

The Race for θ_{13} : Reactors versus Superbeams

Manfred Lindner

Technical University Munich

Introduction

- mass parameters: m_1, m_2, m_3 **or** $m_1, \Delta m_{21}^2, |\Delta m_{31}^2|, sign(\Delta m_{31}^2)$
- mixings:

$$\mathbf{U} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix} \cdot \text{diag}(e^{i\Phi_1}, e^{i\Phi_2}, 1)$$

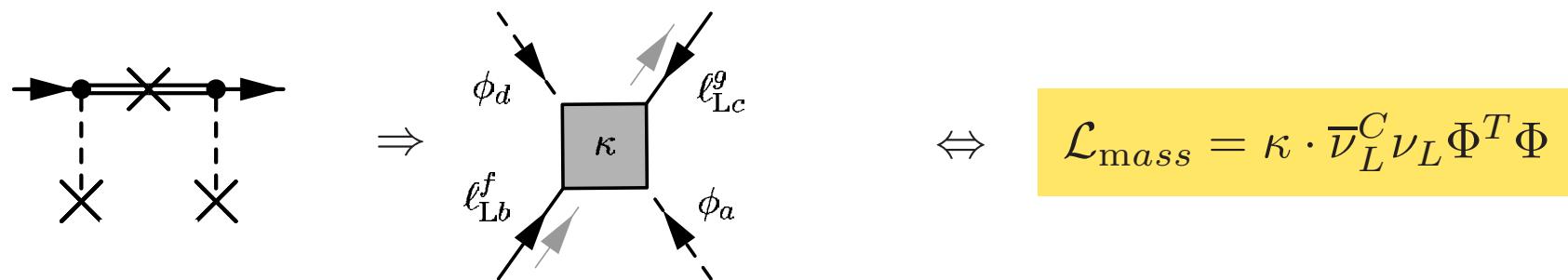
- parameter determination schedule

$\theta_{23}, \Delta m_{31}^2 $ $\theta_{12}, \Delta m_{21}^2$	atmospheric ν -experiments, K2K, MINOS, CNGS solar ν -experiments, KamLAND
θ_{13} absolute mass scale $\text{sgn}[\Delta m_{31}^2], \delta$ Φ_1, Φ_2	upper bound from CHOOZ: $\sin^2 2\theta_{13} < 0.1$ upper bound(s) superbeams, neutrino factories $0\nu\beta\beta + ?$

⇒ **next steps:** 1) neutrino mass scale
 2) θ_{13} \Leftrightarrow 3-flavour effects,, **leptonic CP-violation**

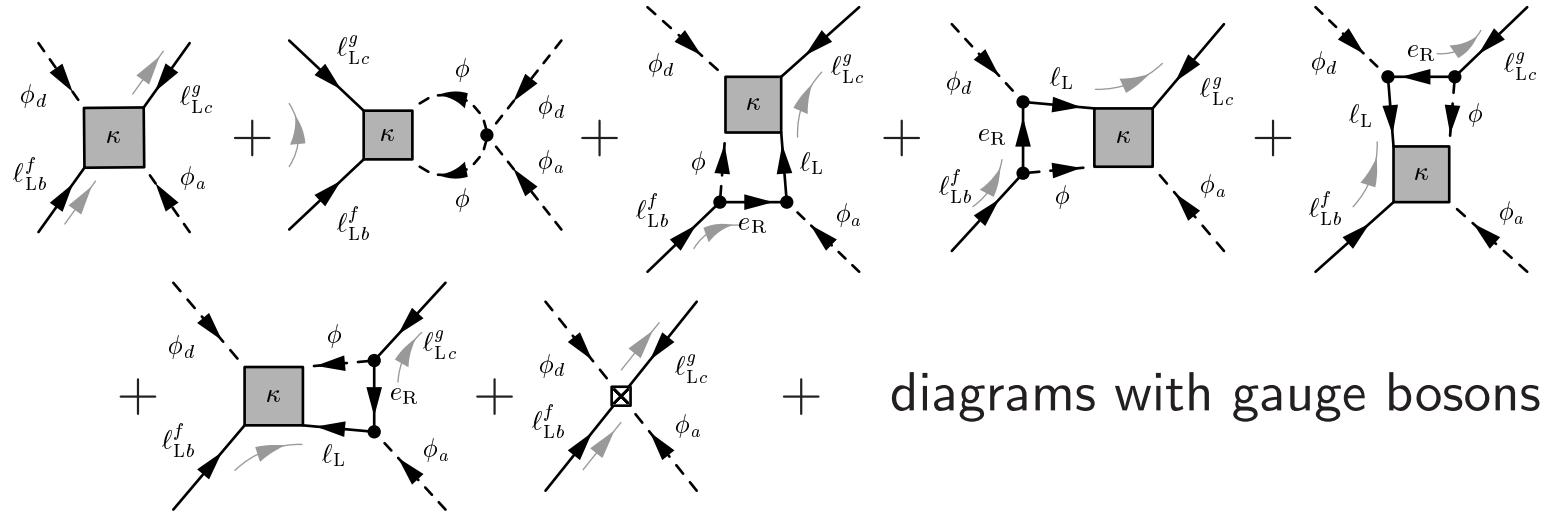
How small could θ_{13} be?

- **neutrino mass models** \Rightarrow diagonalization of “textures”
 - $\theta_{ij} = \mathcal{O}(1)$ or maybe suppressed by mass hierarchies $10^{-1} \dots 10^{-2}$
 - texture parameters may allow $\theta_{13} \equiv 0 \Leftrightarrow$ parameter tuning
 - $\theta_{12} \sim \theta_{23} \sim 1$ and $\theta_{13} \ll 10^{-2} \Rightarrow$ special reason (symmetry, ...)
- **RGE:** Even for $\theta_{13} = 0$ at the GUT scale \Rightarrow evolution to $\theta_{13} \neq 0$ at low energies
 - $d = 5$ **neutrino mass operator** \Rightarrow integrating out all heavy dof, e.g. M_R :



- only light degrees of freedom \Rightarrow ν_L, Φ
- κ is dimension-full , e.g. $\kappa \simeq \frac{1}{M_R}$, $\langle \Phi \rangle = v \Rightarrow$ neutrino masses $\sim \kappa v^2$
- **Comparison of theory and experiment:**
 - **experiment:** masses, mixings at low energies (in the future very precise!)
 - **theory:** \Rightarrow models at high energies

- RGE-evolution at 1-loop: SM, MSSM, 2HSM



View β -function(s):

non-diagonal \Leftrightarrow running mixings

Yukawa-matrices

$$16\pi^2 \beta_\kappa = -\frac{3}{2} \kappa (Y_e^\dagger Y_e) - \frac{3}{2} (Y_e^\dagger Y_e)^T \kappa + \lambda \kappa - 3g_2^2 \kappa$$

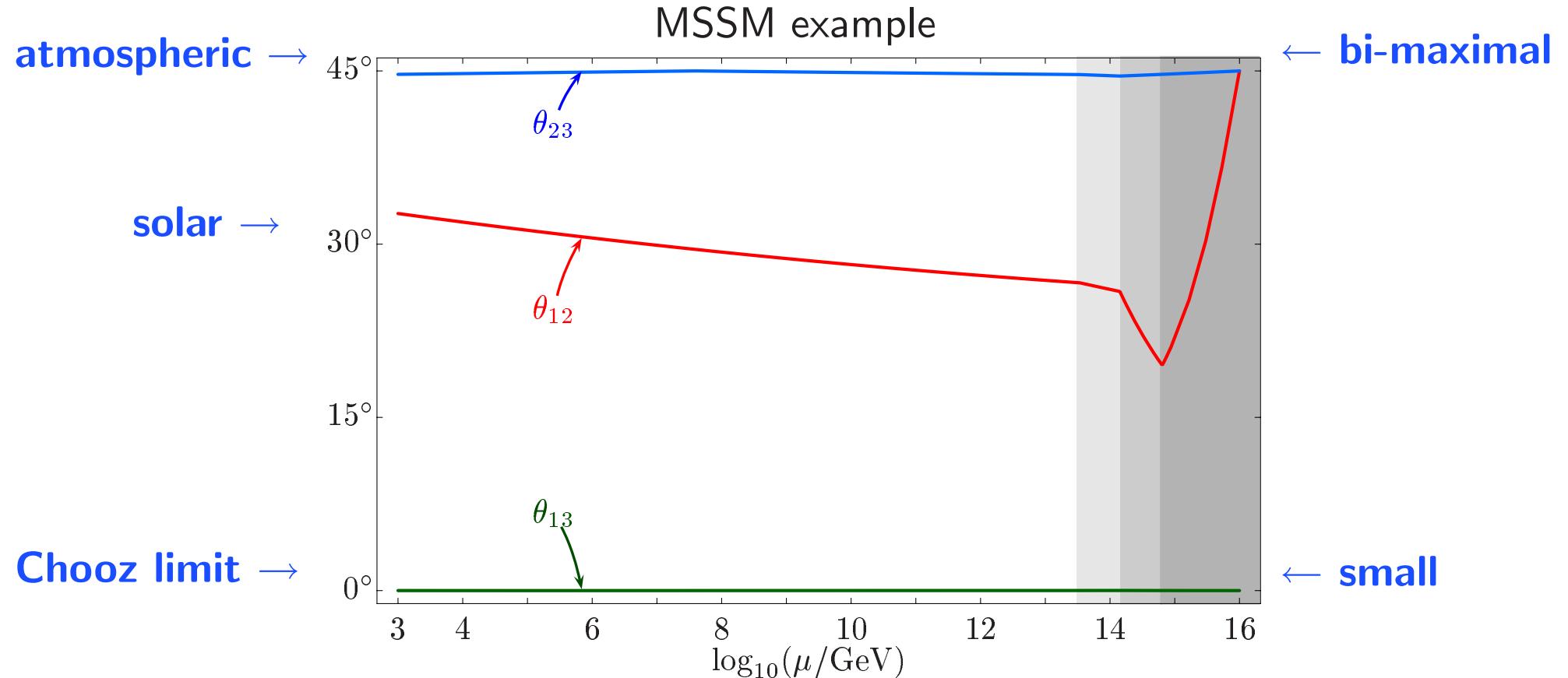
$$+ 2 \operatorname{Tr}(Y_e^\dagger Y_e) \kappa + 6 \operatorname{Tr}(Y_u^\dagger Y_u) \kappa + 6 \operatorname{Tr}(Y_d^\dagger Y_d) \kappa$$

Babu, Leung, Pantaleone

Chankowski, Pluciennik

Antusch, Drees, Kersten, ML, Ratz, PLB 519 (2001) 238 and PLB 525 (2002) 130

- Example: RG-evolution of bi-maximal mixings at the GUT-scale



$$\Rightarrow \frac{\dot{\theta}_{12}}{\dot{\theta}_{23}} \simeq \frac{\Delta m_{31}^2}{\Delta m_{21}^2} \times \dots \Leftrightarrow \theta_{12} \text{ runs more than } \theta_{23}$$

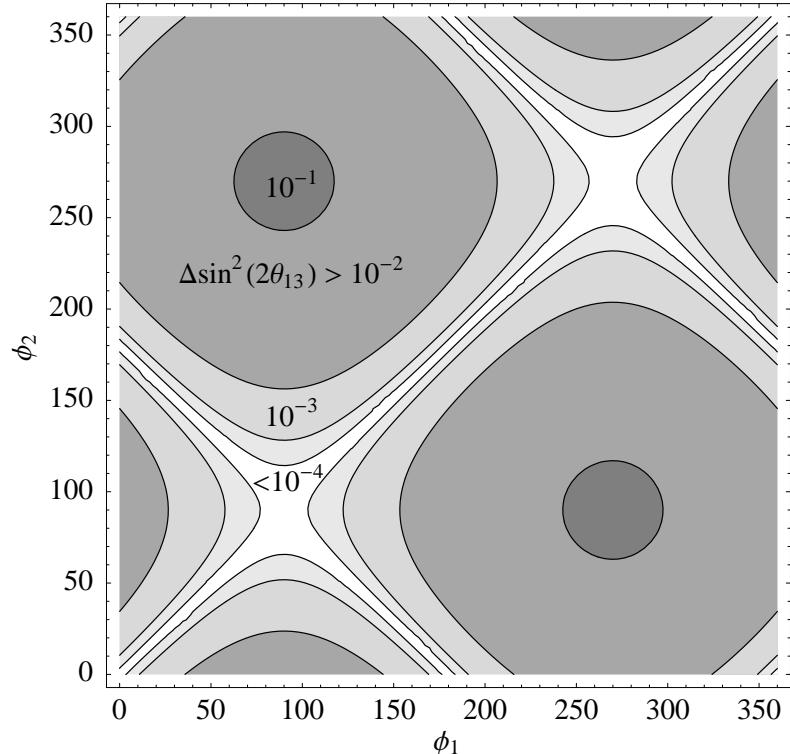
⇒ deviation from bi-maximality can be explained by RGE

Antusch, Kersten, ML, Ratz, Phys.Lett. B544 (2002) 1

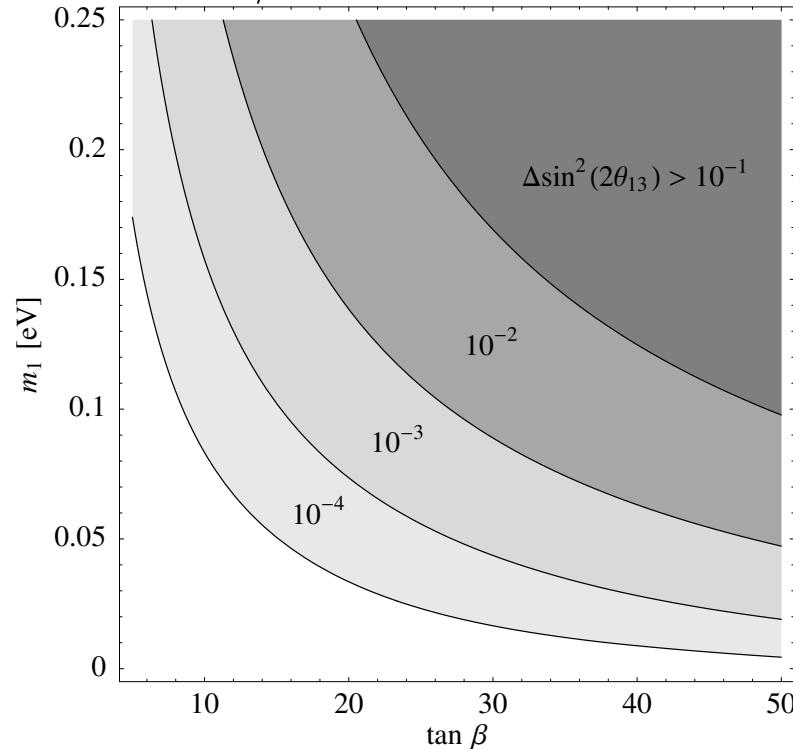
- How big are the RGE effects for θ_{13} ? \Rightarrow change of θ_{13} in MSSM

$$\dot{\theta}_{13} \simeq \frac{y_\tau^2 \sin 2\theta_{12} \sin 2\theta_{23} m_3}{32\pi^2 \Delta m_{\text{atm}}^2} \left[m_1 \cos(\Phi_1 - \delta) - m_2 \cos(\Phi_2 - \delta) - m_3 \frac{\Delta m_{\text{sol}}^2}{\Delta m_{\text{atm}}^2} \cos \delta \right]$$

