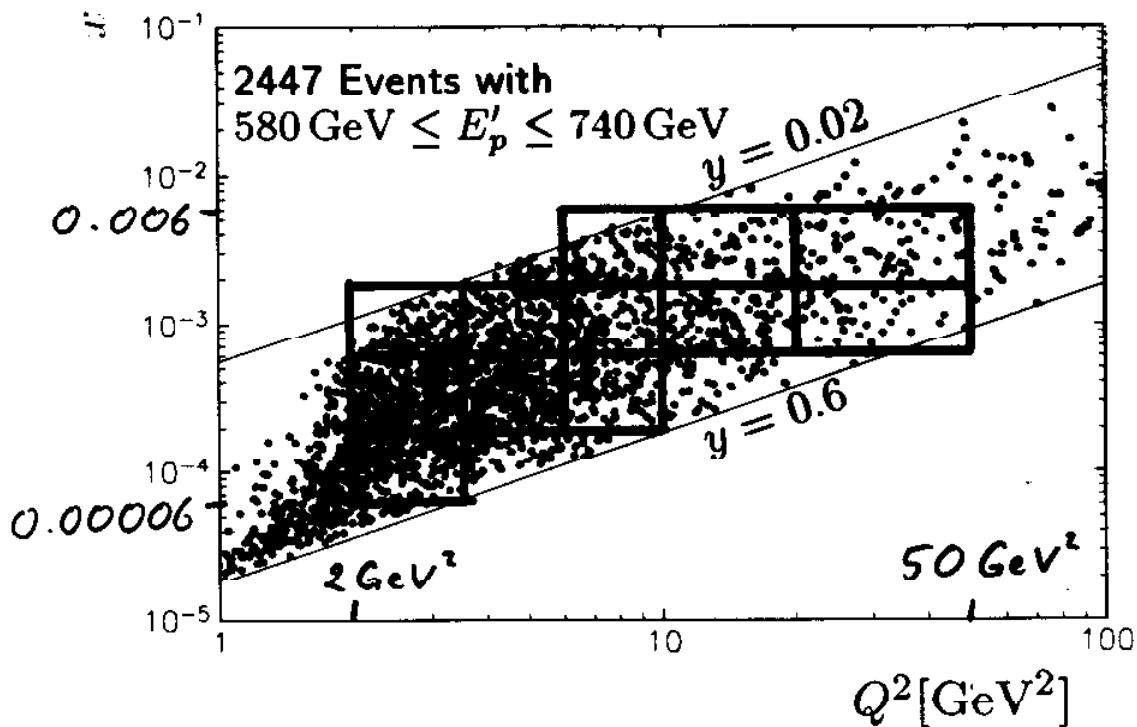
Acceptance  $\gtrsim 50\%$  for  $E'_p = 580 - 740 \text{ GeV}$

## **Analysis:**

#### 4 Energy bins, $580 - 740 \text{ GeV}$ ( $x_\pi = 0.1 - 0.3$ )

Bin size 40 GeV ( $\Delta x_\pi = 0.05$ )

# DIS Analysis



1995 Data,  $\int \mathcal{L} dt = 1.44 \text{ pb}^{-1}$

Cuts:

- ▶ Electron energy:  $E'_e > 12 \text{ GeV}$
- ▶ Electron scattering angle:  $155^\circ < \theta_e < 177^\circ$
- ▶ Inelasticity:  $0.02 < y < 0.6$
- ▶  $\geq 1$  track with  $p_\perp > 450 \text{ MeV}$  at  $20^\circ < \theta < 160^\circ$
- ▶ + further quality cuts

Kinematics:  $\Sigma$  method combines **Electron variables**  $E'_e$ ,  $\theta_e$  with hadronic quantity  $\Sigma = \sum_h (E_h - p_{z,h})$ .

