

U_{e3} : EXPERIMENTAL AND THEORETICAL CHALLENGES

- WHAT IS U_{e3} , AND WHAT DO WE KNOW ABOUT IT ?
- HOW DO WE GO ABOUT MEASURING IT ?
- PREDICTING U_{e3} : THE THEORETICAL CHALLENGE
 - NEUTRINO MASS ANARCHY
- CONCLUSIONS...

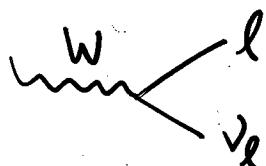
3 FLAVOR NEUTRINO OSCILLATIONS

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

↓ ↓

FLAVOR EIGENSTATES

MASS EIGENSTATES



$$m_{\nu_i} \equiv m_i$$

DEFINING THE MASS EIGENSTATES

- $m_1^2 < m_2^2$ ($\Delta m_{12}^2 = m_2^2 - m_1^2 > 0$)
- $|\Delta m_{13}^2| > \Delta m_{12}^2 \Rightarrow \text{Sign}(\Delta m_{13}^2) \text{ is an "OBSERVABLE"}$

GIVEN THIS (PECULIAR?) DEFINITION

IT TURNS OUT :*

$$\frac{|U_{e3}|^2}{|U_{e1}|^2} = \operatorname{tg}^2 \theta_{12} = \operatorname{tg}^2 \theta_{\text{SOL}}$$

$$|\Delta m_{12}^2| = |\Delta m_{\text{SOL}}^2|$$

$$\frac{|U_{\mu 3}|^2}{|U_{23}|^2} = \operatorname{tg}^2 \theta_{23} = \operatorname{tg}^2 \theta_{\text{ATM}}$$

$$|\Delta m_{13}^2| \approx |\Delta m_{23}^2| = |\Delta m_{\text{ATM}}^2|$$

$$\operatorname{sin}^2 \theta_{13} = |U_{e3}|^2 = ? \quad (\text{CONSTRAINED...})$$

$$J_{CP} = \operatorname{Im} [U_{e3}^* U_{\mu 3} U_{e2} U_{\mu 2}^*] = \frac{1}{8} \operatorname{sin} 2\theta_{23} \times \operatorname{sin} 2\theta_{12} \times$$

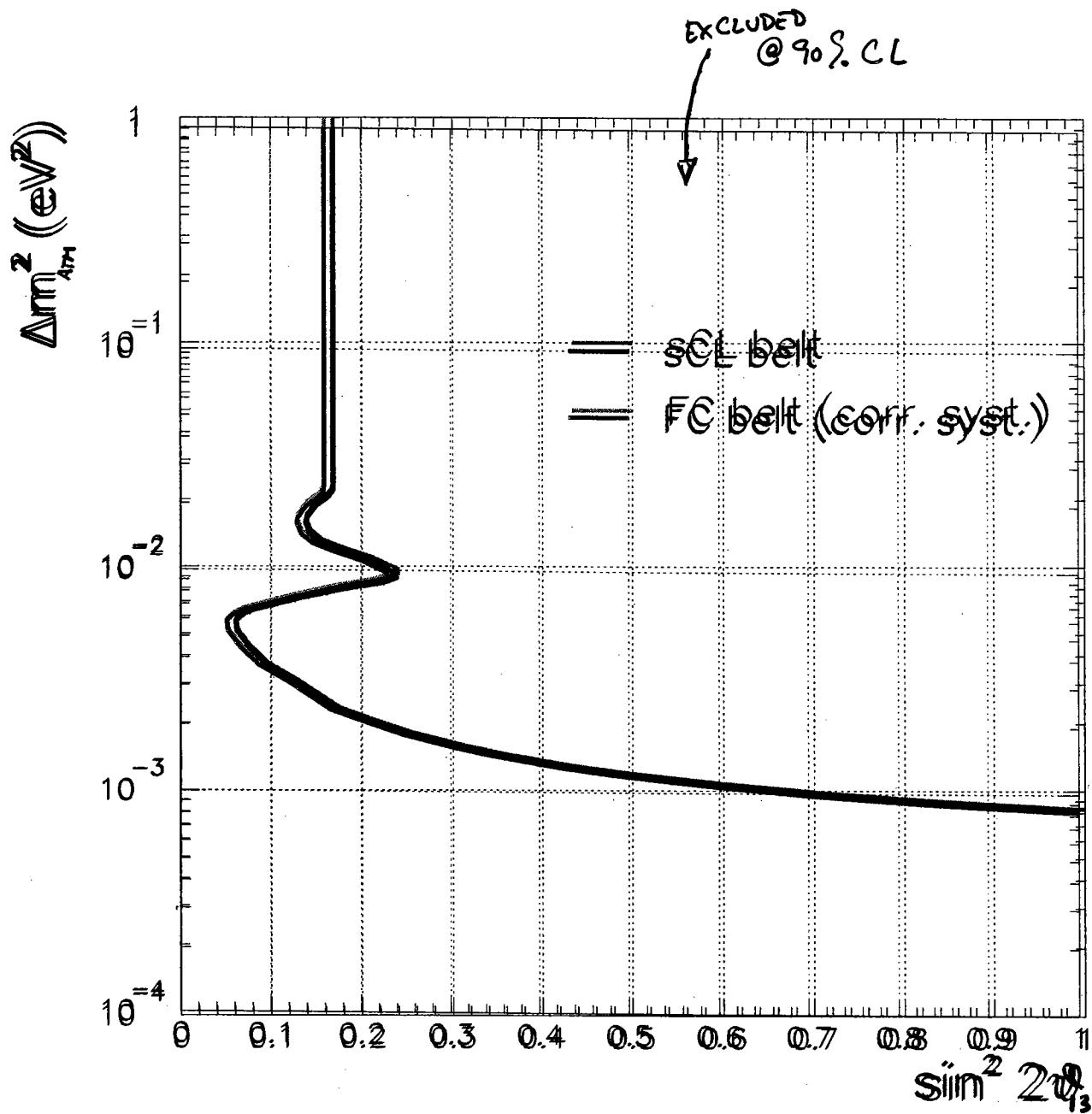
$$\operatorname{sin} 2\theta_{13} \cos \theta_{13} \times$$

$$\frac{\operatorname{sin} \delta}{\operatorname{sin} \delta} = ?$$

* BECAUSE $|U_{e3}|$ SMALL, $\Delta m_{\text{ATM}}^2 \gg \Delta m_{\text{SOL}}^2$ CP-ODD "DIRAC" PHASE

FINAL CHOOZ RESULT

HEP-EX/0301017



ATM + SOLAR DATA TELL YOU

THAT $|U_{e3}|$ IS SMALL (NOT CLOSE TO 1)