$\tan \beta = 50, m_1 = 0.1 \text{ eV}, \delta = \pi/2$



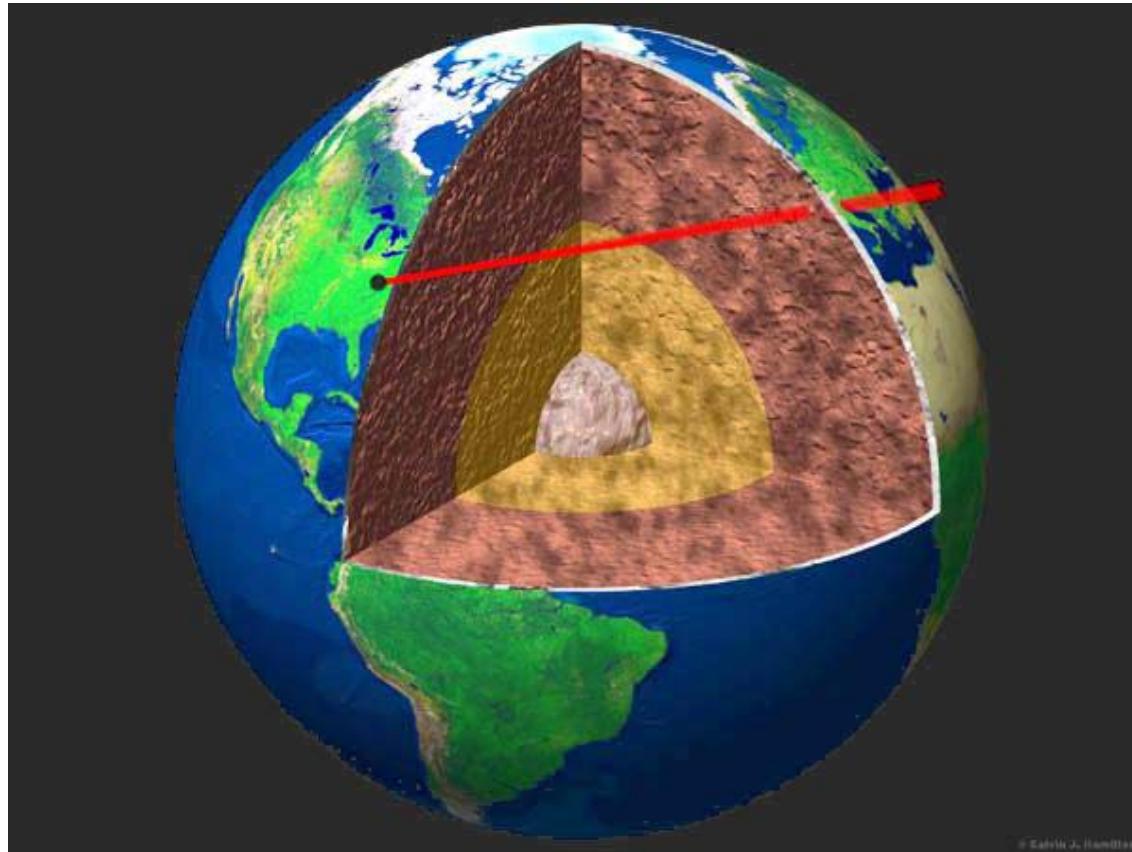
$\delta = \pi/2, \Phi_1 - \Phi_2 = \pi$



- \Rightarrow even for $\theta_{13} = 0$ at the GUT scale **one can often have** $\Delta \sin^2(2\theta_{13}) \geq 10^{-2}$
- \Rightarrow without tuning: typical size of θ_{13} from RGE \Rightarrow sensitivity to $\sin^2(2\theta_{13}) \simeq 10^{-2}$

Antusch, Kersten, ML, Ratz, to appear soon

Hunting $\theta_{13} \neq 0$ with Long Baseline Experiments



Precision!

Source	\otimes	Oscillation	\otimes	Detector
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- neutrino energy E
- flux and spectrum
- flavour composition
- contamination
- symmetric $\nu/\bar{\nu}$ operation

- oscillation channels
- realistic baselines
- MSW matter profile

- effective mass, material
- threshold, resolution
- particle ID (flavour, charge, event reconstruction, ...)
- backgrounds
- x-sections (at low E)

- **Analytic understanding (qualitative)**

- $\Delta = \Delta m_{31}^2 L / 4E$
- matter effects $\hat{A} = A / \Delta m_{31}^2 = 2VE / \Delta m_{31}^2$; $V = \sqrt{2}G_F n_e$
- expand oscillation probabilities in $\alpha = \Delta m_{21}^2 / \Delta m_{31}^2$ and $\sin^2 2\theta_{13}$

$$P(\nu_\mu \rightarrow \nu_\mu) \approx 1 - \cos^2 \theta_{13} \sin^2 2\theta_{23} \sin^2 \Delta + 2 \alpha \cos^2 \theta_{13} \cos^2 \theta_{12} \sin^2 2\theta_{23} \Delta \cos \Delta$$

$$\begin{aligned} P(\nu_\mu \rightarrow \nu_e) &\approx \sin^2 2\theta_{13} \sin^2 \theta_{23} \frac{\sin^2((1-\hat{A})\Delta)}{(1-\hat{A})^2} \\ &\mp \sin \delta_{\text{CP}} \alpha \sin 2\theta_{12} \cos \theta_{13} \sin 2\theta_{13} \sin 2\theta_{23} \sin(\Delta) \frac{\sin(\hat{A}\Delta) \sin((1-\hat{A})\Delta)}{\hat{A}(1-\hat{A})} \\ &+ \cos \delta_{\text{CP}} \alpha \sin 2\theta_{12} \cos \theta_{13} \sin 2\theta_{13} \sin 2\theta_{23} \cos(\Delta) \frac{\sin(\hat{A}\Delta) \sin((1-\hat{A})\Delta)}{\hat{A}(1-\hat{A})} \\ &+ \alpha^2 \sin^2 2\theta_{12} \cos^2 \theta_{23} \frac{\sin^2(\hat{A}\Delta)}{\hat{A}^2} \end{aligned}$$

Cervera, Donini, Gavela, Gomez Cadenas, Hernandez, Mena, Rigolin
 Freund, Huber, ML
 Freund

- **Simplification for vacuum: $V = 0$**

$$\Delta = \Delta m_{31}^2 L / 4E$$

\Rightarrow expansion in powers of $\alpha = \Delta m_{21}^2 / \Delta m_{31}^2 \simeq 10^{-2}$ and $\sin \theta_{13} \leq 10^{-1}$

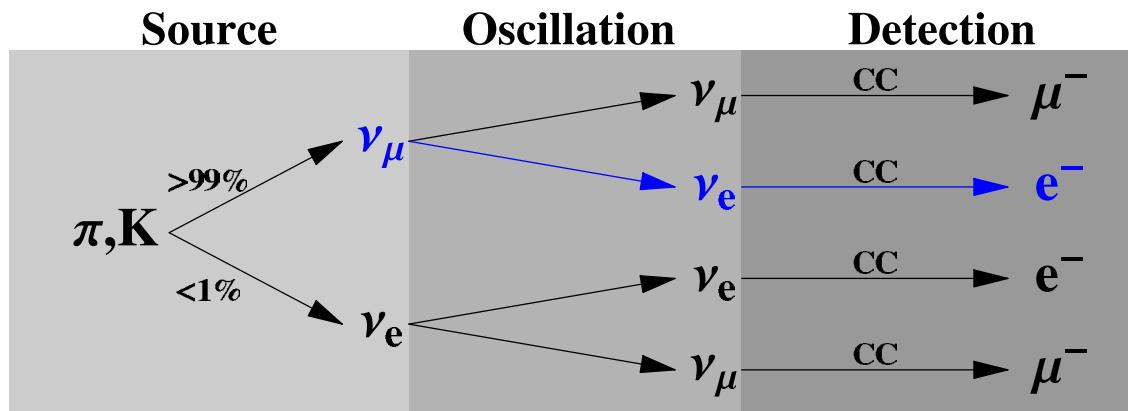
$$\begin{aligned}
 P(\nu_\mu \rightarrow \nu_e) &\approx \sin^2 2\theta_{13} \sin^2 \theta_{23} \sin^2(\Delta) \\
 &\mp \sin \delta_{CP} \alpha \sin 2\theta_{13} \sin 2\theta_{12} \cos \theta_{13} \sin 2\theta_{23} \sin^3(\Delta) \\
 &+ \cos \delta_{CP} \alpha \sin 2\theta_{13} \sin 2\theta_{12} \cos \theta_{13} \sin 2\theta_{23} \cos(\Delta) \sin^2(\Delta) \\
 &+ \alpha^2 \sin^2 2\theta_{12} \cos^2 \theta_{23} \sin^2(\Delta) \\
 &+ \mathcal{O}(\epsilon^3)
 \end{aligned}$$

- most interesting: $\sin^2 2\theta_{13} \simeq \alpha \cdot \sin^2 2\theta_{12} = \sin^2 2\theta_{12} \Delta m_{21}^2 / \Delta m_{31}^2$
- parameter correlations
- depends on solar parameters only via the product $\Delta m_{21}^2 \cdot \sin 2\theta_{12}$
- degeneracies: $(\delta_{CP} - \theta_{13})$, $(\delta_{CP} - \text{sign}(\Delta m_{31}^2))$, $(\theta_{23} - \frac{\pi}{2} - \theta_{23})$
- $\mathcal{O}(\epsilon^3)$ corrections \Leftrightarrow relative contributions $\mathcal{O}(\epsilon)$

• Event rate simulations

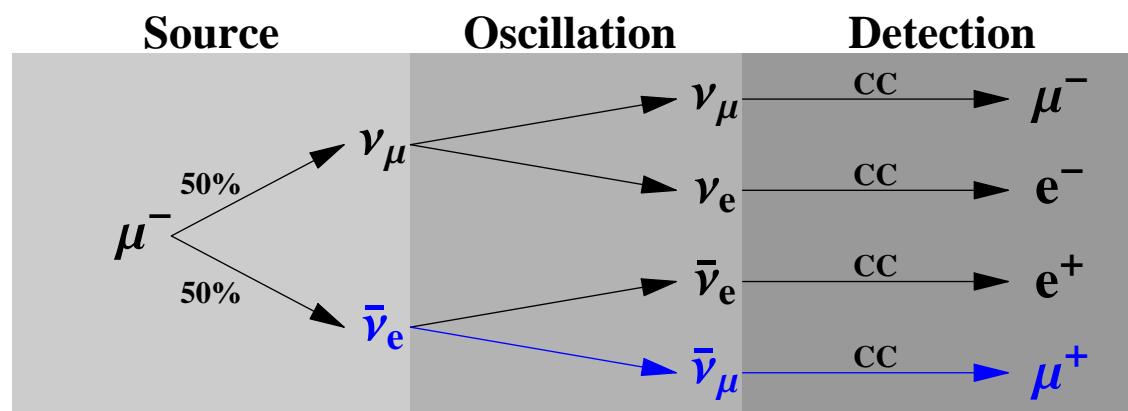
- naive probability based statements are easily many orders of magnitude off
- include all relevant aspects in event rate simulations:
statistics, systematics, backgrounds, efficiencies, resolution, threshold, x-sections, ...
- general three flavour scenario including matter effects (and errors)
- parameters: Δm_{21}^2 , θ_{12} , $|\Delta m_{31}^2|$, θ_{23} , θ_{13} , δ , $\text{sgn}[\Delta m_{31}^2]$ and assume that
 Δm_{21}^2 , θ_{12} are known within 10% at 1σ (KamLAND, K2K, MINOS, CNGS)
- simulate “data” for fixed “true values” of oscillation parameters
- perform 6-parameter fit:
take into account correlations and degeneracies
include available external information **and their errors**
determine sensitivity, precision etc.
- optimization for **individual experiments** and **combinations**
- compare different scenarios on the same footing

• Conventional ν -Beams from Beam Dumps \Rightarrow Superbeams



$\nu_\mu \rightarrow \nu_e$ oscillation most interesting
 ν_e contamination \Leftrightarrow off-axis
 good electron detection efficiency
 good NC background rejection
 near detector
 $\bar{\nu}$ -beam \simeq different experiment

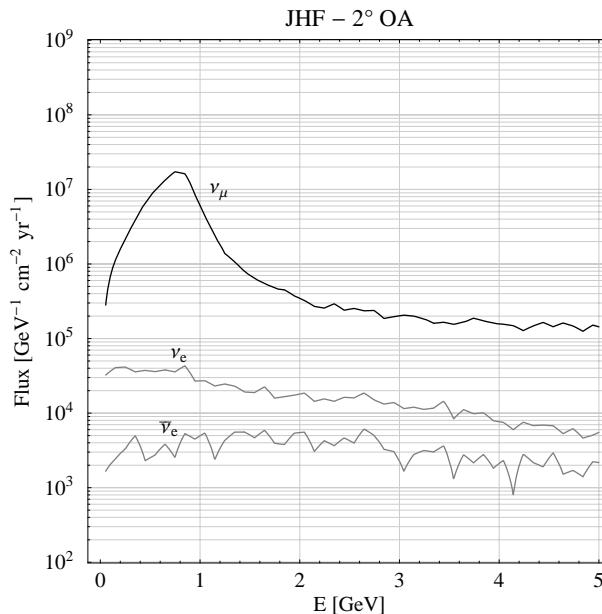
• Neutrino Factories



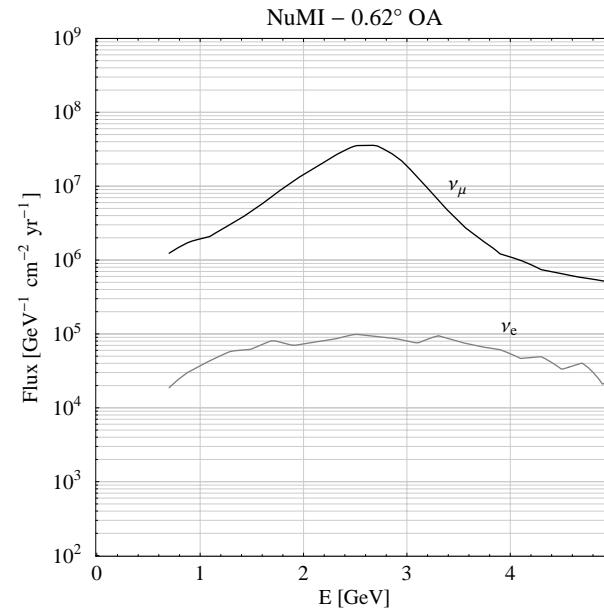
$\bar{\nu}_e \rightarrow \bar{\nu}_\mu$ oscillation most interesting
 excellent beam properties
 very good charge ID required
 good NC background rejection
 μ^+ mode very symmetric

