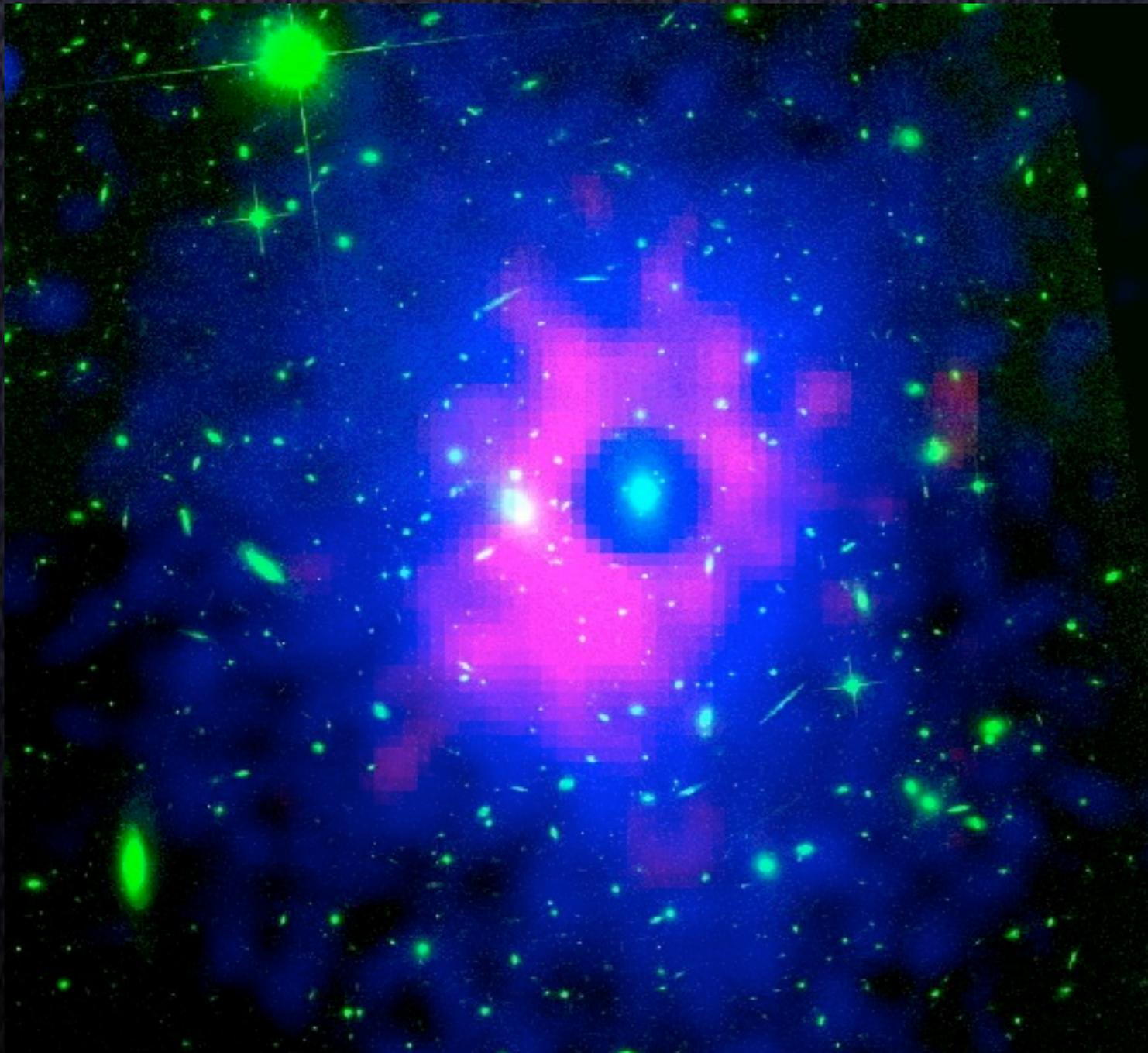


Probing Cluster Masses with Gravitational Lensing

Sanghamitra Deb
ANL

Collaborators: Prof. David M. Goldberg (Drexel University), Prof. Kristian Pedersen (DARK, Copenhagen), Dr. Andrea Morandi (DARK, Copenhagen & Univ. of Tel Aviv.), Dr. Marceau Limousin (LAM Marseille), Dr. Hakon Dahle (Univ. of Oslo), Dr. Signe Riemeer-Sørensen (DARK, Copenhagen), Dr. Catherine Heymans (University of Edinburgh, IfA Royal Observatory), Dr. Reiko Nakajima (UC Berkeley), Dr. Rachel Mandelbaum (Princeton University), Prof. Gary Bernstein (University of Pennsylvania)