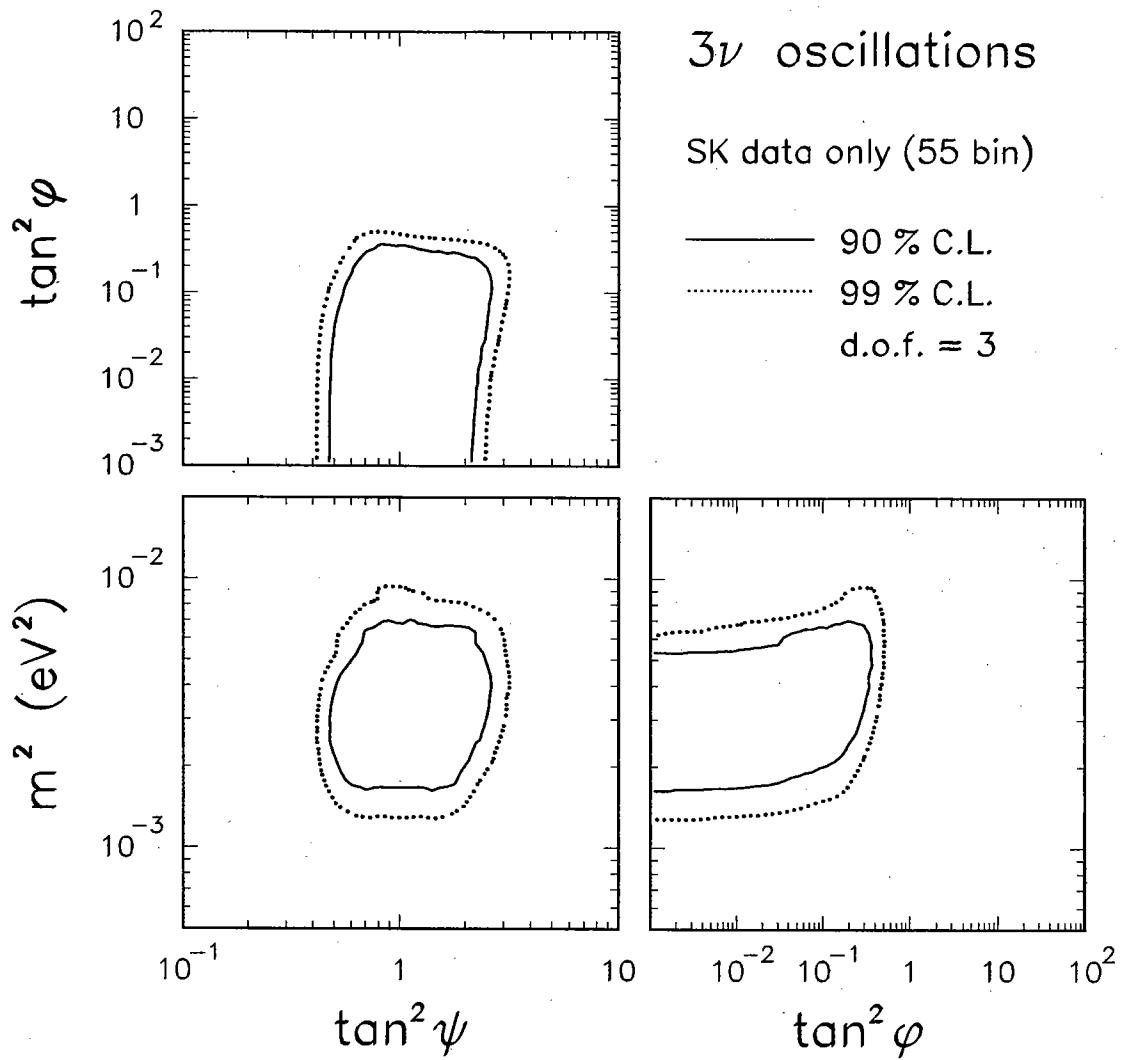


Fig. 3. Projections of the regions allowed in the 3ν parameter space ($m^2, \tan^2 \psi, \tan^2 \phi$) at 90% and 99% C.L. ($\Delta\chi^2 = 6.25$ and 11.36 for $N_{\text{DF}} = 3$) onto the coordinate planes. The fit includes SK data only (79.5 kTy). The pure 2ν case of $\nu_\mu \leftrightarrow \nu_\tau$ oscillations is recovered for $\tan^2 \phi \rightarrow 0$. Nonzero values of ϕ parametrize ν_e mixing.