• The Sources

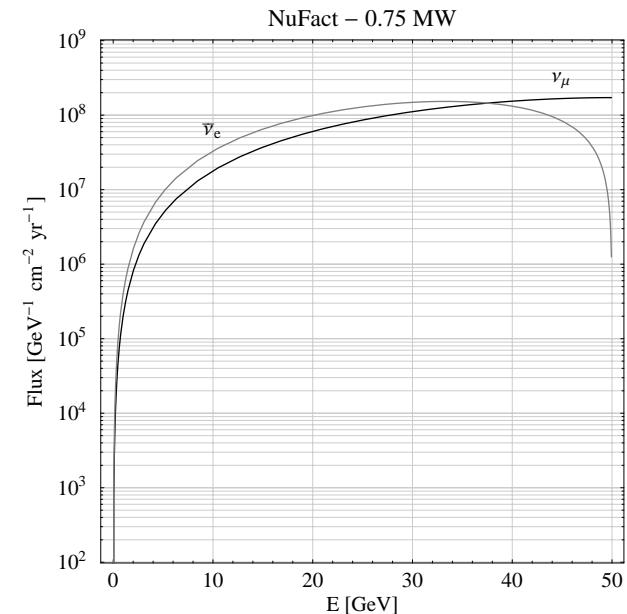
JHF



NuMI off-axis



NuFact



- mean energy 0.51 GeV
- peak intensity $1.7 \cdot 10^7$ GeV⁻¹ cm⁻² yr⁻¹ at 0.78 GeV
- ν_μ/ν_e -ratio at peak 0.2%

- mean energy 2.78 GeV
- peak intensity $3.6 \cdot 10^7$ GeV⁻¹ cm⁻² yr⁻¹ at 2.18 GeV
- ν_μ/ν_e -ratio at peak 0.2%

- mean energy 30 GeV
- peak intensity $1.5 \cdot 10^8$ GeV⁻¹ cm⁻² yr⁻¹ at 33.33 GeV
- ν_μ/ν_e -ratio at peak 83%

Uncertainties in flux and ν_e -background

Itow et al.

Para, Szleper

Uncertainties in flux

Geer

Detectors

	water Cherenkov = SK (HK)	low-Z calorimeter	magnetized iron calorimeter
fiducial mass	22.5 kt (1 000 kt)	20 kt	10 kt (50 kt)
energy range	0.4 – 1.2 GeV	1 – 5 GeV	4 – 50 GeV
energy resolution	5%	10%	20%
signal efficiency	0.5	0.5	0.45
NC rejection	0.01	0.001	$< 10^{-5}$
CID	–	–	$< 10^{-5}$
background uncertainty	5%	5%	5%

- threshold effects for the magnetized iron calorimeter
linear rise of the efficiency between 4 GeV and 20 GeV
- liquid Argon TPC ?

5 Scenarios

	JHF-SK	NuMI	NuFact-I
detector	water cherenkov	low-Z calorimeter	10kt magnetized iron calorimter
baseline	295 km	735 km	3 000 km
matter density	2.8 g cm^{-3}	2.8 g cm^{-3}	3.5 g cm^{-3}
L/E_{peak}	378 km GeV^{-1}	337 km GeV^{-1}	90 km GeV^{-1}

- JHF-HK \Rightarrow $\simeq 95$ times more luminosity than JHF-SK plus anti-neutrino running
- NuFact-II \Rightarrow $\simeq 42$ times more luminosity than NuFact-I

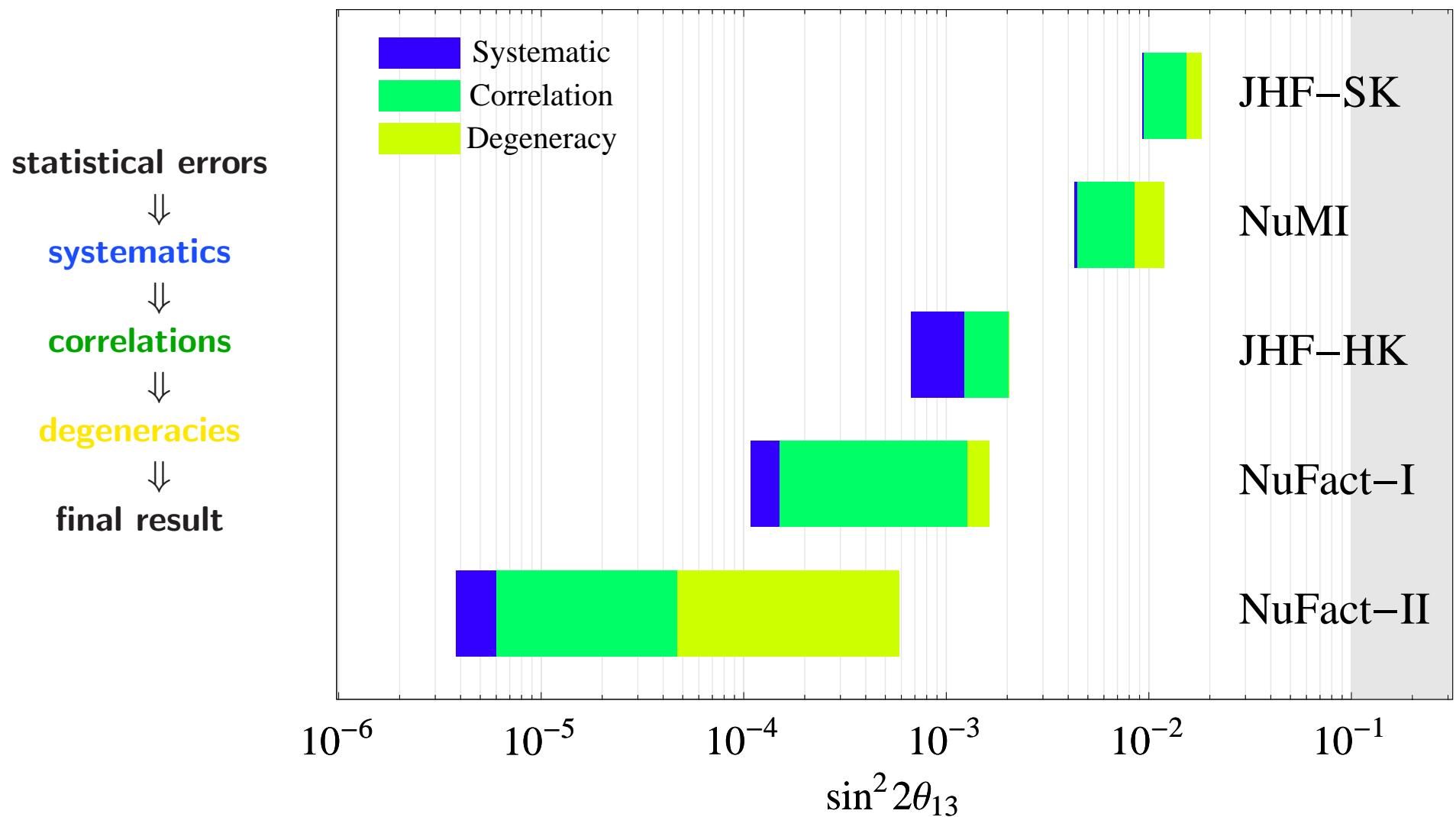
Itow et al., A. Para, A. Blondel et al.

	JHF-SK	NuMI	JHF-HK	NuFact-I	NuFact-II
signal	139.0	387.5	13 180.0	1 522.8	64 932.6
background	23.3	53.3	2 204.6	4.2	180.3
S/N	6	6	6	360	360

- Compare the setups

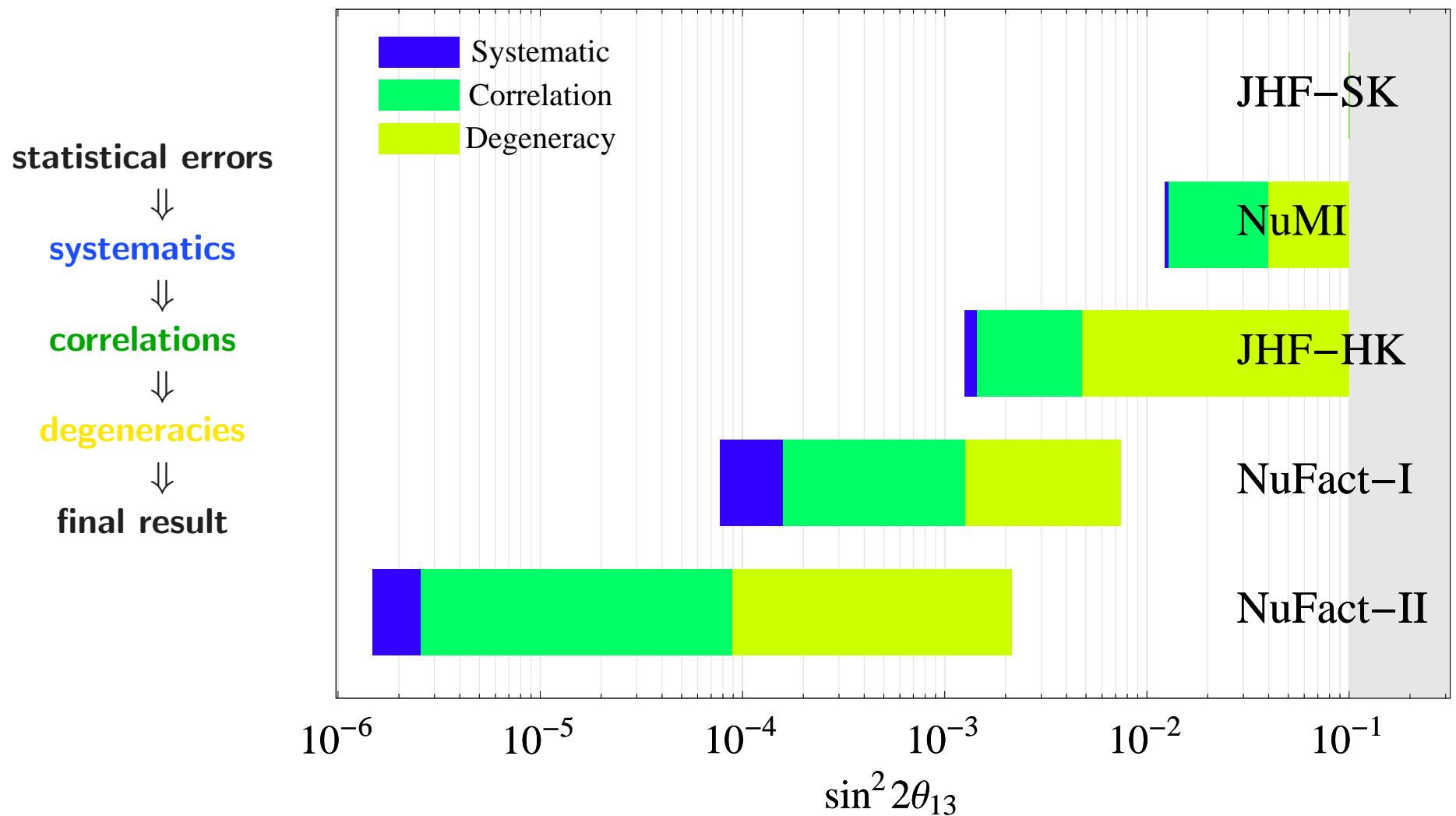
Huber, ML, Winter, NPB 645 (2002) 3

Sensitivity to $\sin^2 2\theta_{13}$



- Different sensitivity reductions by systematics
- Correlations & degeneracies lead to severe limitations
- Improvements by combining experiments

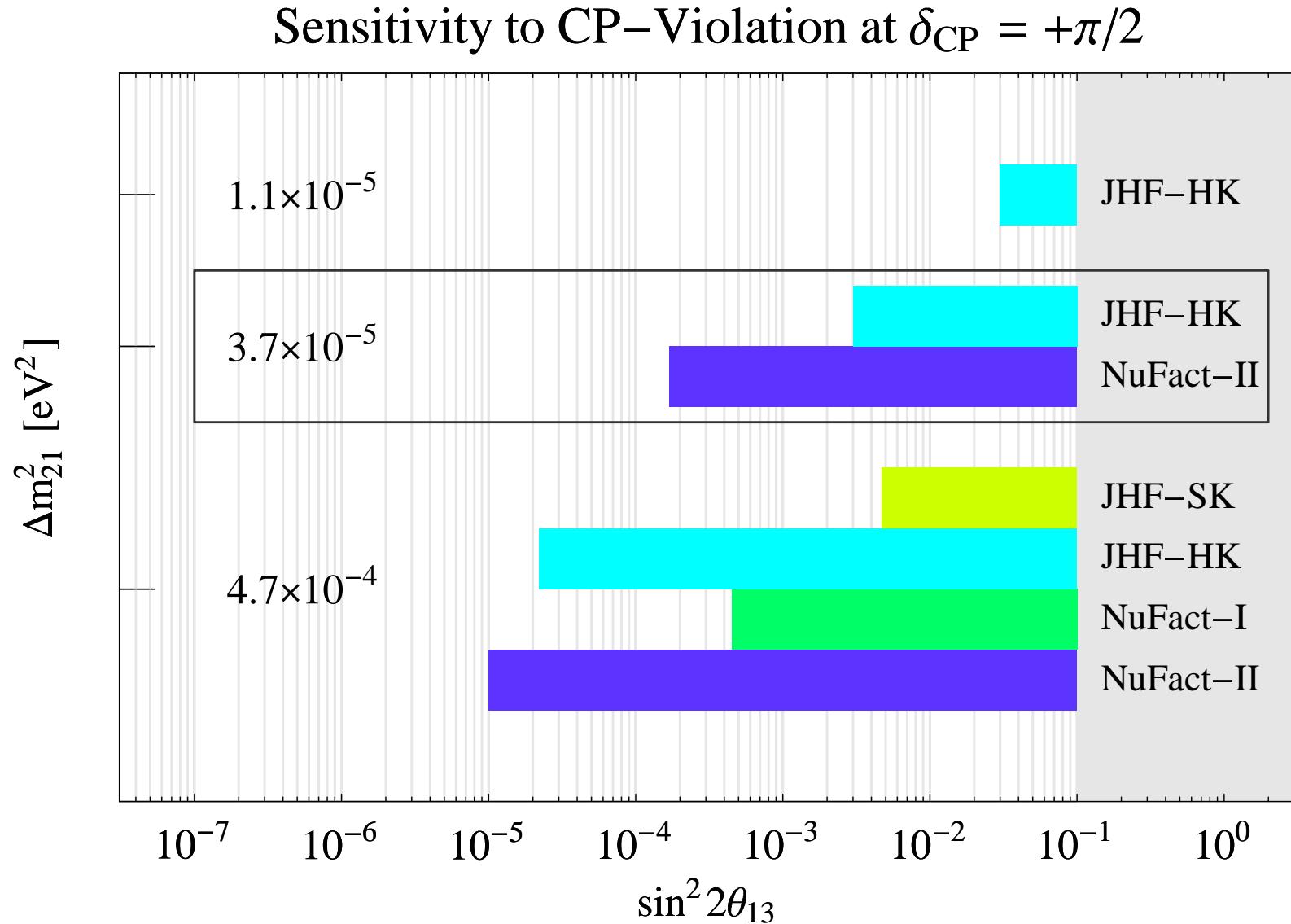
Sensitivity to the sign of Δm_{31}^2



- $sign(\Delta m_{31}^2)$ very hard to determine with superbeams
 - degeneracies with δ_{CP} are the main problem
- ⇒ combine experiments!