$Q^2$  resolution: 8 %

$x$  resolution: 10 ... 30 % at  $y \approx 0.6 \dots 0.02$

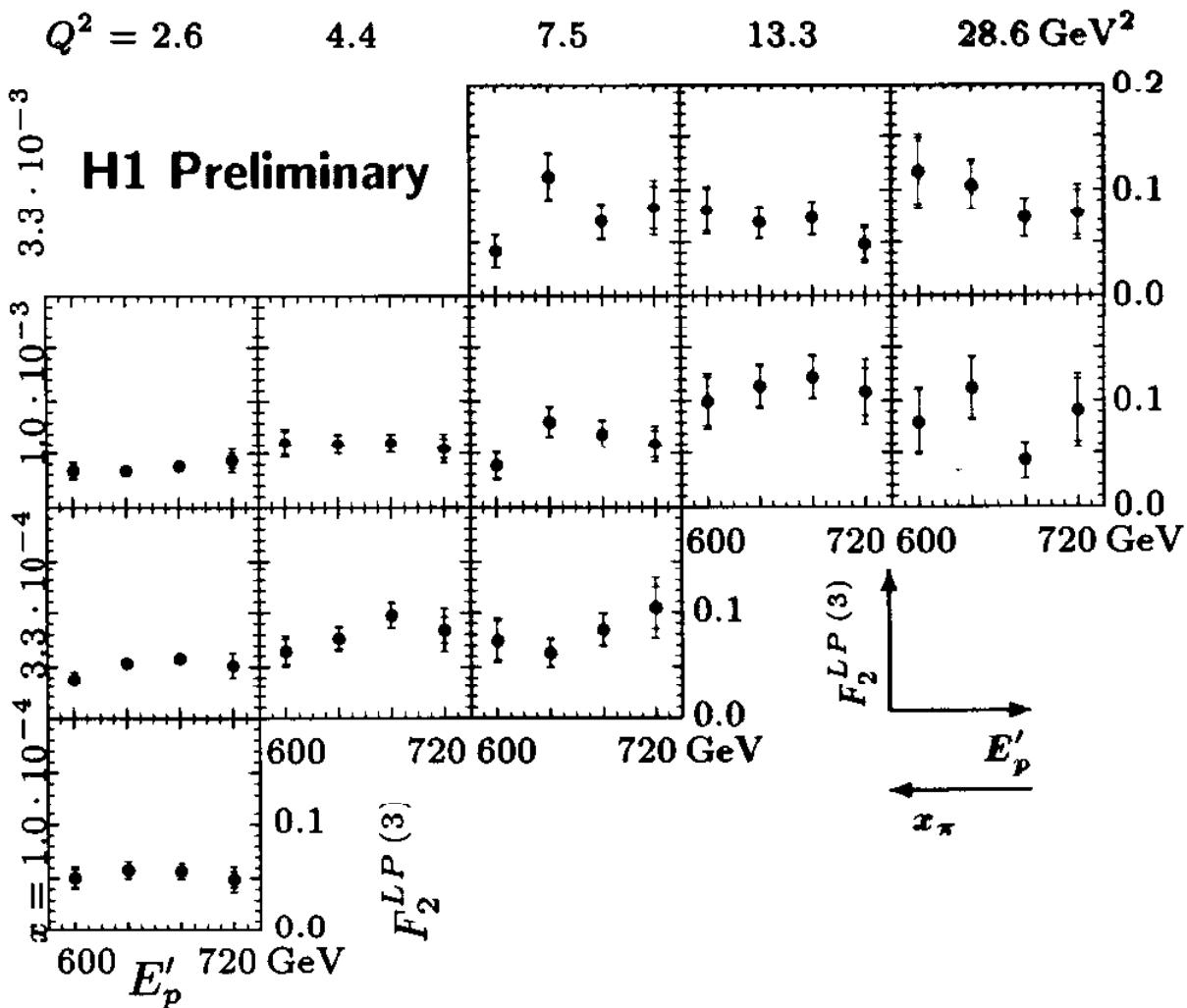
Radiative corrections small

# Errors

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- Normalization: Common error
  - ▶ Luminosity: 1.14 %
  - ▶ Track reconstruction in FPS: 5 %
  - ▶  $z$  position of vertex: 1 %
- Sum: 5.2 %
- FPS induced: Dependent on  $E'_p$  ( $x_\pi$ )
  - ▶ Migration correction: 2.3 ... 18.9 %
  - ▶ Acceptance: 3.7 ... 11.5 %
- Sum: 4.9 ... 19.3 %
- $x, Q^2$  dependent
  - ▶ Trigger efficiency SpaCal: 5 %
  - ▶ Trigger efficiency DCR $\phi$ : 2 %
  - ▶  $\geq 1$  good track: 3 %
  - ▶ Measurement of  $E'_e$ :  $-1.0 \dots + 5.4\%$
  - ▶ Measurement of  $\theta_e$ : 0.8 ... 4.0 %
  - ▶ Measurement of  $\Sigma$ :  $-5.7 \dots + 4.6\%$
  - ▶ Acceptance: 1.7 ... 8.3 %