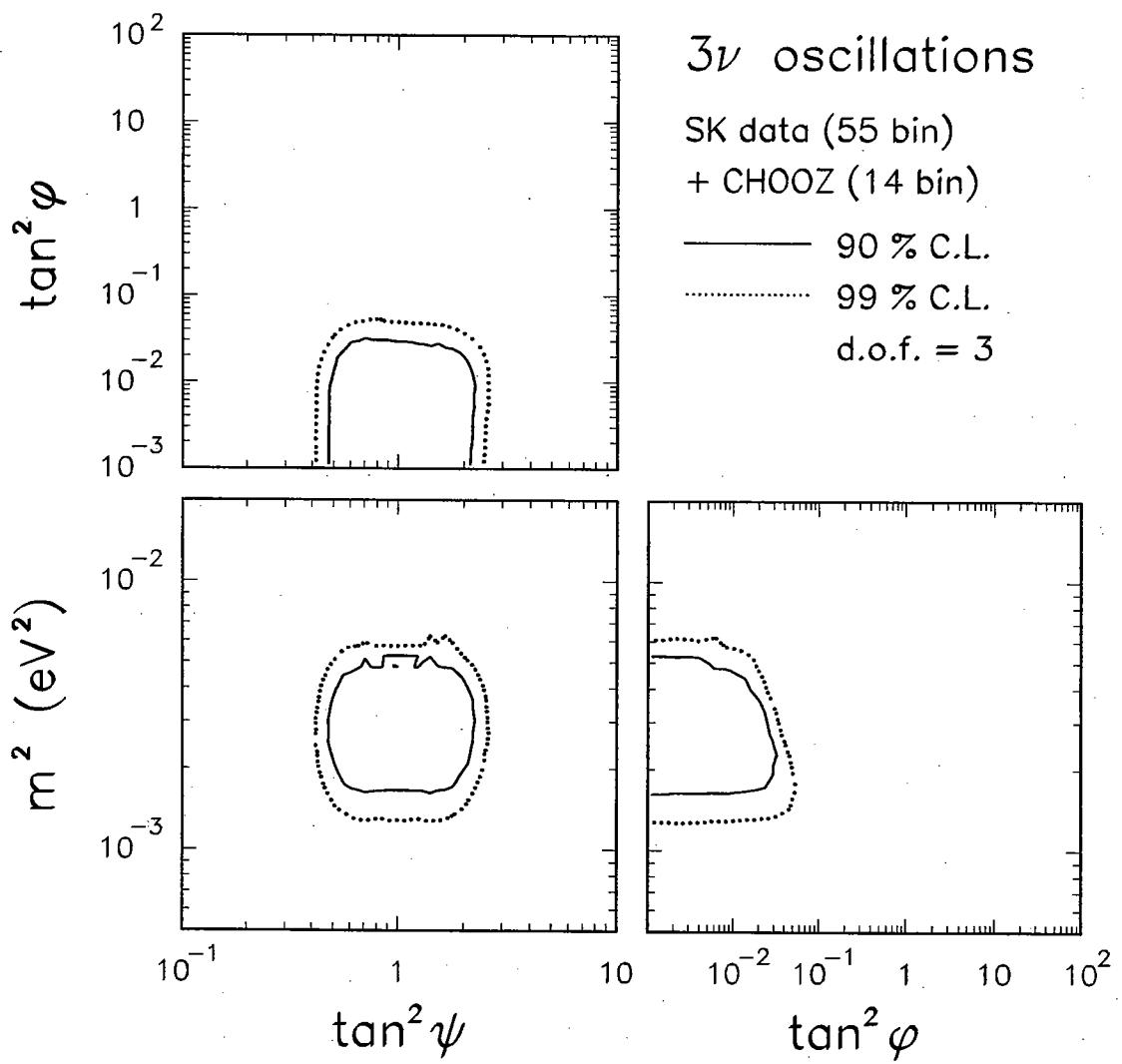


Fig. 4. As in Fig. 3, but including final CHOOZ positron spectra [5] (14 data points minus one adjustable normalization factor).

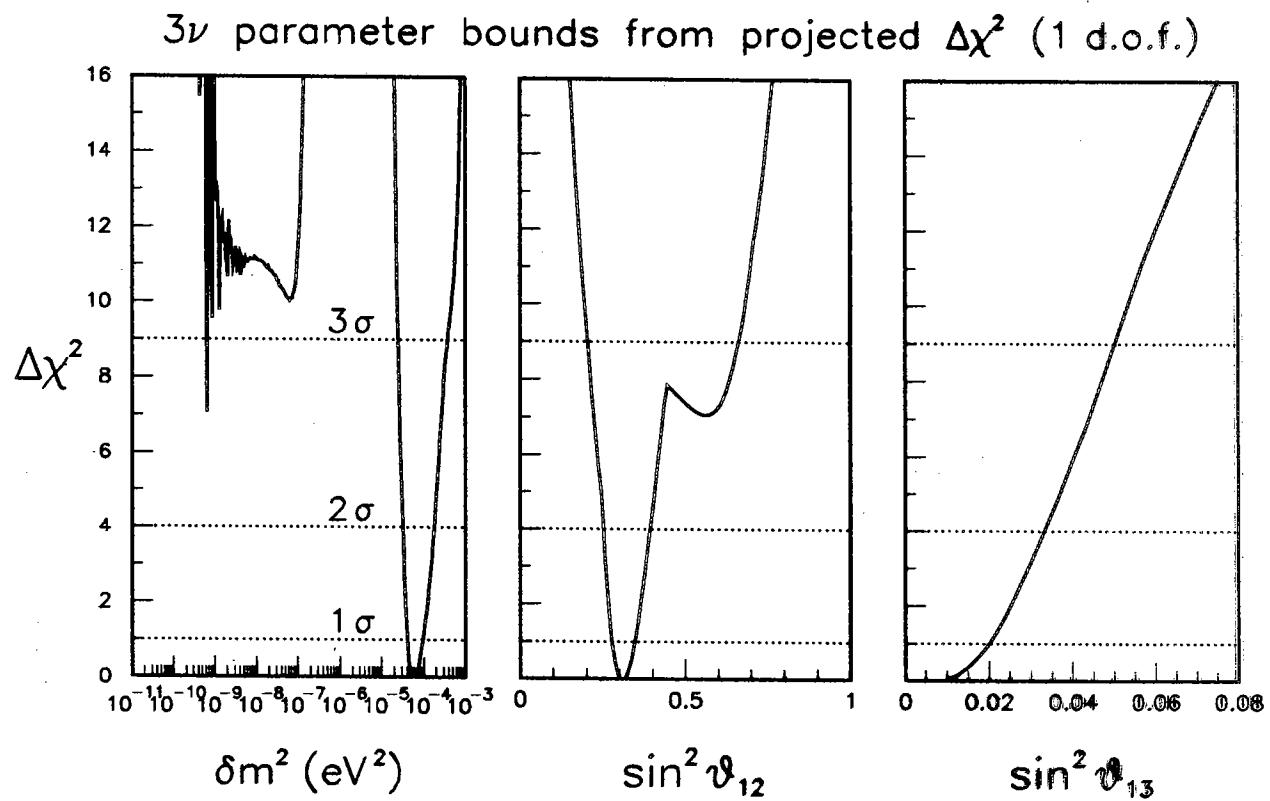
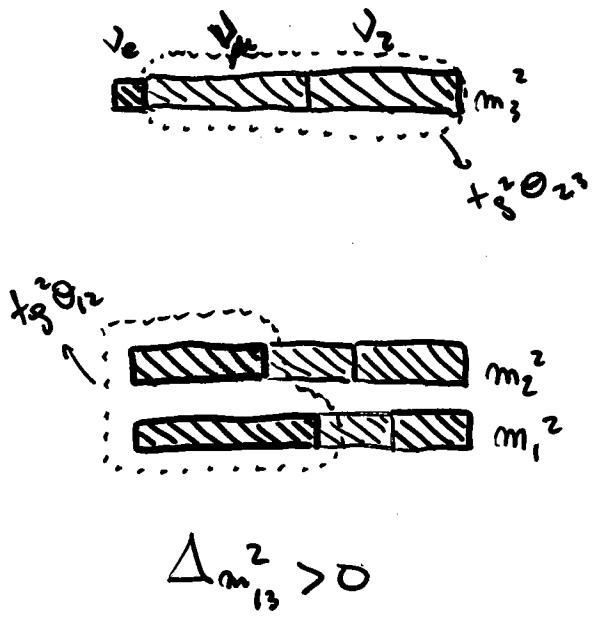
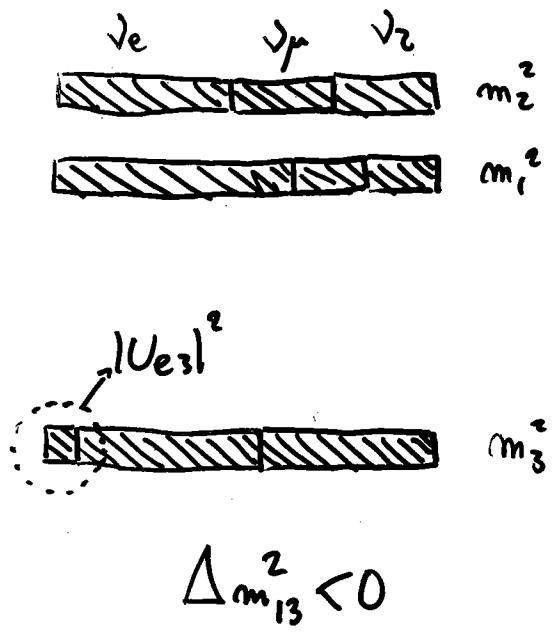