Huber, ML, Winter, NPB 645 (2002) 3

Measurements of CP-violation



- CP violation with high luminosity superbeams feasible
- sensitivity is δ_{CP} dependent

Huber, ML, Winter, NPB 645 (2002) 3

• Combine the Next Generation of LBL Experiments

Huber, ML, Winter, NPB 654 (2003) 3

- $\nu_\mu \rightarrow \nu_e$ appearance using an up-graded conventional ν_μ -beam
- **JHF-SK** combined with **NuMI off-axis** as given in LOIs

	JHF-SK	NuMI
	Y.Ito et al. hep-ex/0106019	D.Ayres et al. hep-ex/0210005
Beam		
Baseline	295 km	712 km
Target Power	0.77 MW	0.4 MW
Off-axis angle	2°	0.72°
Mean energy	0.76 GeV	2.22 GeV
Mean L/E	385 km GeV^{-1}	320 km GeV^{-1}
Detector		
Technology	Water Cherenkov	Low-Z calorimeter
Fiducial mass	22.5 kt	17 kt
Running period	5 years	5 years

Typical S/B results:

	JHF-SK	NuMI
Signal	137.8	132.0
Bckgd.	22.6	19.0

- variation-1: NuMI at 890 km and 950 km \Leftrightarrow matter effects
- variation-2: neutrino running only (ν) or mixed ν - $\bar{\nu}$ mode (c)

Sensitivity to $\sin^2 2\theta_{13}$ for JHF–SK & NuMI

statistical errors



systematics



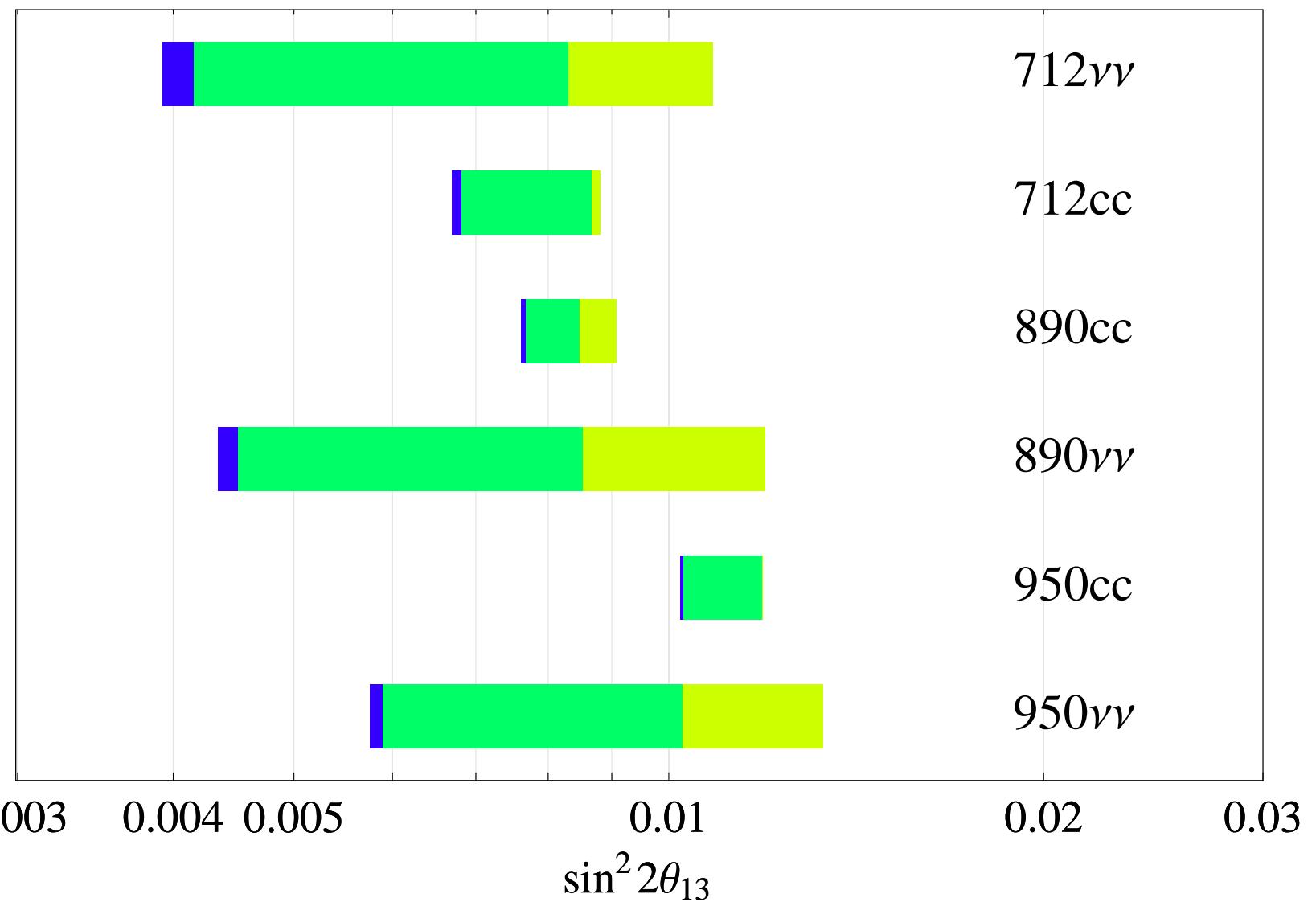
correlations



degeneracies

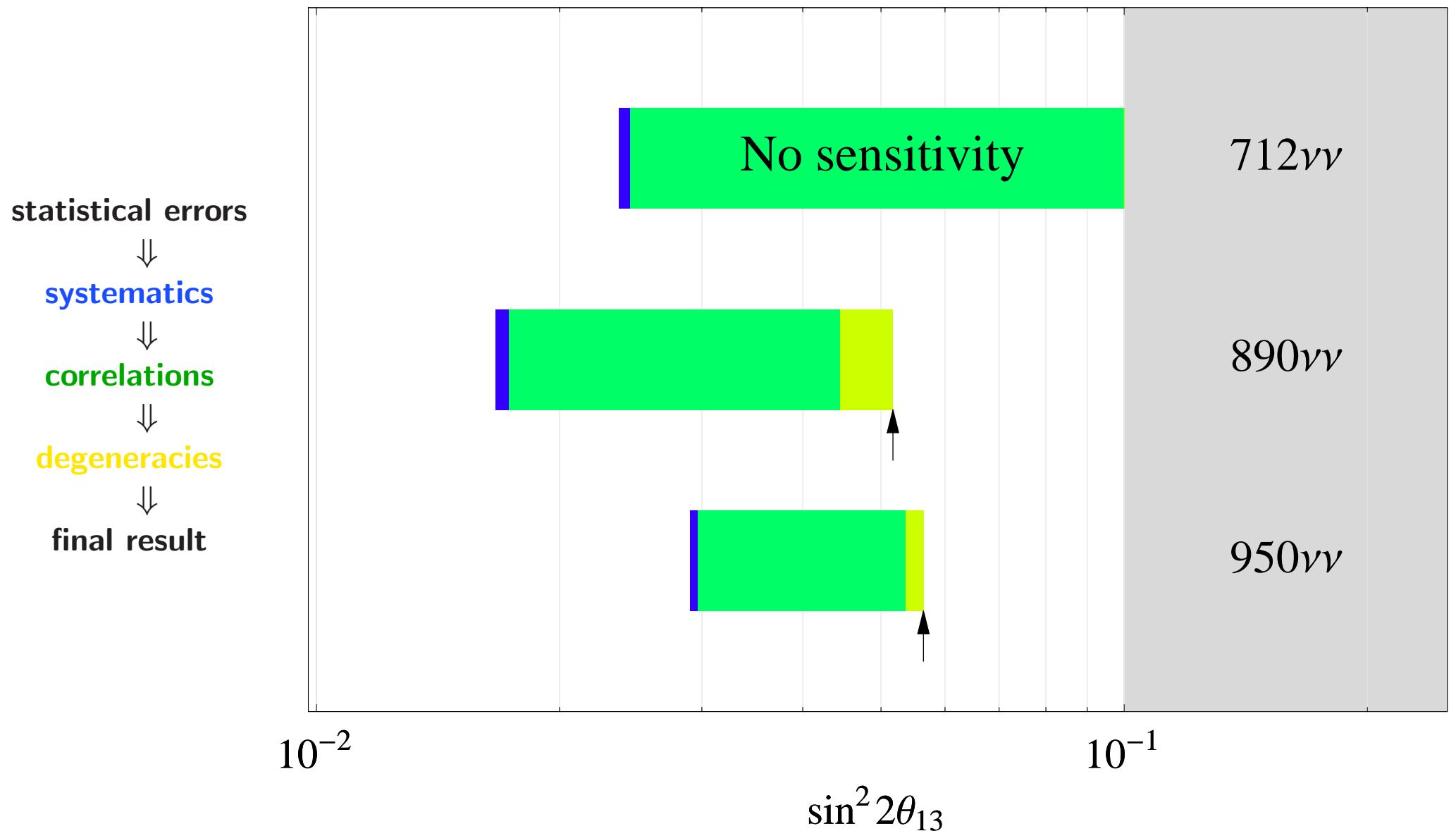


final result



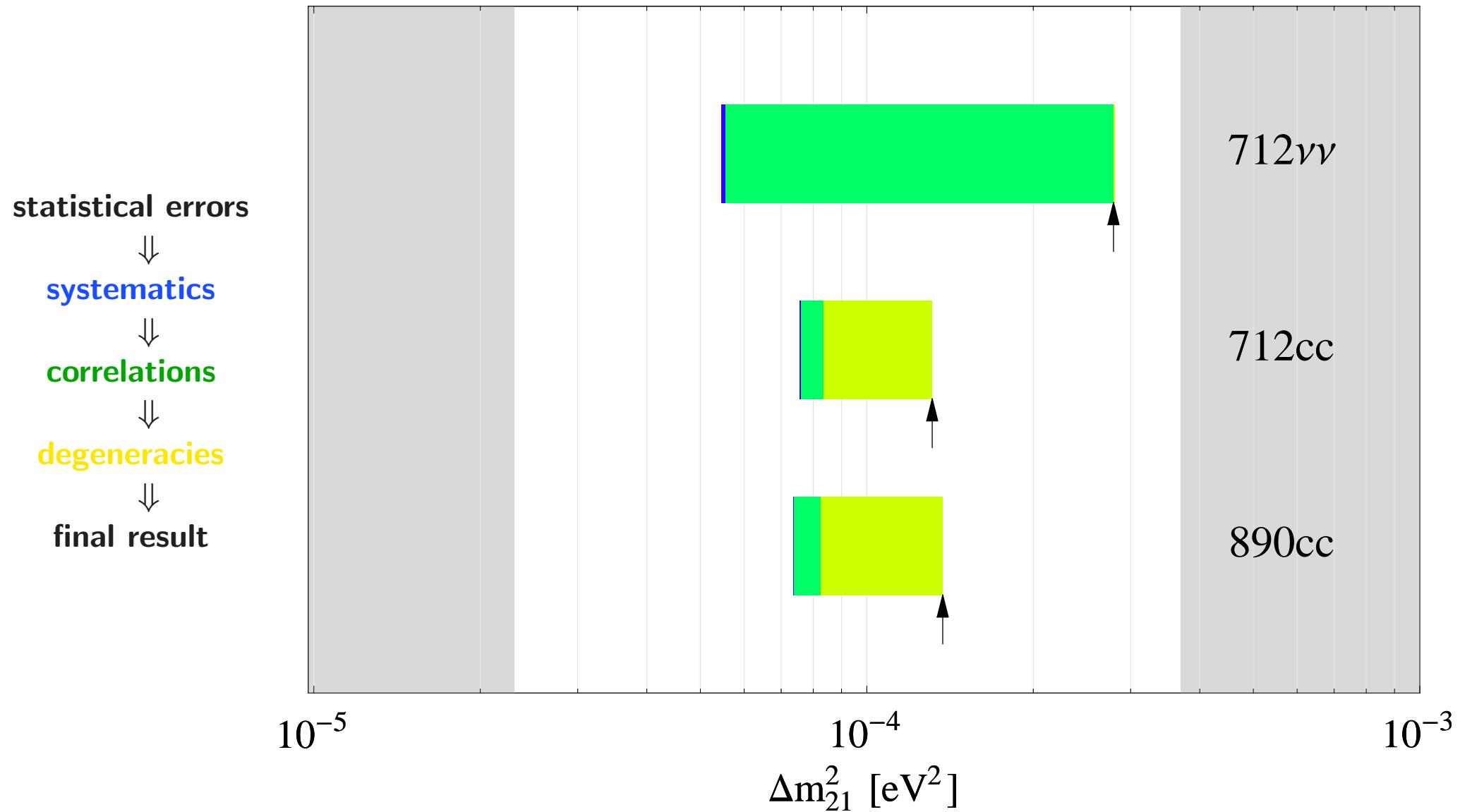
labels: NuMI-baseline(km) JHF-mode(ν, c) NuMI-mode(ν, c)