Observing Clusters



galaxies: HST, optical observations

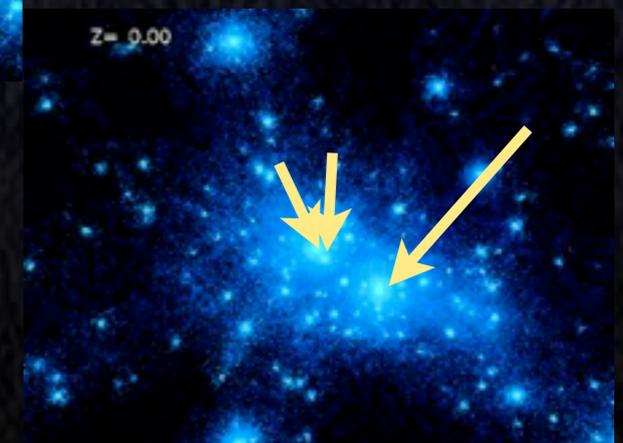
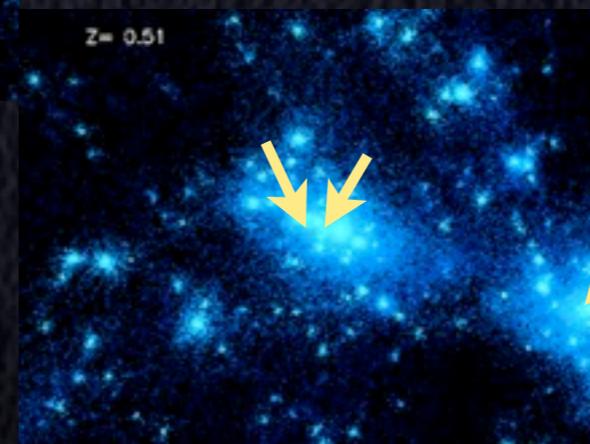
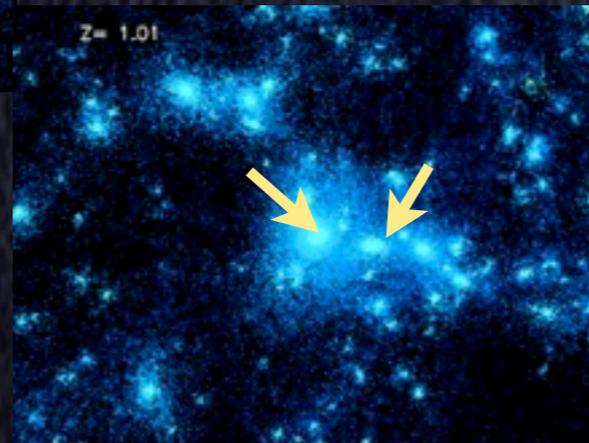
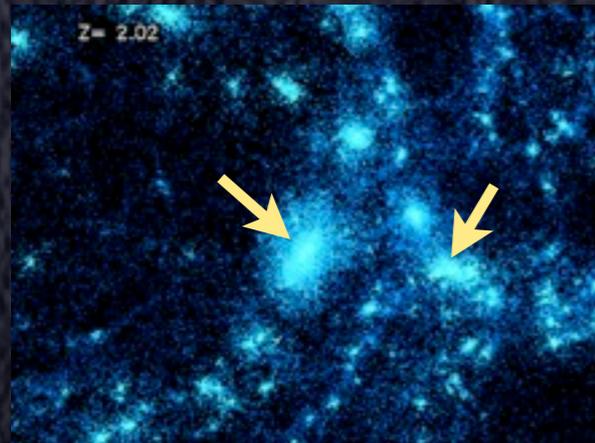
gas: Xray observations