FIG. 4: Projections of the global (solar+terrestrial) $\Delta\chi^2$ function onto each of the $(\delta m^2, \sin^2 \theta_{12}, \sin^2 \theta_{13})$ parameters. The n -sigma bounds on each parameter (the others being unconstrained) correspond to $\Delta\chi^2 = n^2$.

WHAT IS LEFT?



OR



$$\Delta m_{13}^2 > 0$$

$$\Delta m_{13}^2 < 0$$

1 - $|U_{e3}|^2$

2 - WHAT IS THE MASS HIERARCHY?

3 - WHAT IS THE CP-ODD PHASE?

[2] CAN BE ADDRESSED WITHIN OSCILLATIONS IF $|U_{e3}|^2$ IS BIG

[3] CAN BE ADDRESSED WITHIN OSCILLATIONS IF LMA + $|U_{e3}|^2$ IS BIG

LOOKING FOR $|U_{e3}|^2$ EFFECTS (EXPERIMENTALLY)

$\nu_\mu \leftrightarrow \nu_e$ TRANSITIONS "DOMINATED BY $\Delta_{m_{13}}^2$ - TERM"

$$\begin{aligned}
 P_{\bar{\mu}e}^{\text{VAC}} = & 4 |U_{\mu 3}|^2 |U_{e3}|^2 \sin^2 \Delta_{13} - \xrightarrow{\substack{\text{MAXIMIZE BY} \\ \text{CHOOSING } L, E}} \text{"}(\Delta_{12})^2\text{ TERM"} \\
 & 4 \operatorname{Re} [U_{\mu 1} U_{e1}^* U_{\mu 2}^* U_{e2}] \sin^2 \Delta_{12} + \xrightarrow{\substack{\text{"}U_{e3} \Delta_{12}\text{ TERM"}}} \\
 & 2 \operatorname{Re} [U_{\mu 2} U_{e2}^* U_{\mu 3}^* U_{e3}] (\cos 2(\Delta_{12} - \Delta_{13}) - \cos 2\Delta_{13}) - \\
 & \pm 8 \operatorname{Im} [U_{\mu 2} U_{e2}^* U_{\mu 3}^* U_{e3}] \sin \Delta_{12} \sin \Delta_{13} \sin (\Delta_{13} - \Delta_{12}) \\
 & \quad \downarrow \\
 & \text{"}U_{e3} \Delta_{12} \text{ CP-ODD TERM"}
 \end{aligned}$$

$$\boxed{\Delta_{ij} = \Delta_{m_{ij}}^2 \frac{L}{4E}}$$

TO BE STUDIED EITHER WITH INTENSE

ν_μ OR ν_e BEAM \rightarrow NEUTRINO FACTORY

A FEW WORDS ON NEXT GENERATION ν_μ -BEAMS

[SUPERBEAMS OFF-AXIS EXPERIMENTS, ETC..]

(SEE TALKS BY PARKE, LINDNER LATER THIS WEEK...)

- THESE SEEM TO BE THE "BEST BET" FOR NEXT GENERATION NEUTRINO OSCILLATION EXPT (EXCEPT SEE NEXT TOPIC) [NUMI OFFAXIS, JHF-SUPERK]
 - IT IS "EASY" TO PRODUCE INTENSE ν_μ BEAMS ($\pi \rightarrow \mu \nu_\mu$) OF APPROPRIATE ENERGIES
 - NARVELY, APPEARANCE IS THE "RIGHT WAY" TO REACH (VERY) SMALL ANGLES (VERSUS DISAPPEARANCE)
 - SUCH A SETUP WILL ALSO PROVIDE THE (REQUIRED) PRECISE KNOWLEDGE OF ATMOSPHERIC PARAMETERS
 - ONE CAN LOOK FOR CP-PHASE + SIGN($\Delta m_{1,3}^2$)

MATTER EFFECTS MATTER! (DEPENDING ON BASELINE)