Sensitivity to $\text{sgn}(\Delta m_{31}^2)$ for JHF–SK & NuMI



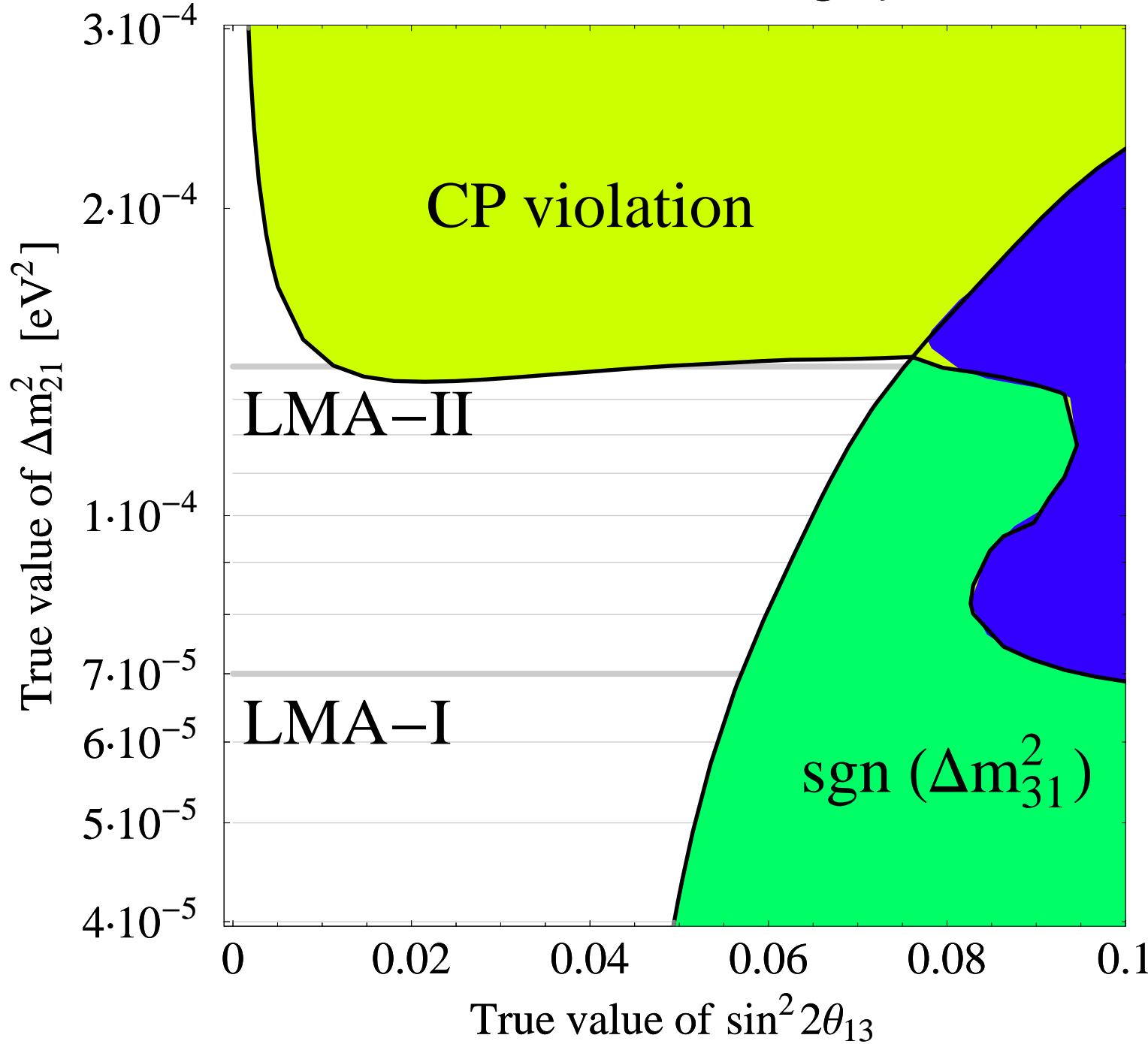
labels: NuMI-baseline(km) JHF-mode(ν, c) NuMI-mode(ν, c)

Sensitivity to CP violation for JHF–SK & NuMI



labels: NuMI-baseline(km) JHF-mode(ν, c) NuMI-mode(ν, c)

JHF–SK & NuMI@890km



Hunting $\theta_{13} \neq 0$ with New Reactor Experiments

- **Many successful experiments**

- Gösgen, G. Zacek et al., Phys. Rev. D34 (1986) 2621
- Bugey, Y. Declais et al., Nucl. Phys. B434 (1995) 503
- CHOOZ, M. Apollonio et al., Phys. Lett. B466 (1999) 415
- Palo Verde, F. Boehm et al., Phys. Rev. D64 (2001) 112001
- KamLAND, Eguchi et al., Phys. Rev. Lett. 90 (2003) 021802
- ...

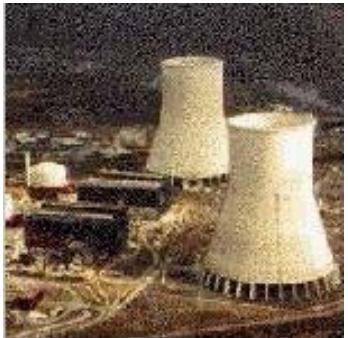
- **Proposals for future reactor experiments:**

- V. Martemyanov, L. Mikaelyan, V. Sinev, V. Kopeikin, Y. Kozlov, hep-ex/0211070
- H. Minakata, H. Sugiyama, O. Yasuda, K. Inoue, F. Suekane, hep-ph/0211111
- M. Shaevitz, Talk at NOON 2003, Kanazawa, Japan
- S. Schönert, T. Lasserre, L. Oberauer, Astropart. Phys. 18 (2003) 565, hep-ex/0203013

detailed study

Huber, ML, Schwetz, Winter, hep-ph/0303232

- The idea:



$$\overline{\nu}_e \rightarrow$$

near detector (170m)

$$\overline{\nu}_e \rightarrow$$

far detector (1700m)

- detection of $\overline{\nu}_e$ by
$$\overline{\nu}_e + p \rightarrow e^+ + n$$
- $E_\nu = E'_e + m_n - m_p$
- prompt energy: $E_{\text{prompt}} = E_{\text{kin}} + 2m_e$
- prompt positron energy and delayed γ from neutron capture
- **identical near and a far detectors \Rightarrow look for distortions**
 - \simeq eliminate reactor information / uncertainties (flux, spectrum)
 - eliminate x-section errors
 - relative precision is easier than absolute precision
- high event rates \Rightarrow use rates **and** spectral information

- **The survival probability:**

- expand in small quantities

$$P_{ee} \approx 1 - \sin^2 2\theta_{13} \sin^2 \frac{\Delta m_{31}^2 L}{4E_\nu} + \left(\frac{\Delta m_{21}^2 L}{4E_\nu} \right)^2 \cos^4 \theta_{13} \sin^2 2\theta_{12}$$

- last term negligible for $\frac{\Delta m_{31}^2 L}{4E_\nu} \sim \pi/2$ and $\sin^2 2\theta_{13} \gtrsim 10^{-3}$
- atmospheric frequency is dominant
- most important:

- No degeneracies!
- Practically no correlations!
- No matter effects!

⇒ evaluate the potential on event rate basis...

- **The setup:**

- one reactor block (spread of individual reactors negligible)
- far detector at **1.7 km**, near detector at **~ 170 m**
- identical near and far detectors ($\geq 10\times$ more events in the near than in the far detector)
- assume background free measurement **Schönert, Lasserre, Oberauer, hep-ex/0203013**
- 62 bins in E_{prompt} from 1 to 7.2 MeV, number of events in bin i :

$$N_i = \mathcal{N} \int dE_\nu \sigma(E_\nu) \varphi(E_\nu) P_{ee}(E_\nu) \int_i dE_e R(E_e, E'_e)$$

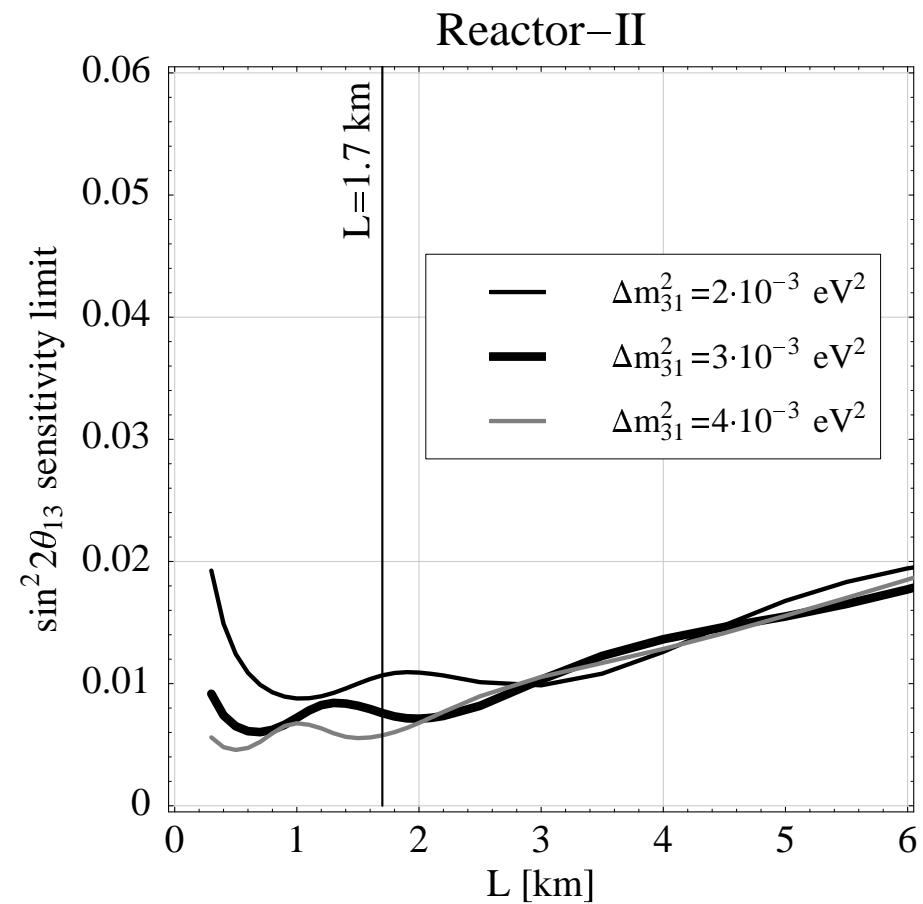
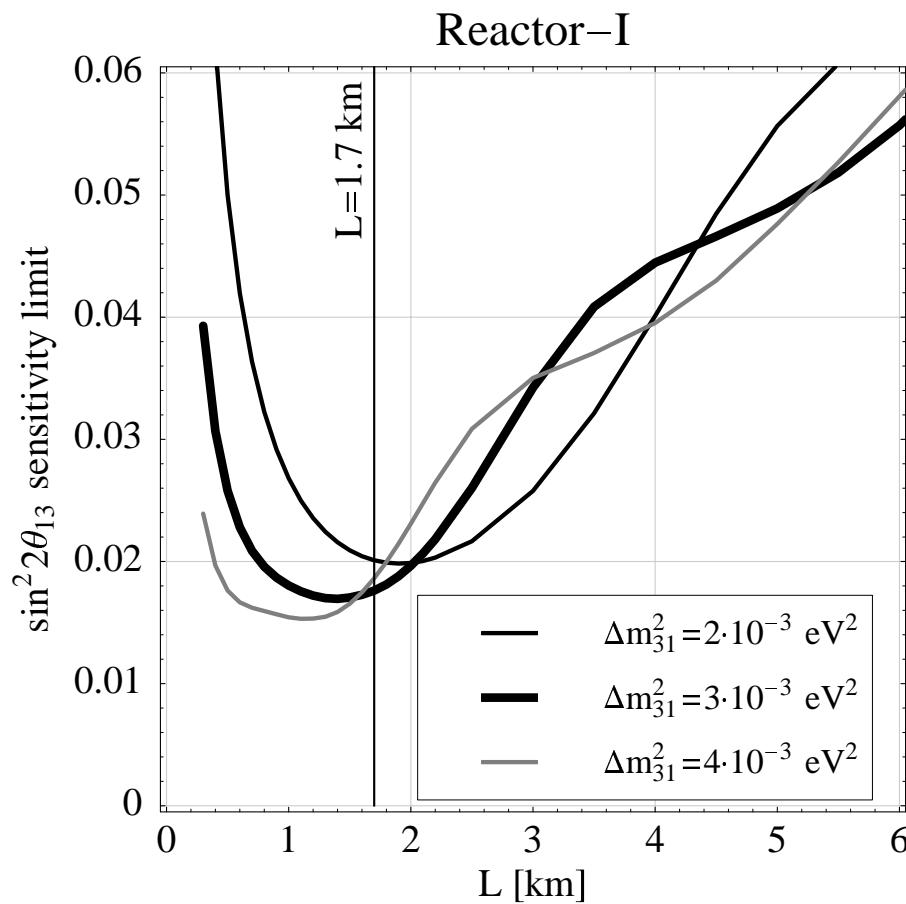
- R : energy resolution $5\%/\sqrt{E_e(\text{MeV})}$
- $\mathcal{N} \propto$ integrated luminosity \mathcal{L}
- $\mathcal{L} \equiv$ detector mass [t] \times thermal reactor power [GW] \times running time [y]

12t detector, 7 GW thermal power, 5 years running time \Rightarrow 400 t GW y

250t detector, 7 GW thermal power, 5 years running time \Rightarrow 8000 t GW y

- Scenarios and optimal distance

setup	\mathcal{L}	# of events (no osc)	baseline
Reactor-I	400 t GW y	31 500	1.7 km
Reactor-II	8000 t GW y	630 000	1.7 km