gas: Sunyaev Zeldovich Effect

Galaxy Cluster RXJ1347-1145

<http://chile1.physics.upenn.edu/gbtpublic/>

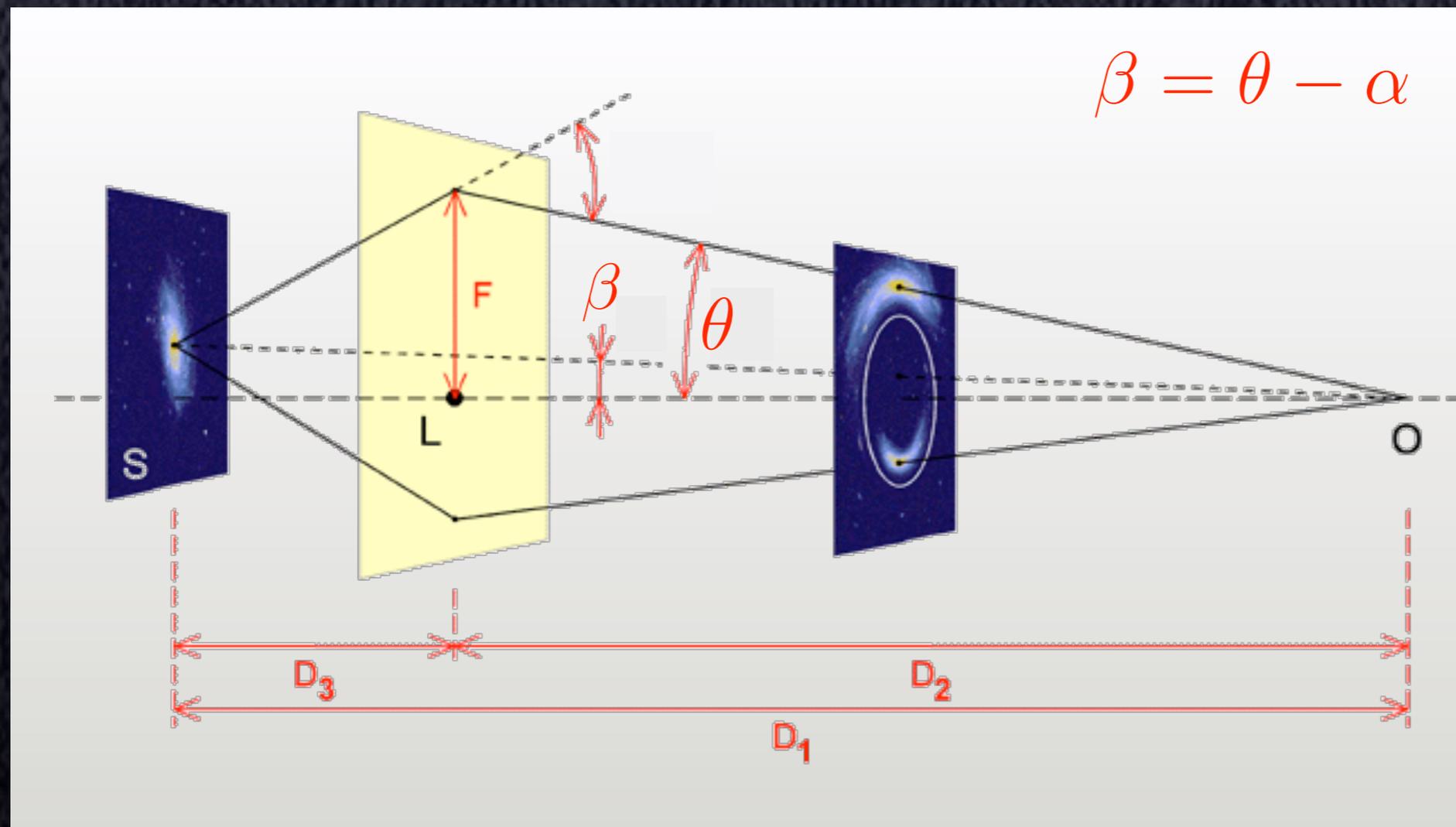
Substructure: Elliptical Halos



What is the distribution of cluster ellipticity?

How does the distribution and alignment vary with redshift & mass?

Gravitational Lensing



Dimension less
surface mass
density

$$\kappa = \frac{\Sigma}{\Sigma_{cr}}$$

Gravitational Lensing is co-ordinate transformation between the foreground (θ), and background positions(β)