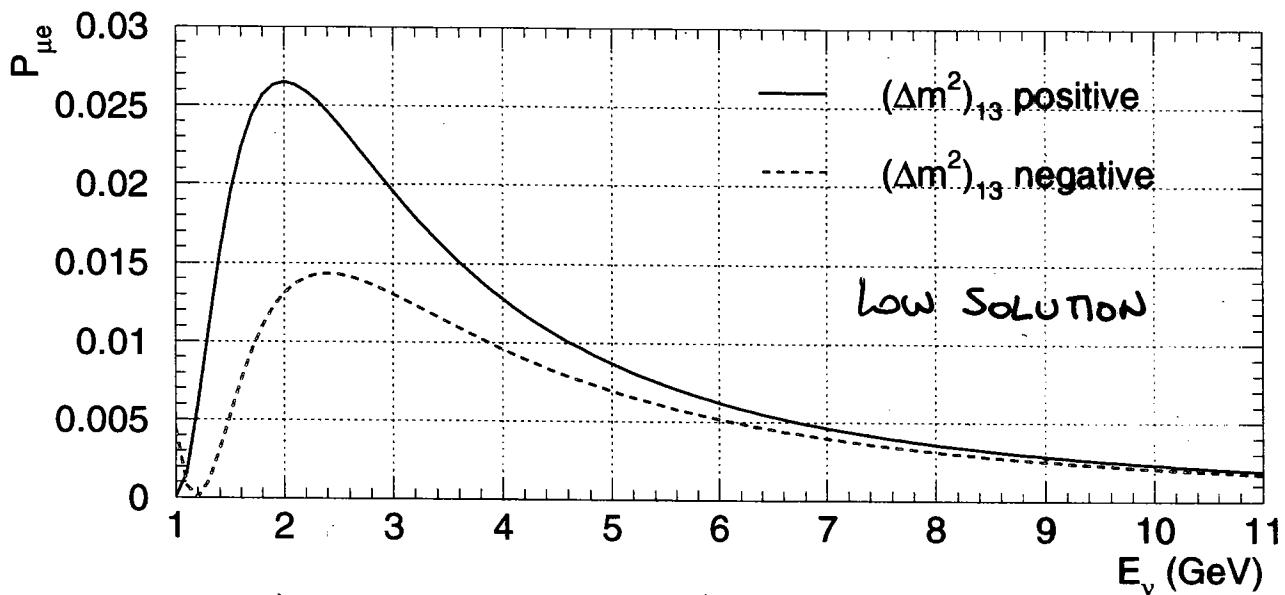


Figure 1: $\nu_\mu \rightarrow \nu_e$ oscillation probability for $\Delta m_{13}^2 > 0$ (solid line) and $\Delta m_{13}^2 < 0$ (dashed line). $|\Delta m_{13}^2| = 3 \cdot 10^{-3} \text{ eV}^2$, $\theta_{\text{atm}} = \pi/4$, $\Delta m_\odot^2 = 1 \times 10^{-7} \text{ eV}^2$, $\theta_\odot = \pi/6$, $|U_{e3}|^2 = 0.01$, and $\delta = 0$. $L = 900 \text{ km}$

[BARENBOIM, ADG, SZLEPER,

VELASCO, HEP-PH/0204208]

$$\frac{\Delta m^2}{2E} \times \sqrt{2} G_F N_e \approx 1.4 \times 10^{-4} \frac{\text{eV}^2}{\text{GeV}}$$

AS LONG AS $E \lesssim 10 \text{ GeV}$, MATTER EFFECTS ARE AN
IMPORTANT PERTURBATION. NOTE THAT FOR $E > 10 \text{ GeV}$,
WE NEED DISTANCES BIGGER THAN $\gtrsim 5000 \text{ km}$ TO
AFFECT $\Delta_{13} \sim \pi/2 \dots$

How ABOUT A "SUPER BUGGY" EXPERIMENT?

[SEE TALK BY LINDNER]

$$P_{\bar{e}\bar{e}} = 1 - 4 |U_{e3}|^2 (1 - |U_{e3}|^2) \sin^2 \Delta_{13} \\ - 4 |U_{e1}|^2 |U_{e2}|^2 \sin^2 \Delta_{12} \xrightarrow{\text{"SOLAR TERM"}} \\ + 2 |U_{e2}|^2 |U_{e3}|^2 [\cos 2(\Delta_{13} - \Delta_{12}) - \cos 2\Delta_{13}] \\ \xrightarrow{\text{"INTERFERENCE TERM" (SMALL)}}$$

- MATTER EFFECTS ARE IRRELEVANT

- THERE ARE LOTS OF NUCLEAR REACTORS AROUND
(PLUS, THEIR NEUTRINOS ARE FREE...)

- NO $\delta\phi$ OR SIGN OF Δ_{13}^2 SENSITIVITY...

\Rightarrow MUST HAVE INCREDIBLY SMALL SYSTEMATIC
UNCERTAINTIES TO BE "COMPETITIVE" !

SUBJECT OF (INTENSE?) RESEARCH RIGHT NOW...

INTERLUDE : WHY DO WE CARE ABOUT $|U_{e3}|$ ET AL ?

- NEUTRINO MIXING PARAMETERS ARE FUNDAMENTAL CONSTANTS OF THE (NOW EXTENDED) S.M., JUST LIKE THE CABIBBO ANGLE, THE FINE STRUCTURE CONSTANT OR THE TOP MASS.
- WITH FUTURE OSCILLATION EXPERIMENTS, WE HAVE THE OPPORTUNITY OF PROBING WHETHER CP-INVARIANCE HOLDS IN THE LEPTONIC SECTOR. DOES A "CKM-LIKE" PICTURE DESCRIBES CP IN LEPTONS AS WELL ?
- "PRECISE" MEASUREMENTS OF THE NEUTRINO MIXING PARAMETERS WILL SHED LIGHT [HOPEFULLY...] INTO OUR UNDERSTANDING OF FLAVOR [+ MORE...]

THEORETICAL CHALLENGES

- "NEUTRINO FLAVOR CONVERSION" IS THE ONLY EVIDENCE WE HAVE FOR PHYSICS BEYOND THE STANDARD MODEL.
- EVEN THE SIMPLEST (MOST LIKELY FROM EXPERIMENTS) SOLUTION REQUIRES A QUADRATIC MODIFICATION OF WHAT WE MEAN BY "S.M."
- FURTHERMORE, LEPTONIC MIXING SEEMS TO BE "DIFFERENT". BY THAT WE MEAN:

$$V_{CKM} \sim \begin{pmatrix} 1 & \lambda & \lambda^3 \\ \lambda & 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix} \quad \times$$

$$\lambda \approx 0.2$$

$$V_{MNS} \sim \begin{pmatrix} 1 & 1 & \delta \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}$$

$$\delta \lesssim 0.2$$

WHILE SOME MIGHT CLAIM THAT THEORIST
"PREDICTED" VERY SMALL NEUTRINO MASS, NOONE
CAN CLAIM THAT WE ANTICIPATED IN ANY
WAY THE LARGE NEUTRINO MIXING ANGLES...

ONE REASON FOR THIS IS THAT WE BELIEVE
(VIA GUTS OF ALL KINDS) THAT QUARKS AND
LEPTONS ARE CONNECTED AT SOME VERY
HIGH SCALE : (NAIYER $V_{CKM} \sim V_{MNS}$ AT M_{Pl})

[OF COURSE, WE LEARNED (SEE TALKS BY ABRIGAD
MOHAPATRA, FOR EXAMPLE) THAT GUTS CAN BE MADE
TO PROPERLY FIT V_{CKM} AND V_{MNS} ...]

THE FACT THAT WE DON'T KNOW THE "PHYSICS"
BEHIND MASSES + MIXING DOES NOT STOP US
FROM TRYING - QUITE THE CONTRARY.

WE DRAW "INSPIRATION" FROM THE QUARK

SECTOR. THERE, THE PECULIAR VALUES OF

MASSES + MIXING ANGLES HAVE LED
PEOPLE TO BELIEVE THAT NATURE IS TRYING
TO TELL US SOMETHING...

WHAT WE AIM AT IS THE PRESENCE OF
SOME NEW FUNDAMENTAL PRINCIPLE (SYMMETRY)

THAT DYNAMICALLY EXPLAINS WHY MASSES +
MIXING ANGLES COME OUT AS THEY DO...