- Sum: 7.7 ... 12.3 %
- Statistical error: 9.4 ... 41 %

# Results for $F_2^{LP(3)}$



- Weak  $x_\pi$  dependency
- Weak  $x$  dependency
- $F_2^{LP(3)}$  rises with  $Q^2$

$$\frac{d^3\sigma(ep \rightarrow e' p' X)}{dx dQ^2 dx_\pi} = \frac{4\pi\alpha^2}{x Q^4} \left(1 - y + \frac{y^2}{2}\right) F_2^{LP(3)}(x, Q^2, x_\pi)$$

for protons with  $p_\perp < 200 \text{ MeV}$

# Global Fit to $F_2^{LP(3)}$

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Hypothesis:

$$F_2^{LP(3)}(\beta, Q^2, x_\pi) = f_{\pi/p}(x_\pi) \cdot F_2^\pi(\beta, Q^2)$$

Normalization of  $f_{\pi/p}(x_\pi)$  uncertain  
(additional trajectories)

Choose form

$$F_2^{LP(3)}(\beta, Q^2, x_\pi) = r(x_\pi) \cdot \tilde{F}_2^{LP}(\beta, Q^2)$$

with  $r(x_{\pi 3} = 0.171) = 1$ ,  
 $r(x_{\pi j}) = r_j$ , take  $r_j$  as free parameters for  $j \neq 3$ .