Shape Distortions

$$\kappa = (\psi_{,11} + \psi_{,22})/2$$

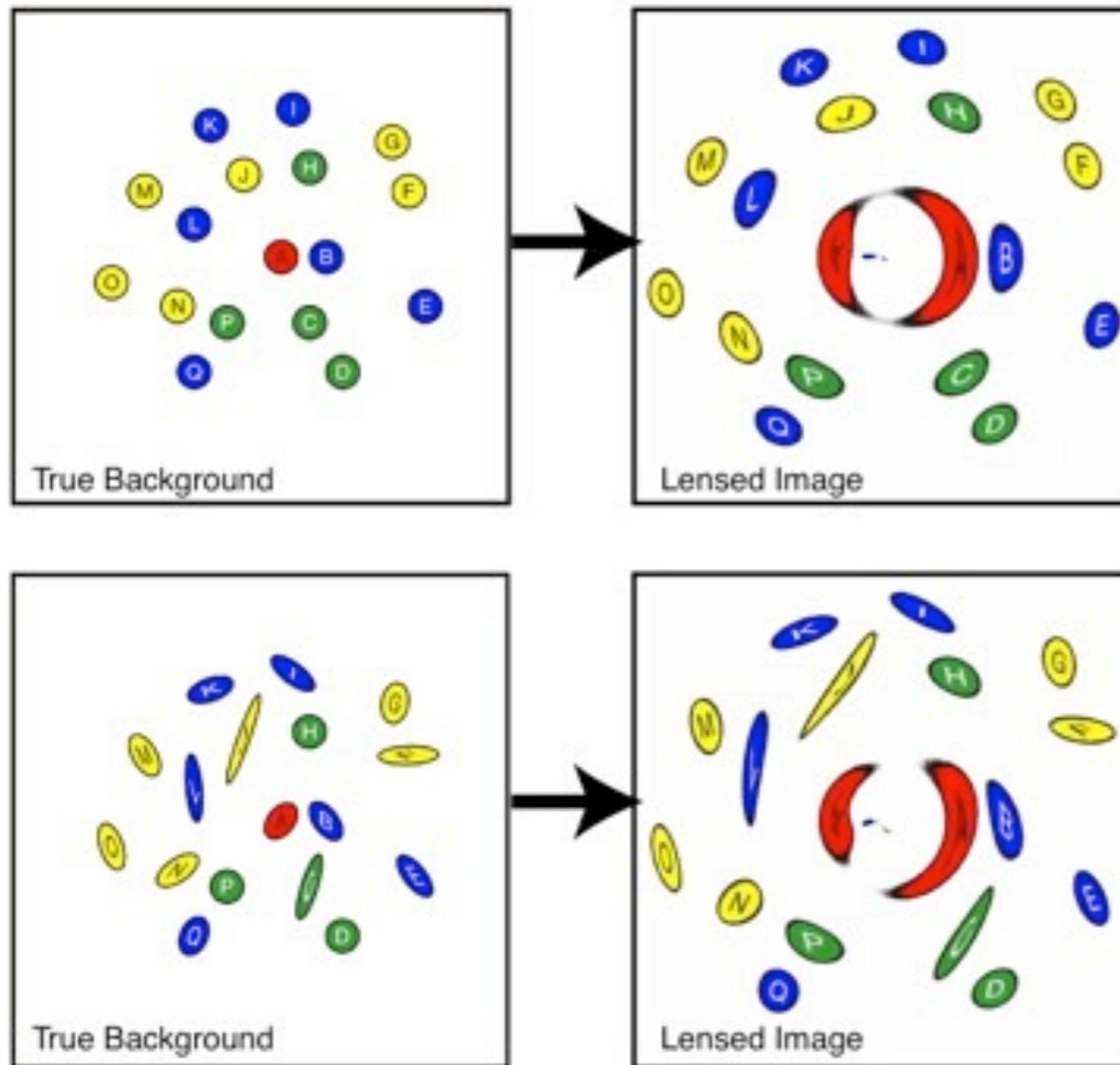
$$\gamma_1 = (\psi_{,11} - \psi_{,22})/2$$

$$\gamma_2 = \psi_{,12}$$

**Distortion Observables are
Measured Ellipticities.**

For semi-strong regime: $g = \gamma/(1 - \kappa)$

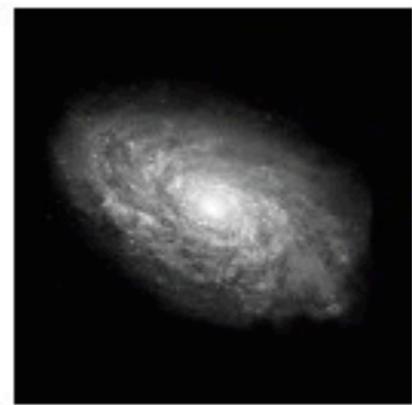
Weak Lensing



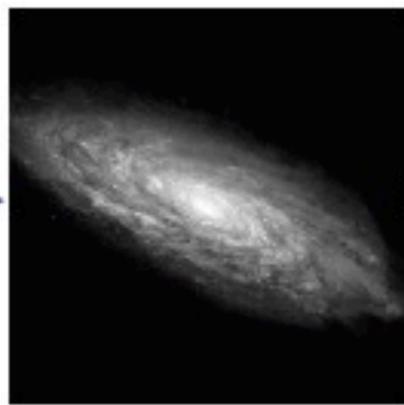
Weak lensing is a statistical measure of the distortion of background galaxies due to the intervening mass.