FLAVOR SYMMETRIES

STARTING POINT: WHAT DO THE MASS MATRICES "ROUGHLY" LOOK LIKE?

10

(EXPLAINING ALL DATA WITH "SMALLEST" AMOUNT OF INPUT)

Table 1

Leading order low energy neutrino Majorana mass matrices m_{LL} consistent with large atmospheric and solar mixing angles, classified according to the rate of neutrinoless double beta decay and the pattern of neutrino masses.

	Type I Small $\beta\beta_{0\nu}$	Type II Large $\beta\beta_{0\nu}$
A Normal hierarchy $m_1^2, m_2^2 \ll m_3^2$	$\beta\beta_{0\nu} \lesssim 0.0082 \text{ eV}$ $\begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 1 & 1 \end{pmatrix} \frac{m}{2}$	-
B Inverted hierarchy $m_1^2 \approx m_2^2 \gg m_3^2$	$\beta\beta_{0\nu} \lesssim 0.0082 \text{ eV}$ $\begin{pmatrix} 0 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix} \frac{m}{\sqrt{2}}$	$\beta\beta_{0\nu} \gtrsim 0.0085 \text{ eV}$ $\begin{pmatrix} 1 & 0 & 0 \\ 0 & \frac{1}{2} & \frac{1}{2} \\ 0 & \frac{1}{2} & \frac{1}{2} \end{pmatrix} m$
C Approximate degeneracy $m_1^2 \approx m_2^2 \approx m_3^2$	$\begin{pmatrix} 0 & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{\sqrt{2}} & \frac{1}{2} & \frac{1}{2} \end{pmatrix} m$	$\beta\beta_{0\nu} \gtrsim 0.035 \text{ eV}$ $\text{diag}(1,1,1)m$ $\begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} m$

Table 2
Some candidate GUT and Family symmetry groups.

G_{GUT}	G_{Family}
E_6	$SU(3)$
$SO(10)$	$SU(2)$
$SU(5)$	$U(1)$
$SU(5) \times U(1)$	Z_N
$SU(3)^3$	$O(3) \times O(3)$
$SU(4) \times SU(2) \times SU(2)$	$SO(3)$
$SU(3) \times SU(2) \times SU(2) \times U(1)$	$S(3) \times S(3)$
$SU(3) \times SU(2) \times U(1) \times U(1)$	$S(3)$
$SU(3) \times SU(2) \times U(1)$	Nothing

"Good" Frank notes
SOLVE MANY PROBLEMS
AT ONCE + LEAD
TO NEW EXPERIMENTAL
CONSEQUENCES!

Table 2: Order-of-magnitude estimates for θ_{13} .

Texture	θ_{12}	θ_{13}	Perturbations
$m_\nu^{\text{D1}} = m \begin{pmatrix} \delta & -\frac{1}{\sqrt{2}} & \frac{(1-\epsilon)}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} & \frac{(1+\eta)}{2} & \frac{(1+\eta-\epsilon)}{2} \\ \frac{(1-\epsilon)}{\sqrt{2}} & \frac{(1+\eta-\epsilon)}{2} & \frac{(1+\eta-2\epsilon)}{2} \end{pmatrix}$	$\approx \pi/4$	$\approx \left(\frac{\Delta m_{\text{sun}}^2}{\Delta m_{\text{atm}}^2}\right)^{1/2}$	$\epsilon \gg \delta$
		≈ 0	$\epsilon \ll \delta$
$m_\nu^{\text{D2}} = m \left[\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} + r \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} \right] + \delta m_\nu$	$\approx \pi/4$	$\approx \left(\frac{m_e}{m_\mu}\right)^{1/2}$	
$m_\nu^{\text{I}} = m \begin{pmatrix} \delta & -1 & 1 \\ -1 & \eta & \eta \\ 1 & \eta & \eta \end{pmatrix}$	$\approx \pi/4$	$\approx \frac{\Delta m_{\text{sun}}^2}{\Delta m_{\text{atm}}^2}$	$\eta \gg \delta$
		$\ll \frac{\Delta m_{\text{sun}}^2}{\Delta m_{\text{atm}}^2}$	$\eta \ll \delta$
$m_\nu^{\text{N}} = m \begin{pmatrix} \delta & \epsilon & \epsilon \\ \epsilon & 1+\eta & 1+\eta \\ \epsilon & 1+\eta & 1+\eta \end{pmatrix}$	$O(1)$	$\approx \left(\frac{\Delta m_{\text{sun}}^2}{\Delta m_{\text{atm}}^2}\right)^{1/2}$	$\eta < \delta \approx \epsilon$
	$\approx \pi/4$	$\approx \left(\frac{\Delta m_{\text{sun}}^2}{\Delta m_{\text{atm}}^2}\right)^{1/3}$	$\delta \approx \epsilon^2 \approx \eta^2$
			$\delta \approx \epsilon^2 \quad \eta = 0$

a) Degenerate case. If $|m|$ is the common mass, apart from a phase, and taking $\theta_{13} = 0$, which, as already observed, is a safe approximation in this case, we have $m_{ee} = m(c_{12}^2 \pm s_{12})$. Here the phase ambiguity has been reduced to a sign ambiguity.

OF COURSE, WE SAY THAT NEUTRINO
MIXING IS STRANGE BECAUSE WE
HAVE GROWN ACCUSTOMED TO
QUARK MIXING.

PERHAPS WE SHOULD BACKUP AND
RE-EXAMINE THIS:

AFTER ALL QUARK MIXING IS

STRANGE, WHILE NEUTRINO MIXING

MIGHT BE QUITE "COMMON".

CAN ONE QUANTIFY THIS STATEMENT?