• Systematical errors

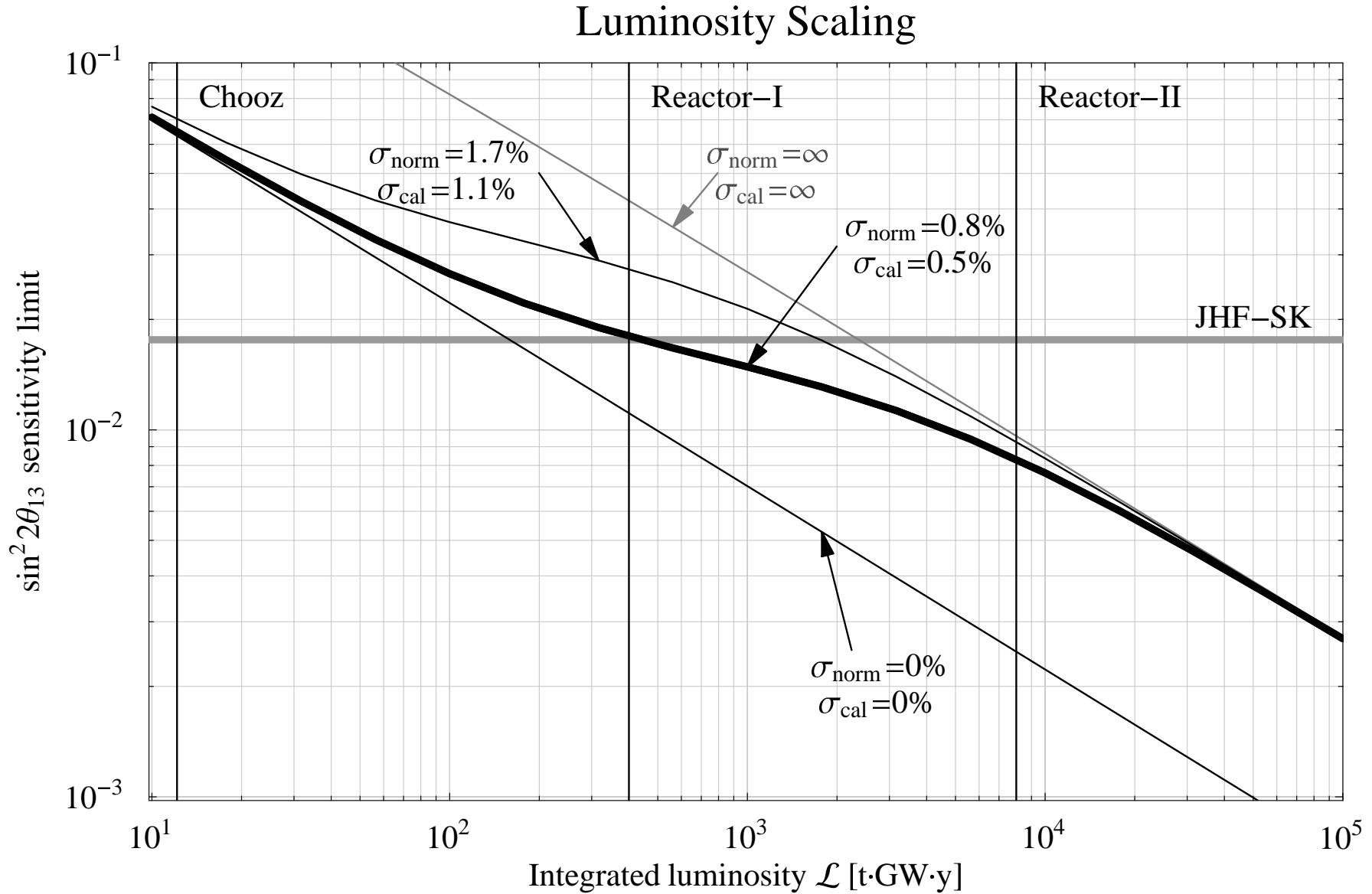
- absolute normalisation error common to both detectors $\sigma_{\text{tot}} \sim \text{few \%}$
e.g., neutrino flux normalisation, cross section uncertainty, ...
- relative normalisation errors of the two detectors $\sigma_{\text{rel}} \lesssim 1\%$
e.g., error on the fiducial masses, ...
 \Rightarrow effective normalisation error for the far detector

$$\sigma_{\text{norm}}^2 \simeq \sigma_{\text{rel}}^2 + \left(\frac{1}{\sigma_{\text{tot}}^2} + \frac{1}{\sigma_{\text{rel}}^2} \right)^{-1}$$

e.g.: $\sigma_{\text{tot}} = 2\%$ and $\sigma_{\text{rel}} = 0.6\% \rightarrow \sigma_{\text{norm}} \simeq 0.8\%$

- energy calibration uncertainty $\sigma_{\text{cal}} \sim 0.5\%$
- shape uncertainty of the expected energy spectrum $\sigma_{\text{shape}} \sim \text{few \%}$
uncorrelated between energy bins, but correlated between detectors
- completely uncorrelated experimental bin-to-bin error $\sigma_{\text{exp}} \lesssim 0.5\%$
e.g., background uncertainty

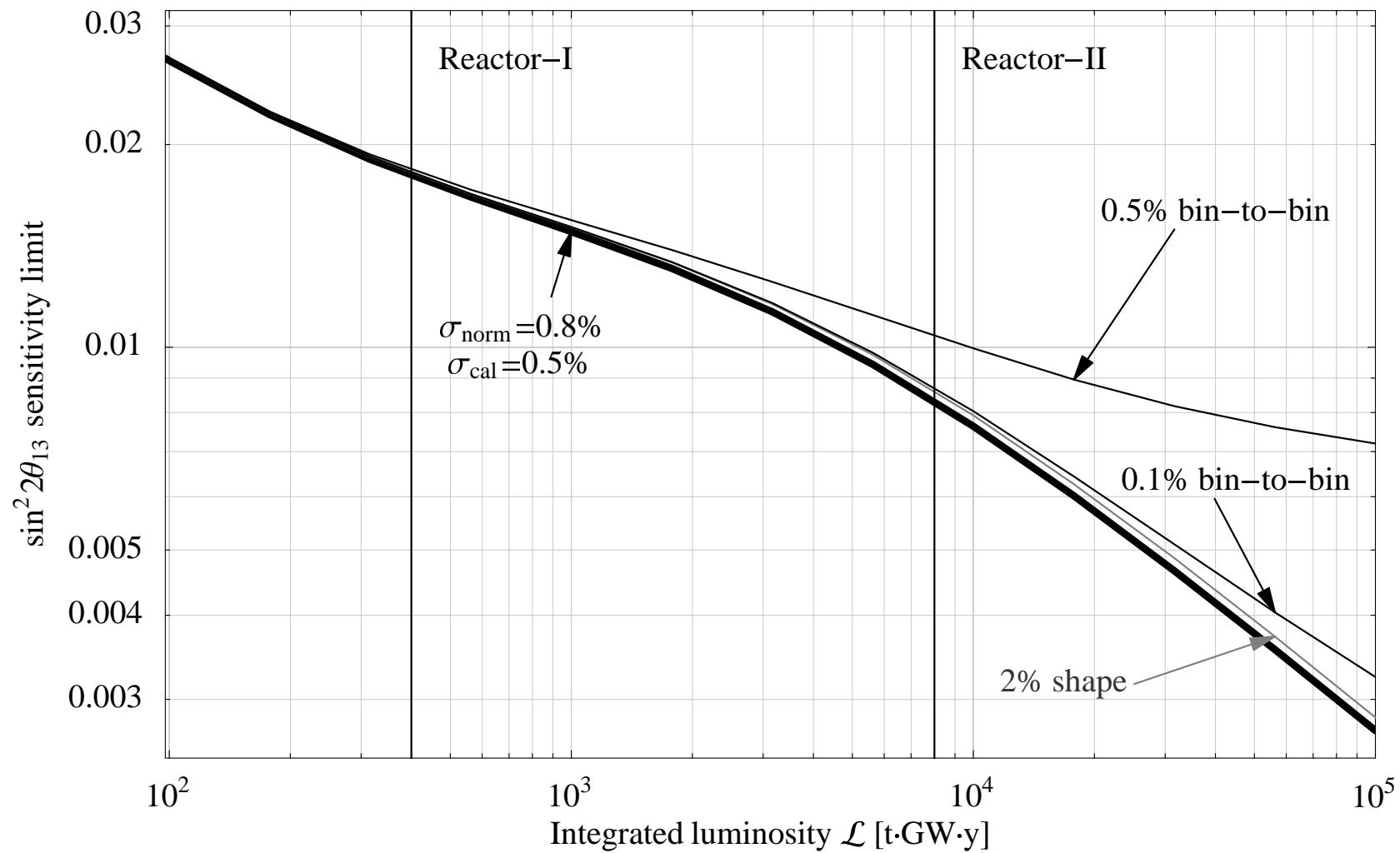
- Sensitivity to $\sin^2 2\theta_{13}$ at 90% CL



Reactor-I: Limit depends crucially on σ_{norm}
Reactor-II: essentially independent of σ_{norm}

- Theoretical shape and experimental bin-to-bin errors

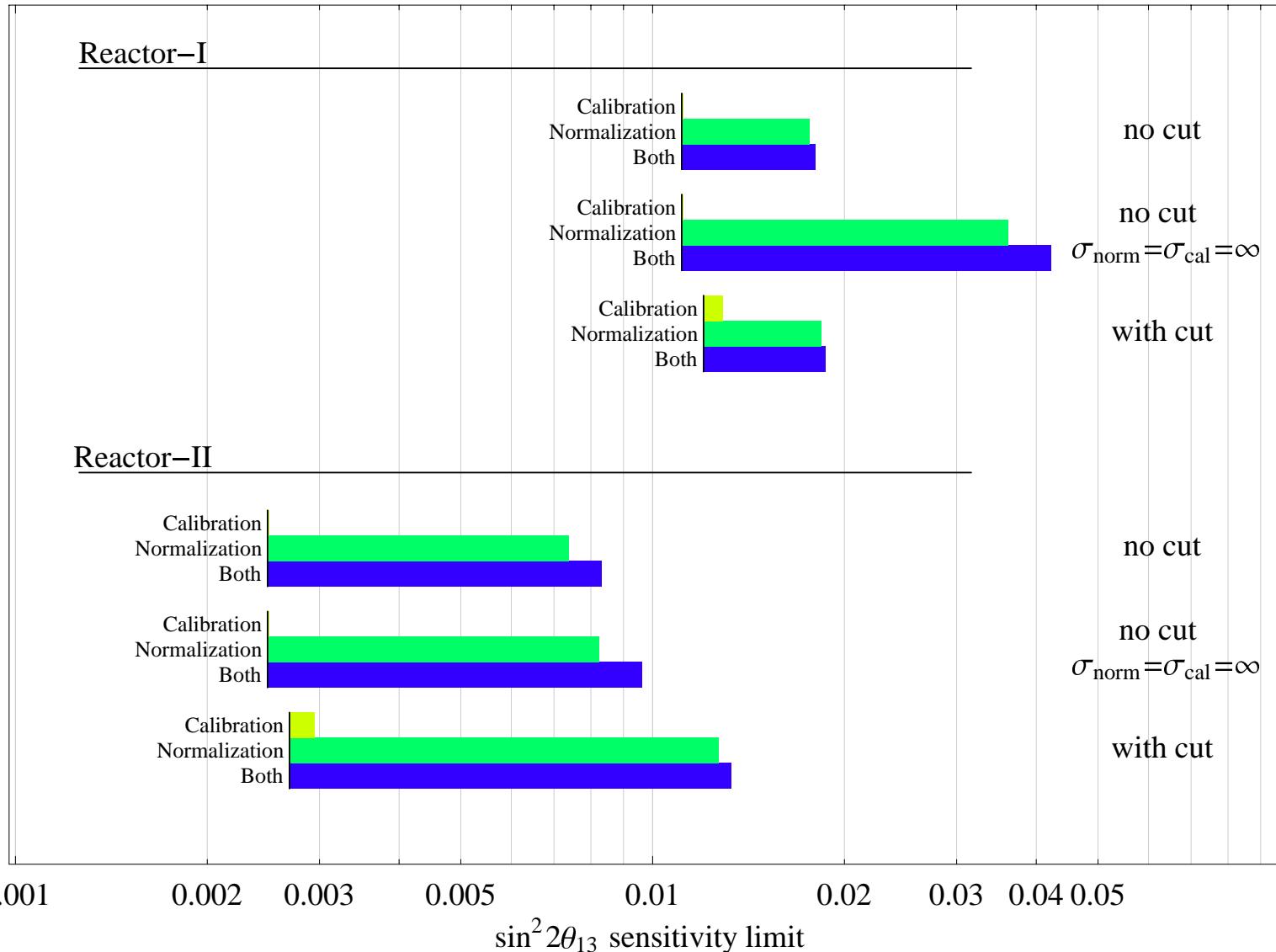
Luminosity Scaling



experimental bin-to-bin error: e.g. back ground uncertainty

a BG of 1% of the signal, known within 10% \rightarrow 0.1% exp. error

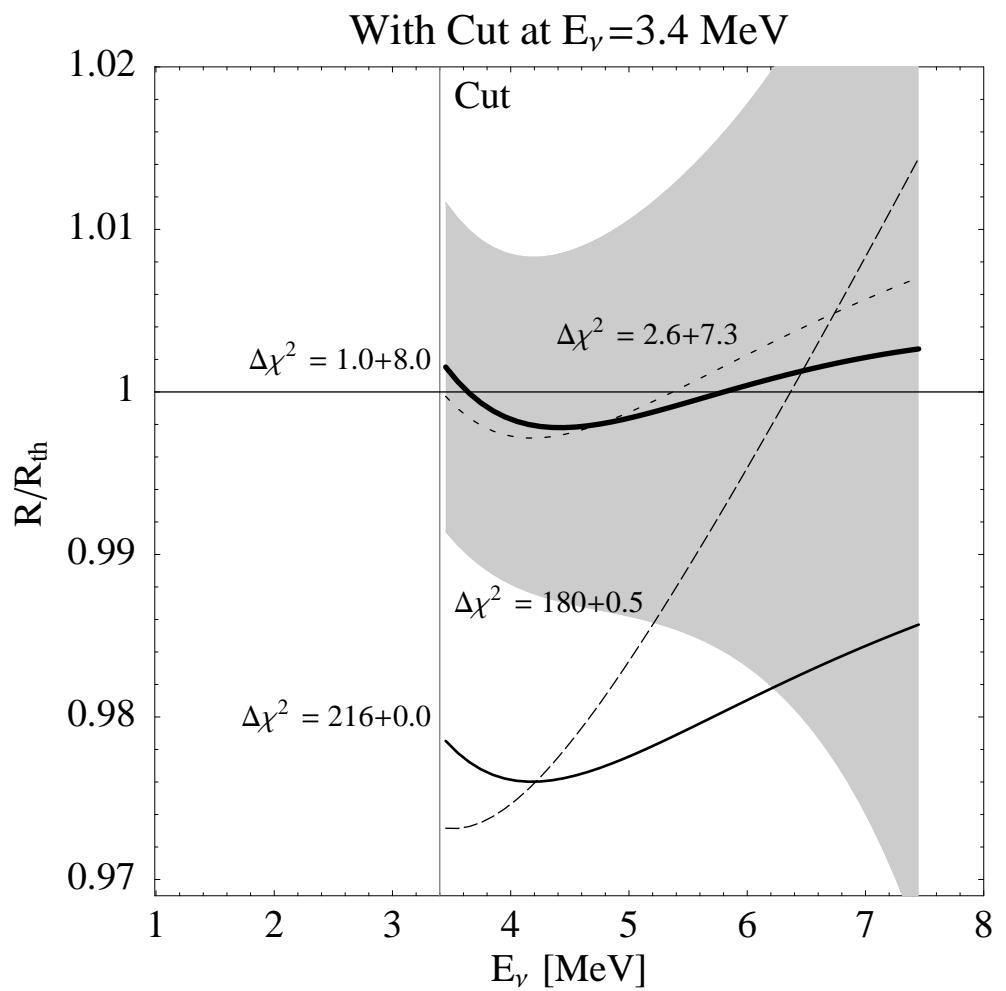
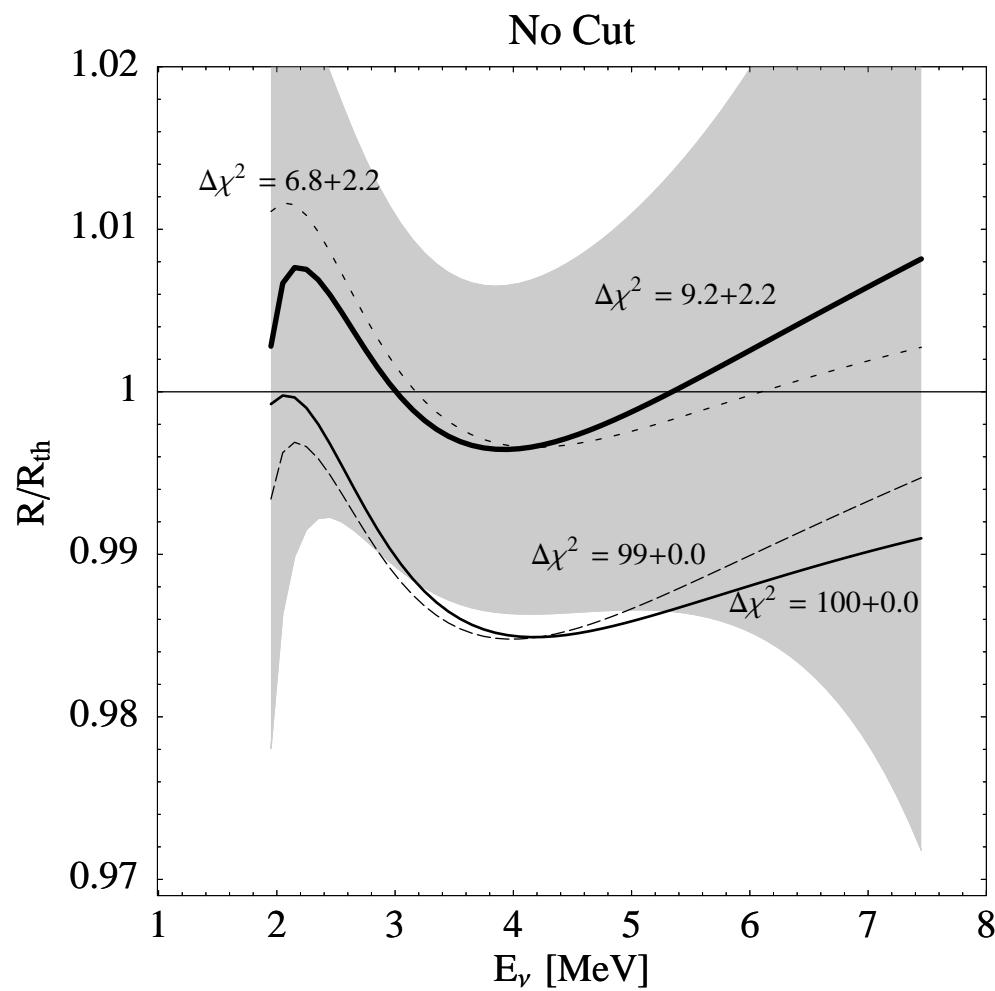
Breakdown of Systematical Errors