Fit to

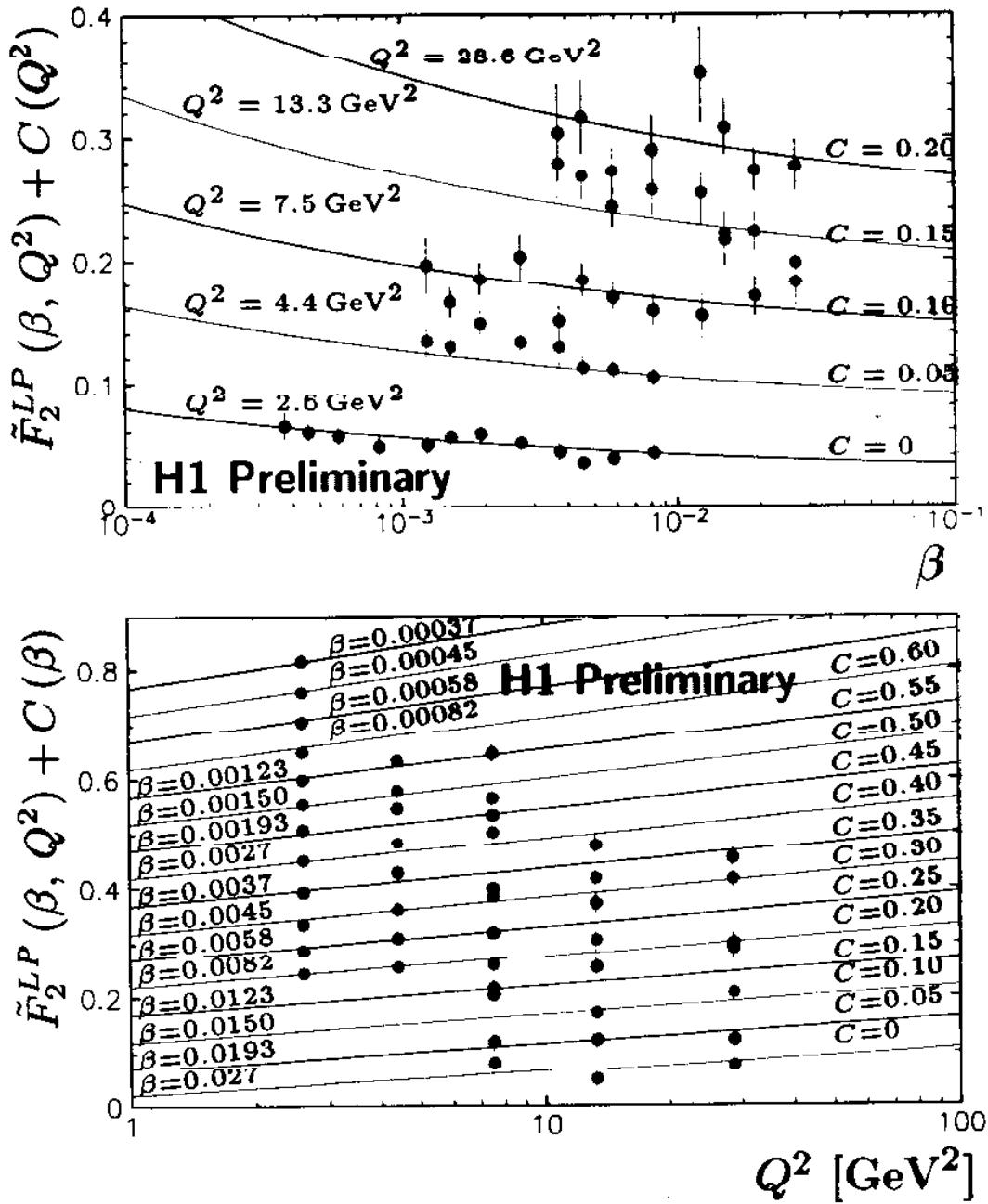
$$F_2^{LP(3)}(\beta, Q^2, x_\pi) = r_j \cdot (a \cdot \beta^b + c \cdot \beta^d \cdot \log Q^2).$$

$\chi^2/df = 52.9/41$  ( $CL = 10.1\%$ ),  
only statistical and  $x, Q^2$  dependent errors

Reminder:

$\beta = x/x_\pi$  Momentum fraction of quark out of “pion”  
 $x_\pi = 1 - E'_p/E_p$  Momentum fraction carried by “pion”

# Global Fit to $F_2^{LP(3)}$



Factorisation:

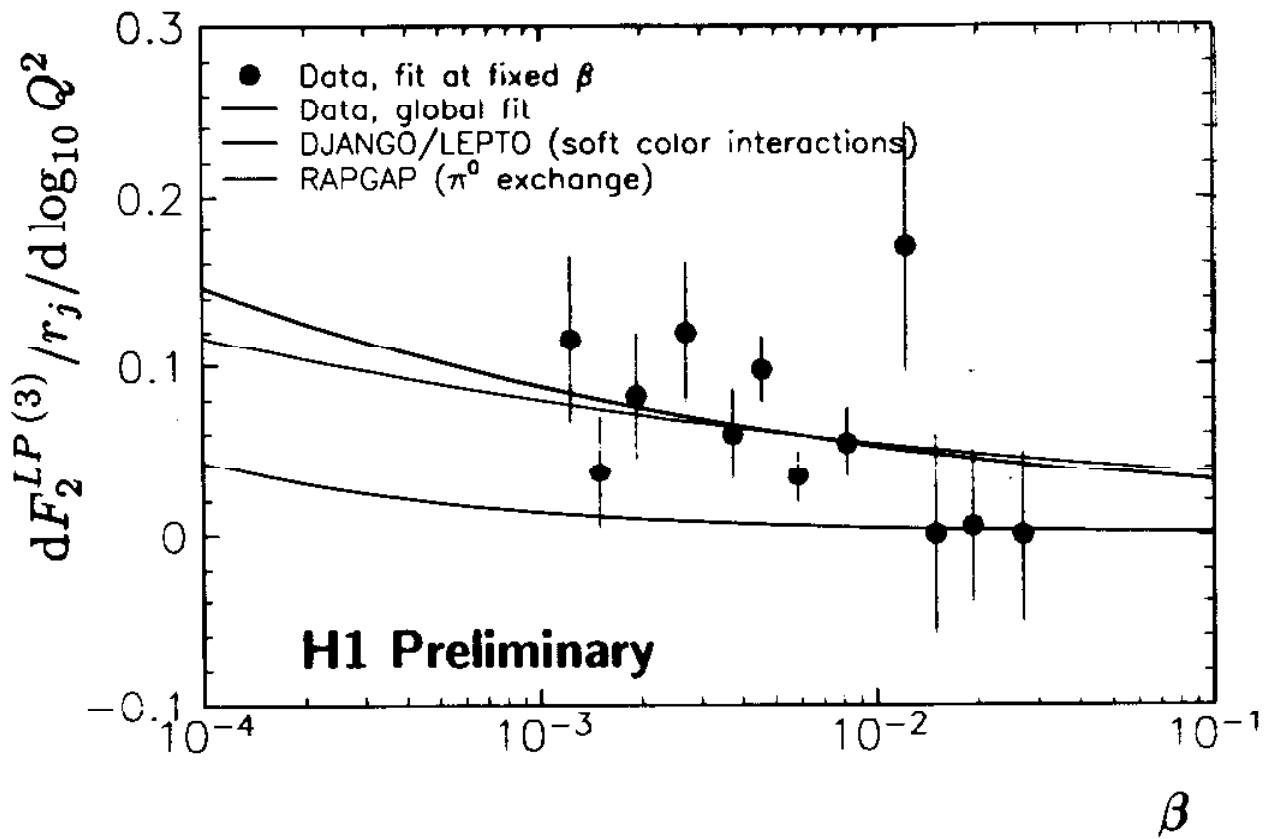
$$F_2^{LP(3)}(\beta, Q^2, x_\pi) = r(x_\pi) \cdot \tilde{F}_2^{LP}(\beta, Q^2)$$

$\tilde{F}_2^{LP}(\beta, Q^2)$  rises with  $Q^2$  and falling  $\beta$ , like hadron structure function