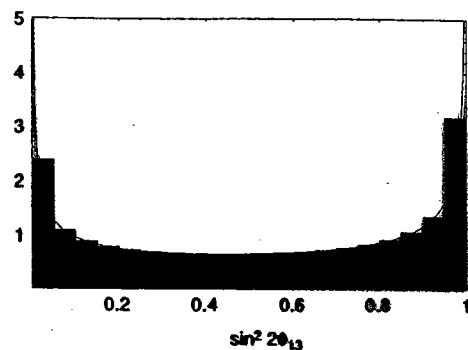
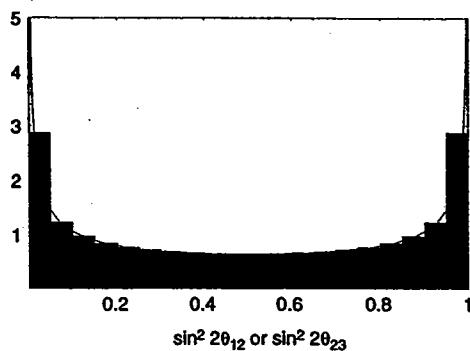
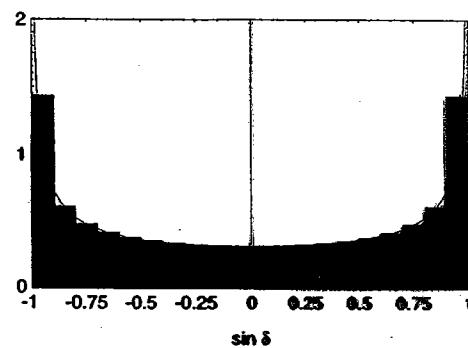
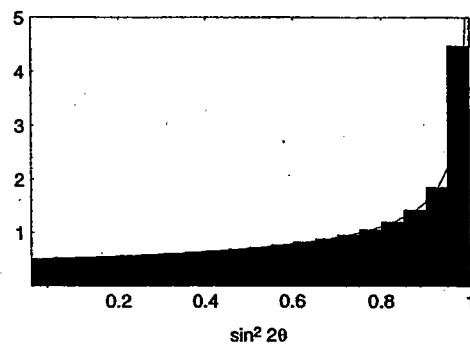


Figure 1: Distributions in (a) $\sin^2 2\theta_{12}$ or $\sin^2 2\theta_{23}$ and (b) $\sin^2 2\theta_{13}$ for the case of real mass matrices.



$O(3)$

$U(3)$

Figure 2: Distributions in (a) $\sin^2 2\theta_{12}$ or $\sin^2 2\theta_{13}$ or $\sin^2 2\theta_{23}$ and (b) $\sin \delta$ for the case of complex mass matrices.

NEUTRINO FLAVOR WITHOUT FLAVOR?

→ SIMPLEST BOTTOM-UP APPROACH! ←

IS THE MNS MATRIX "TYPICAL" OF WHAT

YOU WOULD EXPECT IF THERE WAS NO

FUNDAMENTAL DISTINCTION AMONG THE 3

NEUTRINOS, i.e., IS THE MNS MATRIX

"AN OLD" 3×3 UNITARY MATRIX?

TABLE I: $\sin^2 \theta_{ij}$ in the MNS and CKM mixing matrices, according to the PDG parametrization [1]. In square brackets we quote the currently allowed experimental values for the CKM (MNS) entries at the 90% (three sigma) confidence level.

"angle"	CKM [90% expt.]	MNS [3σ expt.]
$\sin^2 \theta_{13}$	$ V_{ub} ^2 [(6.2 - 23) \times 10^{-6}]$	$ U_{e3} ^2 [0 - 0.05]$
$\sin^2 \theta_{12}$	$\sin^2 \theta_C [0.048 - 0.051]$	$\sin^2 \theta_{\text{sol}} [0.2 - 0.5]$
$\sin^2 \theta_{23}$	$ V_{cb} ^2 [(1.4 - 1.9) \times 10^{-3}]$	$\sin^2 \theta_{\text{atm}} [0.35 - 0.65]$

"ANARCHY" * IN THE MIXING MATRIX MIGHT BE
EXPRESSED AS THE FOLLOWING "MODEL":

WE PREDICT THAT THE MIXING MATRIX
IS A "RANDOM VARIABLE" DRAWN FROM A
FLAT DISTRIBUTION OF UNITARY 3×3
MATRIX.

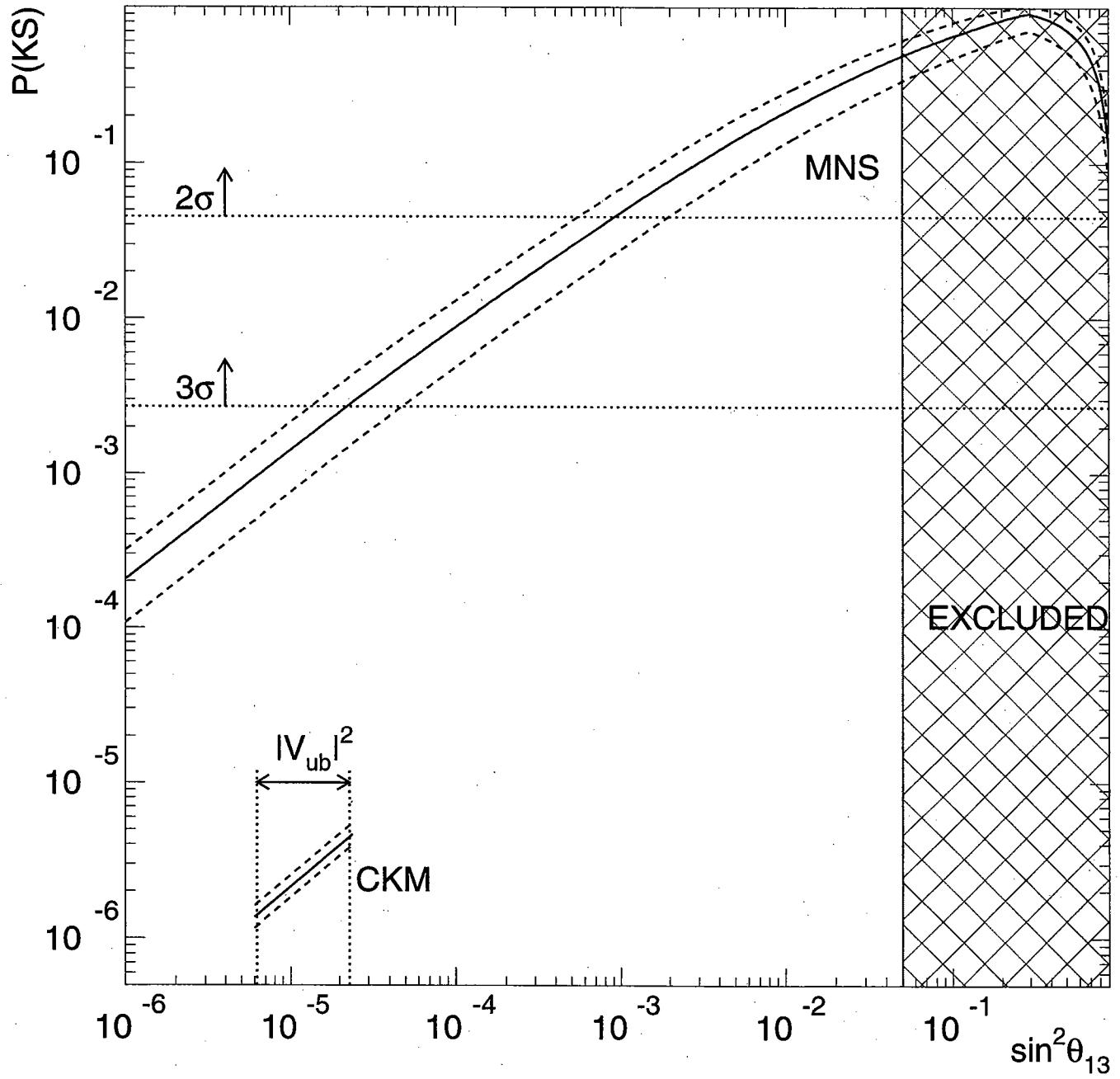
GIVEN NATURE'S "DRAW", HOW LIKELY
IS IT THAT THIS HYPOTHESIS IS CORRECT?