Reactor-I:
 σ_{cal} and cut
not important
 σ_{norm} important

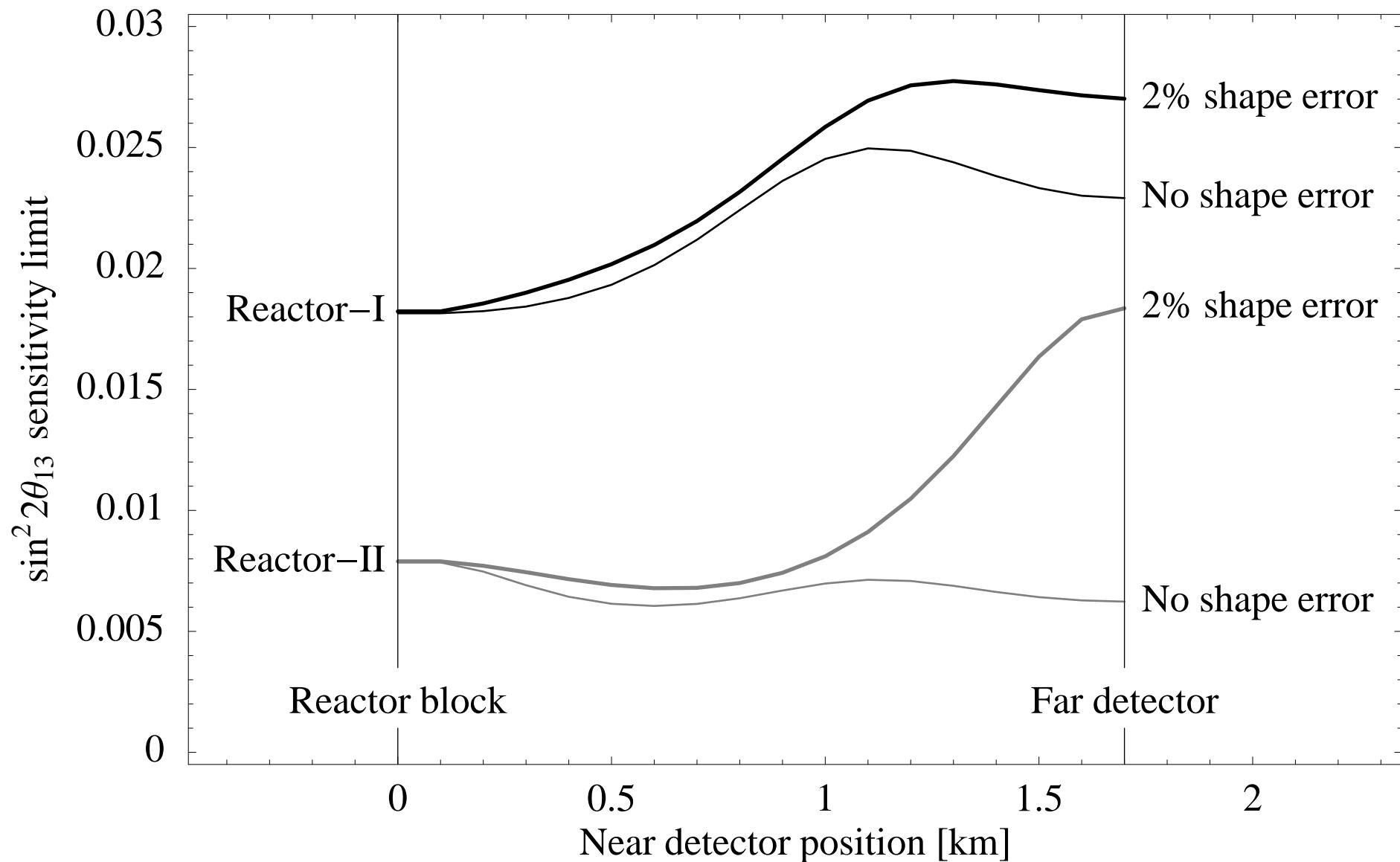
Reactor-II:
 σ_{cal} and σ_{norm}
not important
energy cut
some impact

- Effect of an energy cut



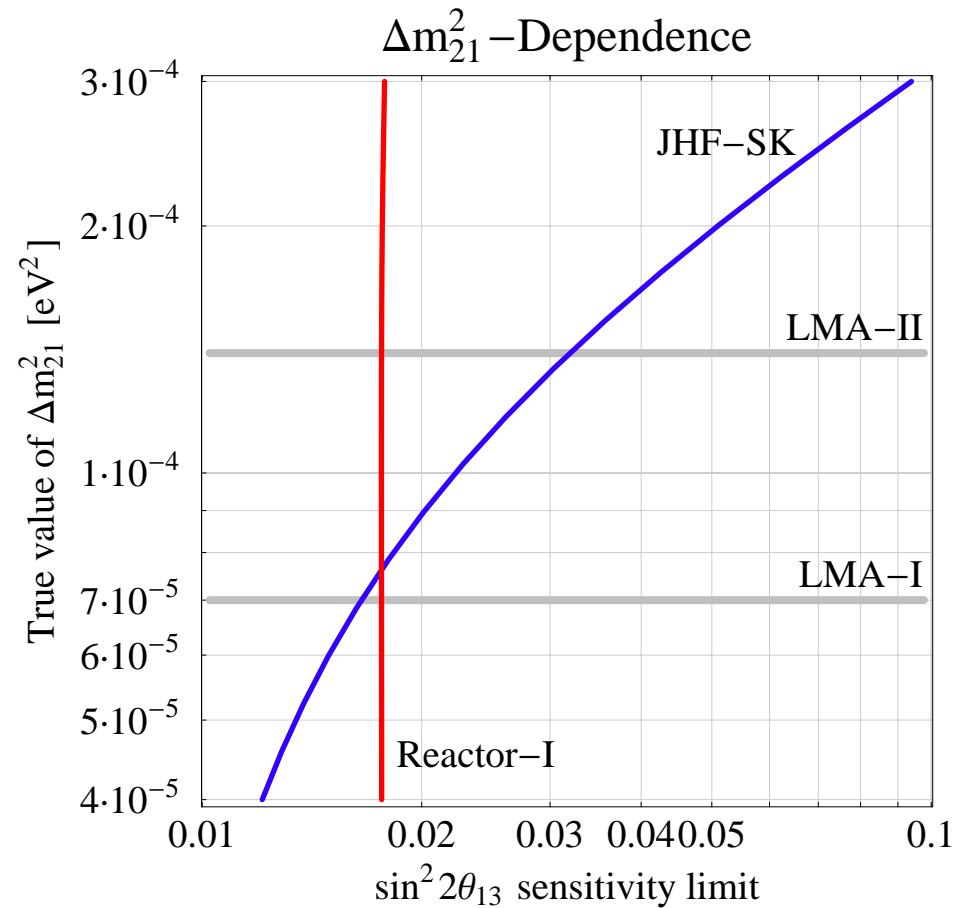
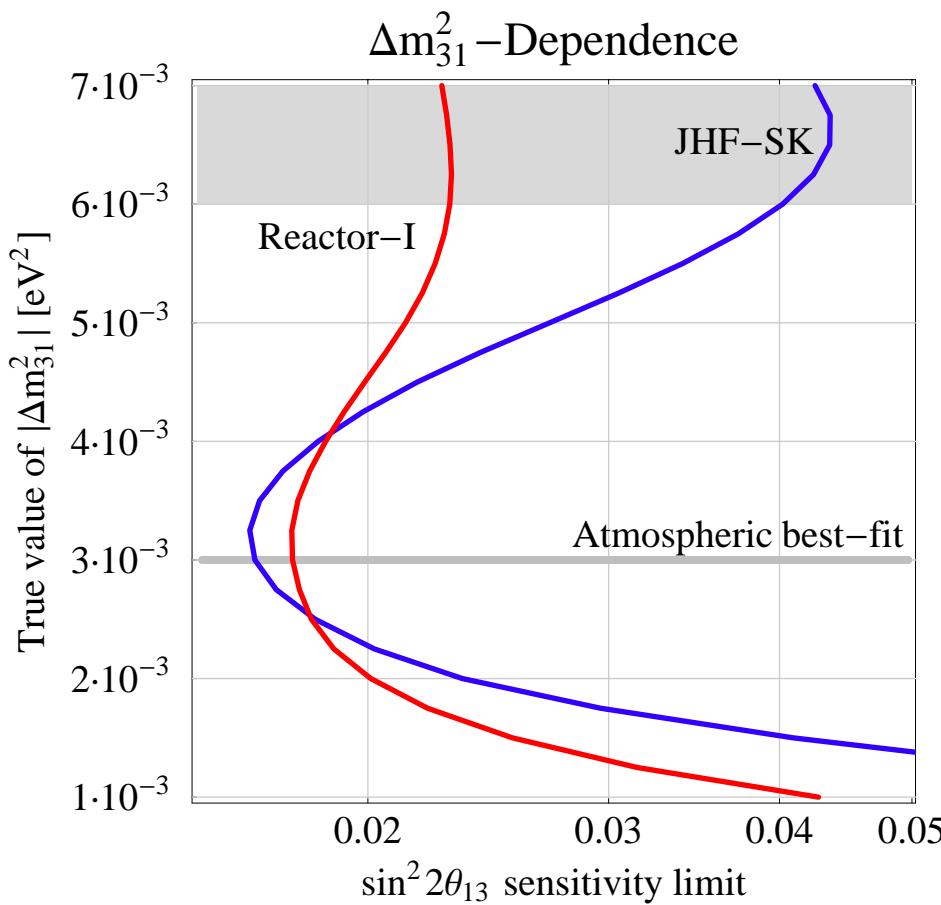
- The position of the near detector