$$\chi^2/df = 52.9/41 \quad (CL = 10.1\%)$$

# $Q^2$ Rise

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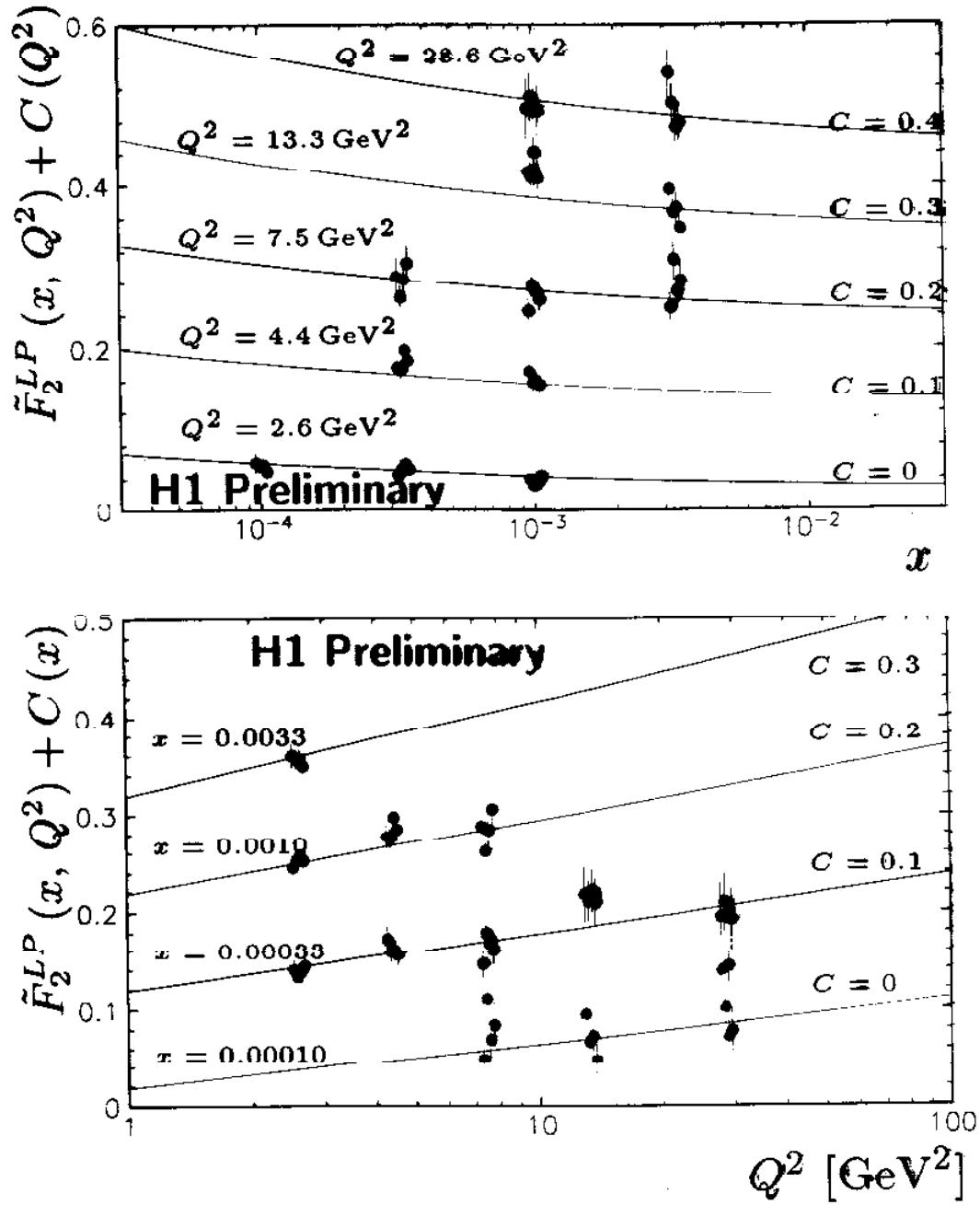
$$dF_2^{LP(3)} / d \log_{10} Q^2$$

Red points:

$Q^2$  dependence fitted for each  $\beta$  bin independently

$$F_2^{LP(3)}(\beta, Q^2) = a(\beta) \cdot \log_{10} Q^2 + b(\beta)$$

# Factorisation in $x$ , $Q^2$ , $x_\pi$ ?

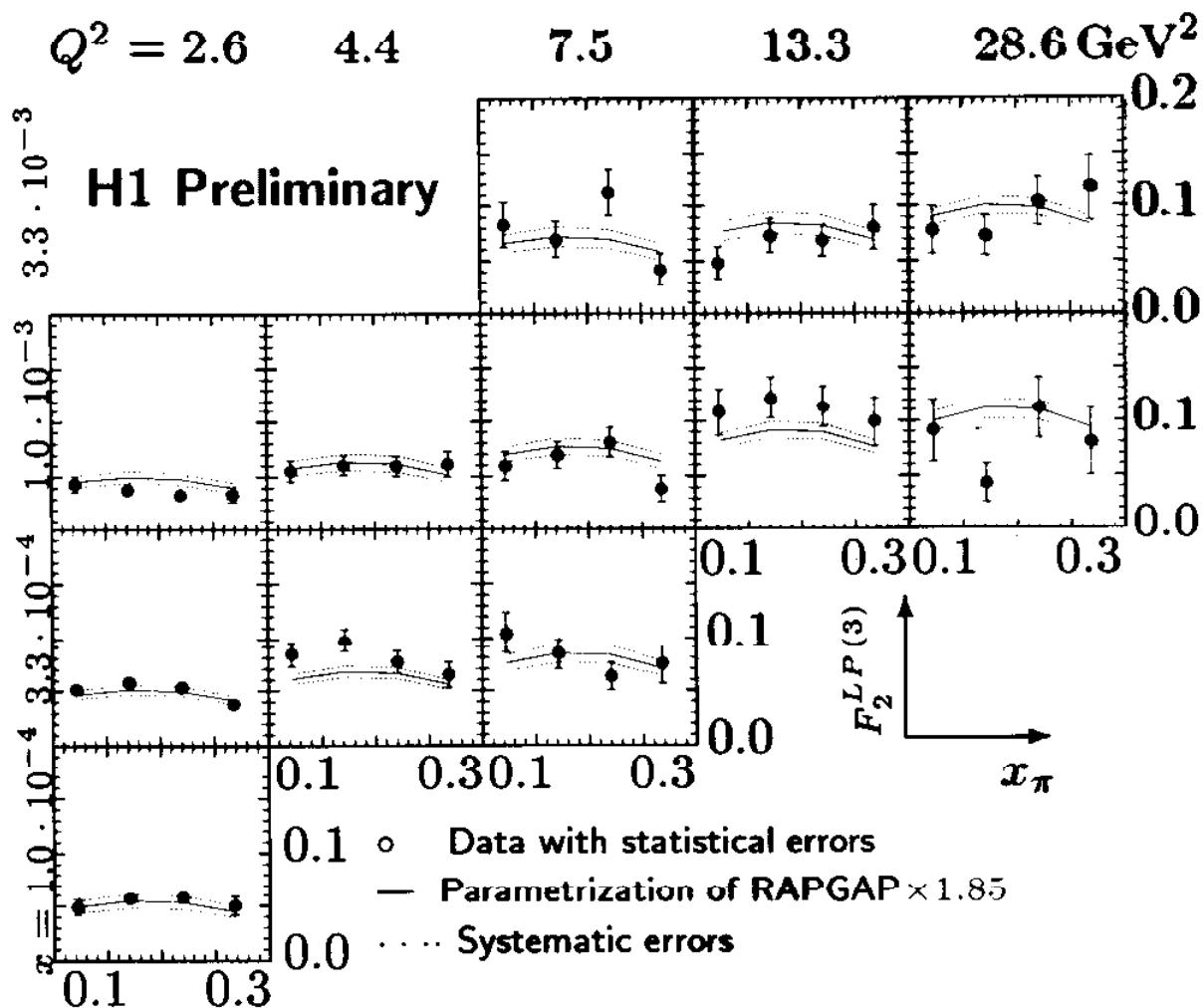


$$F_2^{LP(3)}(x, Q^2, x_\pi) = r(x_\pi) \cdot \tilde{F}_2^{LP}(x, Q^2)$$

$$\chi^2/df = 53.1/41 \quad (CL = 9.8\%)$$

Answer: Factorisation as good as in  $\beta$ ,  $Q^2$ ,  $x_\pi$

# Comparison with RAPGAP



RAPGAP:  $\pi^0$  exchange

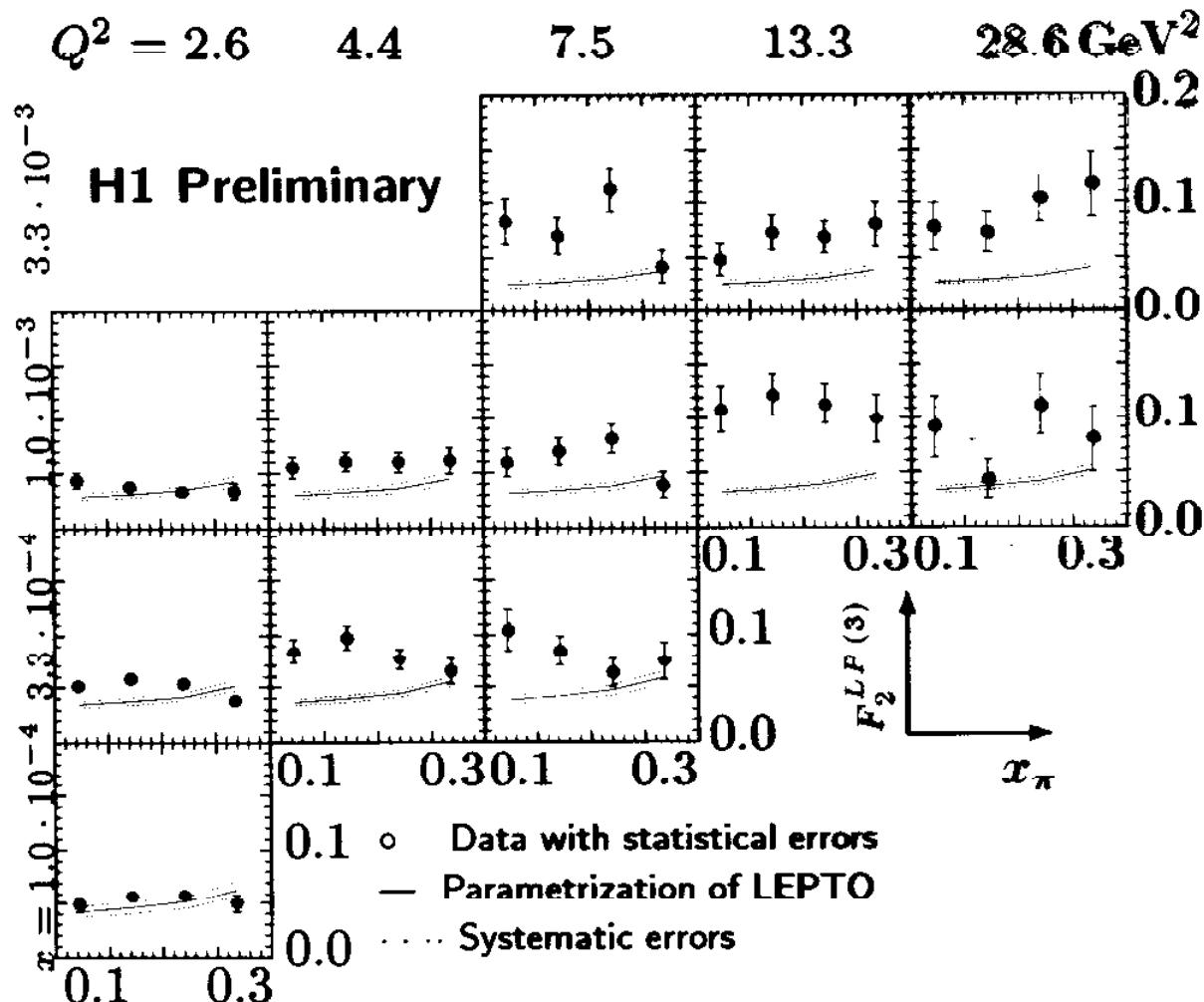
Pion structure function: GLÜCK, REYA, and VOGT

Cross section prediction factor 1.85 too low,

Shape of distributions well described

$\chi^2/df = 54.2/47$ , ( $CL = 21.9\%$ )

# Comparison with LEPTO



LEPTO: Soft color interactions

Cross section at small  $Q^2$  OK

$x_\pi$  spectrum rises too steeply

$Q^2$  rise of data not described

# Summary

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- Measurement of  $\frac{d^3\sigma(ep \rightarrow e' p' X)}{dx dQ^2 dx_\pi}$  for  $p_\perp < 200 \text{ MeV}$ ,  
parametrized by  $F_2^{LP(3)}$   
Analysis:  $E'_p = 580 - 740 \text{ GeV}$  ( $x_\pi = 0.1 - 0.3$ )
- Rise of  $F_2^{LP(3)}$  with  $Q^2$  and with falling  $x$
- Small  $x_\pi$  dependency
- Data compatible with factorization in  $\beta, x_\pi$  and  $x, x_\pi$
- $\pi^0$  exchange (RAPGAP) describes shape of  $F_2^{LP(3)}$ ,  
normalization too low
- Soft color interactions (LEPTO): Too shallow  $Q^2$  rise