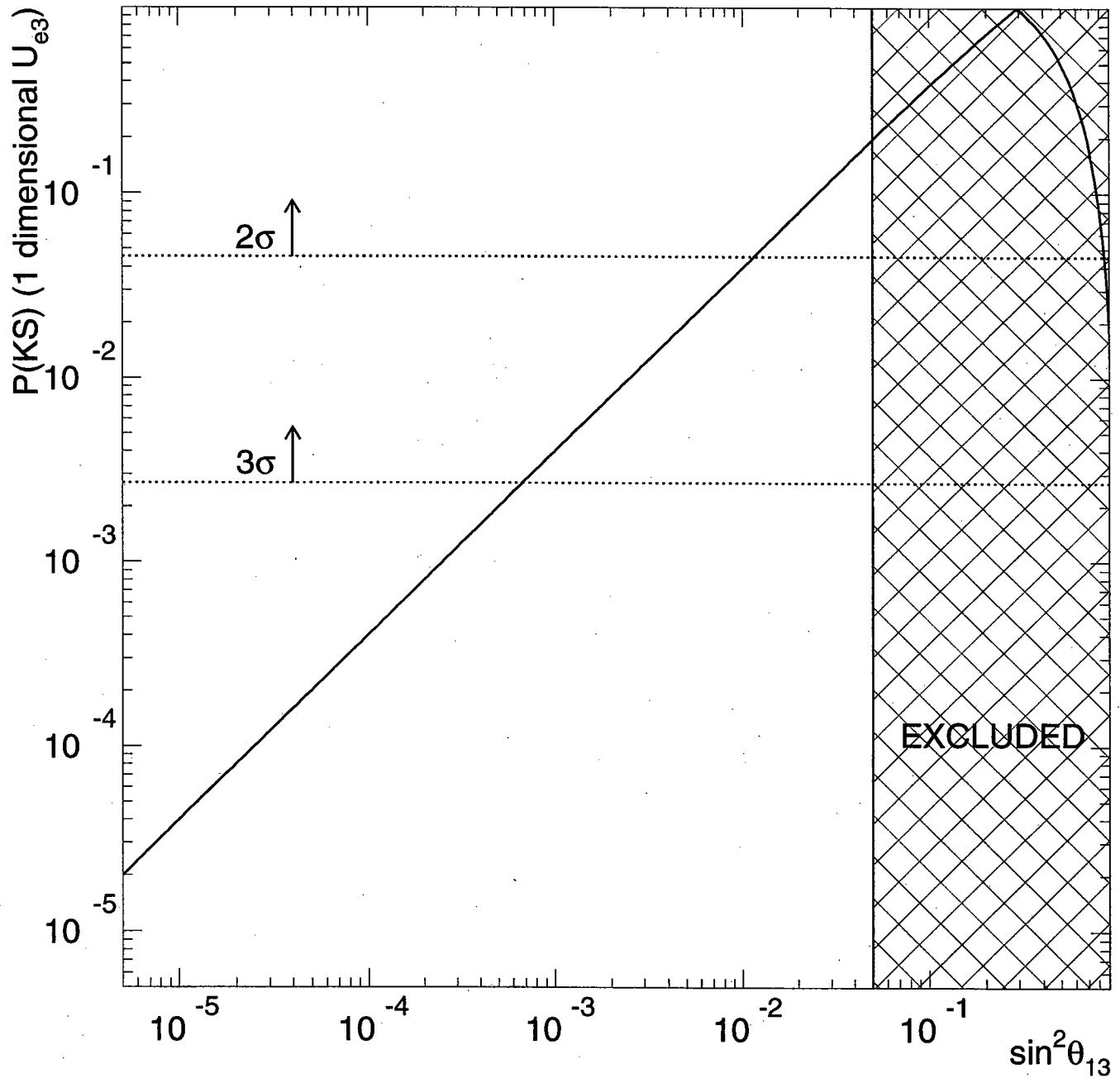
SEE AdG, NURAYANA

HEP-PH/0301050

* Hall, Nurayana, Werner

PRL 84, 2572 (2000)





COMMENTS ON ANARCHY:

- THE FACT THAT THIS MODEL WORKS DOES NOT MEAN THAT FAIR MODELS DO NOT WORK OR ARE DISFAVORED. THEY DO, HOWEVER, HAVE THE "BURDEN OF PROOF".
- WE NEED NOT (INDEED, DO NOT) SAY ANYTHING ABOUT MASS EIGENVALUES...
- IS THERE SOME "DEEP SIGNIFICANCE" BEHIND NEUTRINO MASS ANARCHY?
 - MAYBE IT MEANS THAT THERE ARE SEVERAL "COMPETING" CONTRIBUTIONS TO THE NEUTRINO MASS-MATRIX...

SUMMARIZING

- IN THE MOST BORING EXTENSION TO THE S.M THERE ARE A FEW, NEW "FUNDAMENTAL PARAMETERS" OF OUR UNDERSTANDING OF NATURE THAT REMAIN COMPLETELY UNKNOWN
- WE NEED NEW EXPERIMENTS? FINDING $|U_{e3}|$ IS ESSENTIAL BECAUSE, IF FOR NO OTHER REASON, LEARNING THE VALUE OF $|U_{e3}|$ WILL TELL US IF WE CAN PROBE $\delta\theta + \text{sign}(A_{\mu_1}^2)$ VIA OSCILLATION EXPERIMENTS.

- THEORY DOES NOT "KNOW" THE VALUE OF $|U_{e3}|$.

THERE ARE SEVERAL DIFFERENT PREDICTIONS IN

THE MARKET

$$|U_{e3}| \underset{\text{THEORY}}{\in} [0, \text{Chooz Bound}]$$

↑
"DATA DRIVEN FIELD"!

- MAYBE EXPLAINING MIXING IN THE LEPTON SECTOR

IS VERY (TOO?) SIMPLE: WOULDN'T THAT
BE SURPRISING?