Real sites may not allow a near detector at 0.17 km (no-oscillation) \Rightarrow

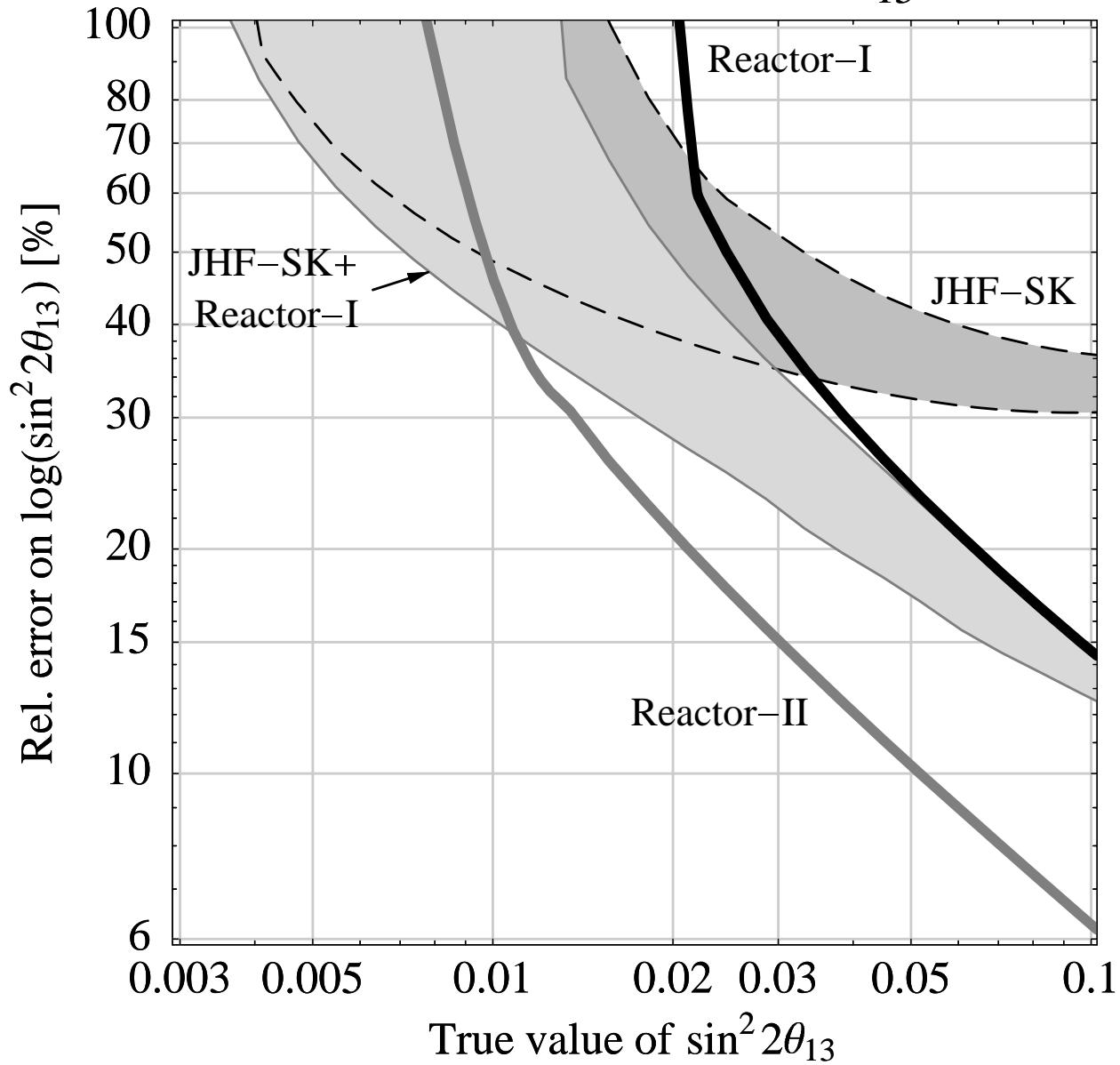


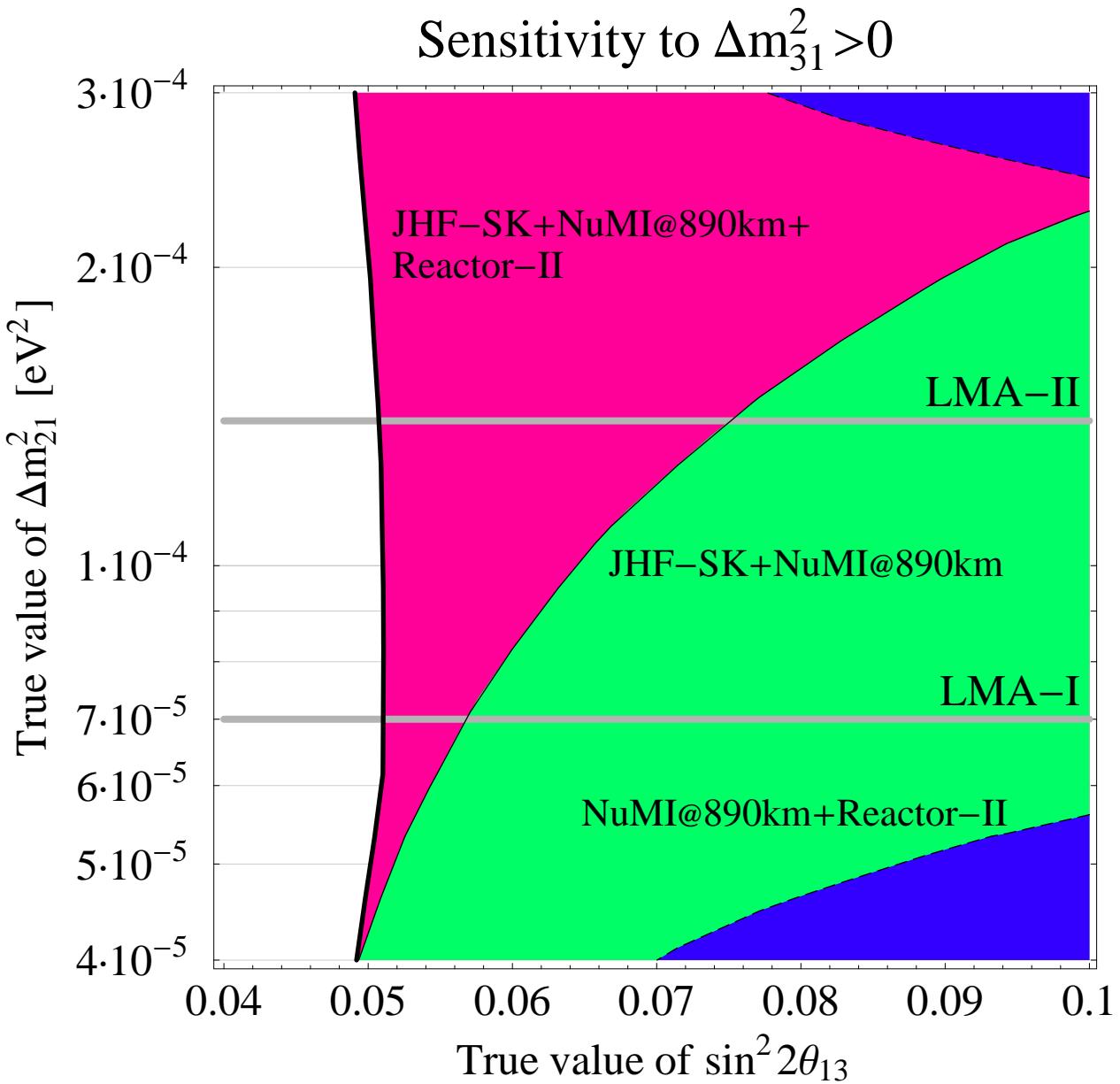
Comparison of Reactor and Superbeam experiments

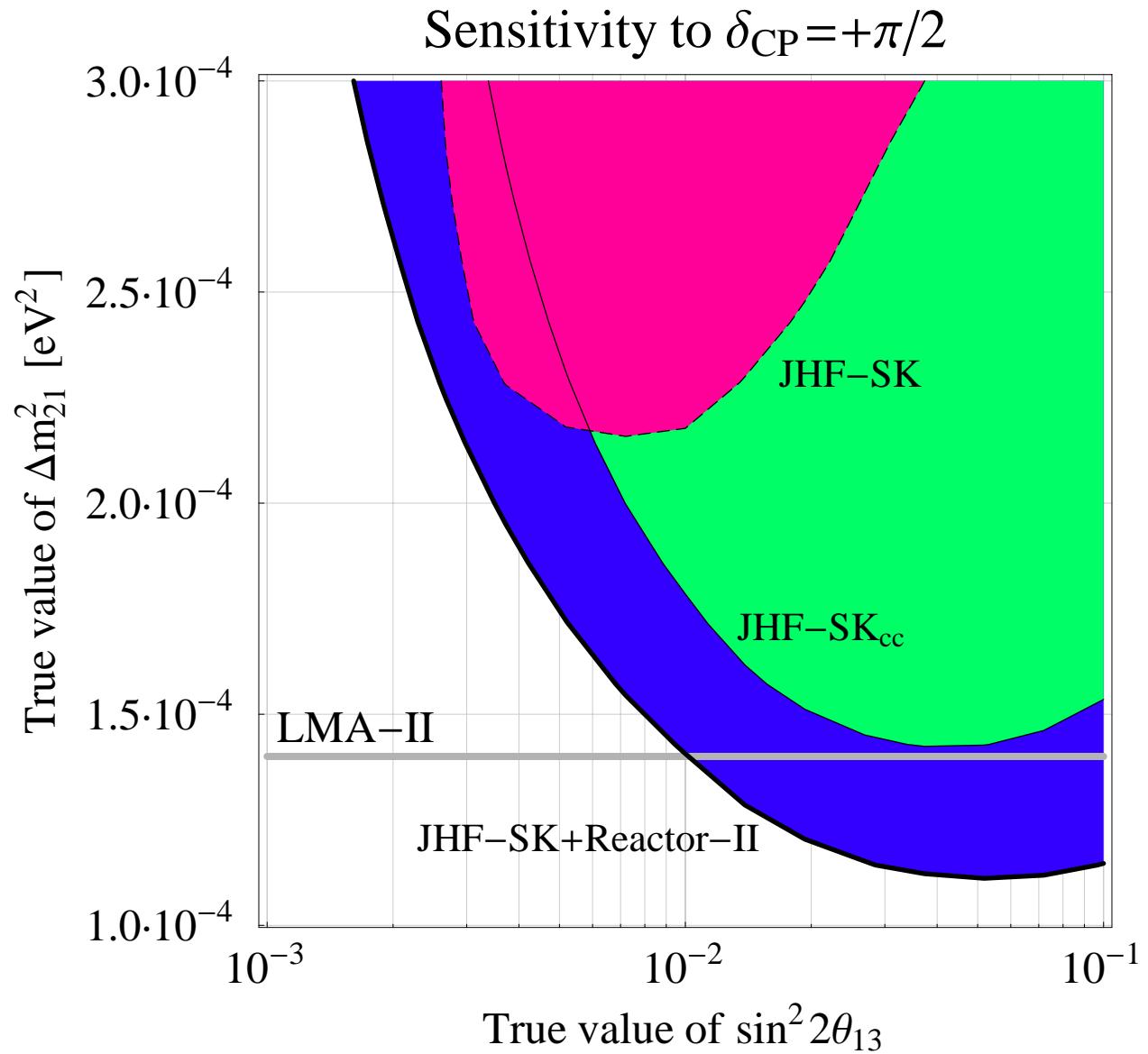
- The sensitivity to $\sin^2 2\theta_{13}$ at 90% CL



The Precision of $\sin^2 2\theta_{13}$







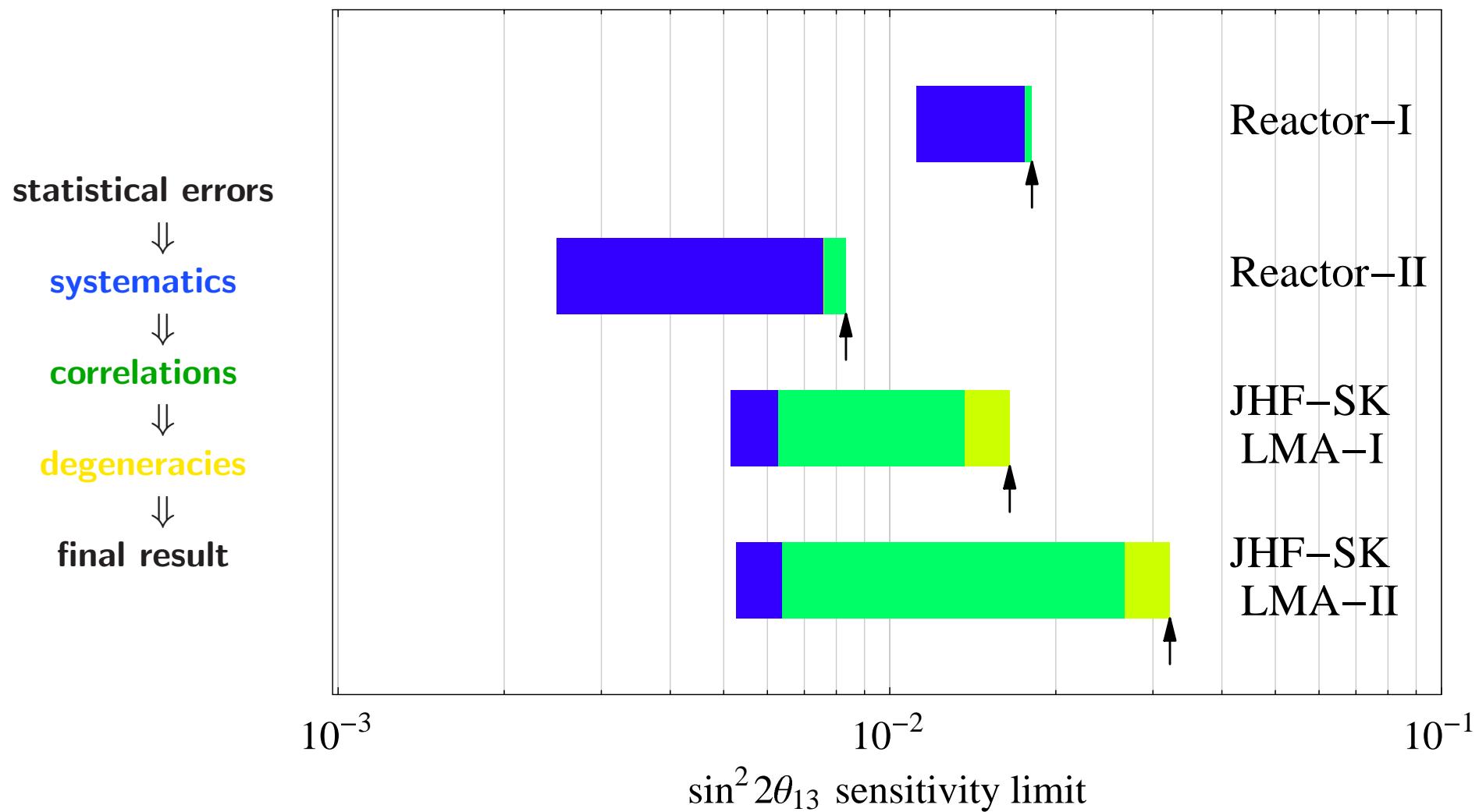
Summary

- a sensitivity of $\sin^2 2\theta_{13} \lesssim 10^{-2}$ seems reachable by reactor neutrino experiments
- near-far detector setup allows the efficient reduction of systematical effects
(over-all normalisation, shape uncertainty)
- Reactor-I ($\mathcal{L} \sim 400 \text{ t GW y}$)
limit depends sensible on a relative normalisation error

Reactor-II ($\mathcal{L} \sim 8000 \text{ t GW y}$)
limit is rather independent of the relative normalisation error
- energy calibration error has no big effect
- experimental bin-to-bin uncorrelated systematical error
should be $\lesssim 0.1\%$ for very large experiments ($\mathcal{L} \gtrsim 10^4 \text{ t GW y}$)

- $\sin^2 2\theta_{13}$ -limit is highly competitive to first generation superbeams

Sensitivity to $\sin^2 2\theta_{13}$



- superbeam experiments suffer from **correlations** and **degeneracies**
.... especially for **large Δm_{21}^2**

- Combined analysis of reactor and superbeam experiments:
 - clean θ_{13} measurement of the reactor resolves degeneracies
- JHF-SK + NuMI@890km + Reactor-II:
significantly improved sensitivity to the neutrino mass hierarchy
- JHF-SK + Reactor-II:
better sensitivity for leptonic CP violation

Reactor neutrino experiments

- are a very promising option to measure θ_{13}
- are complementary to the long-baseline program