Williamson et al. 2007.

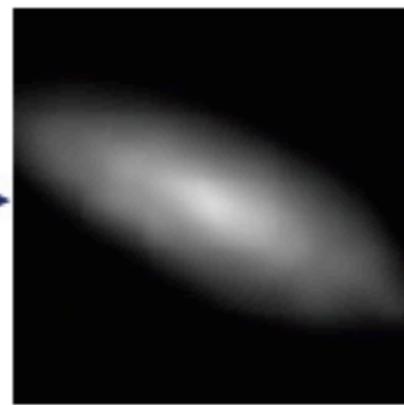
The shear signal



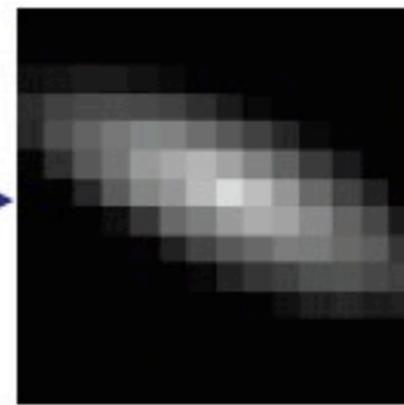
Intrinsic galaxy
(shape unknown)



Gravitational lensing
causes a **shear** (g)



Atmosphere and telescope
cause a convolution



Detectors measure
a pixelated image

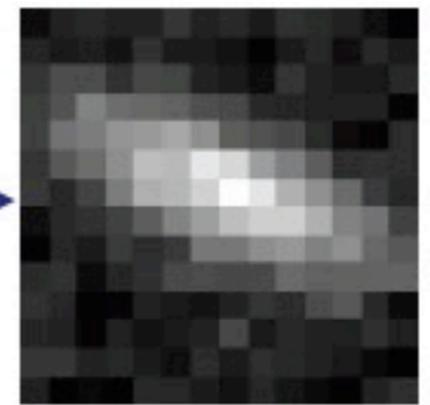
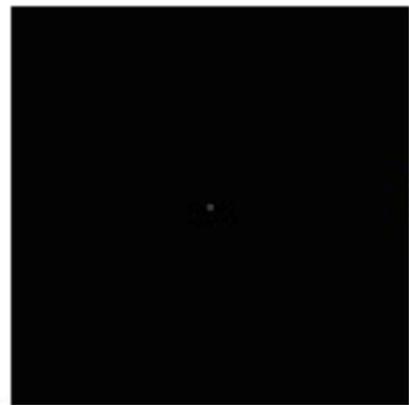


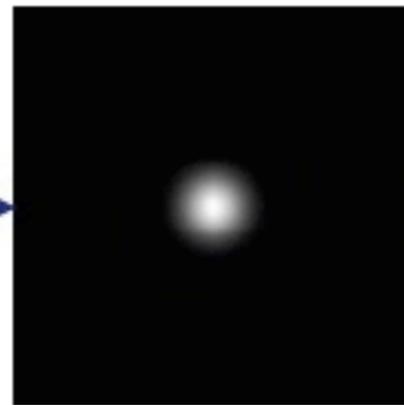
Image also
contains noise

Stars: Point sources to star images:

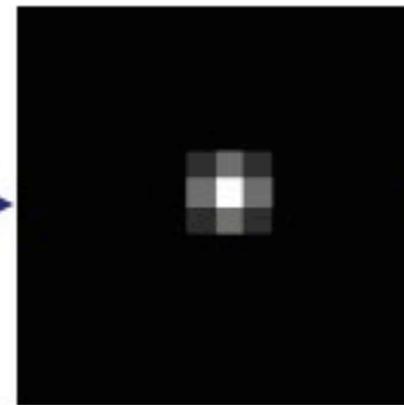
PSF



Intrinsic star
(point source)



Atmosphere and telescope
cause a convolution



Detectors measure
a pixelated image

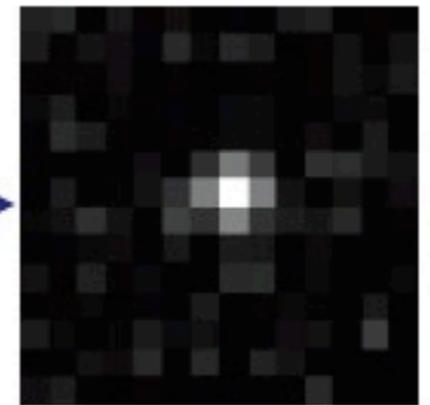
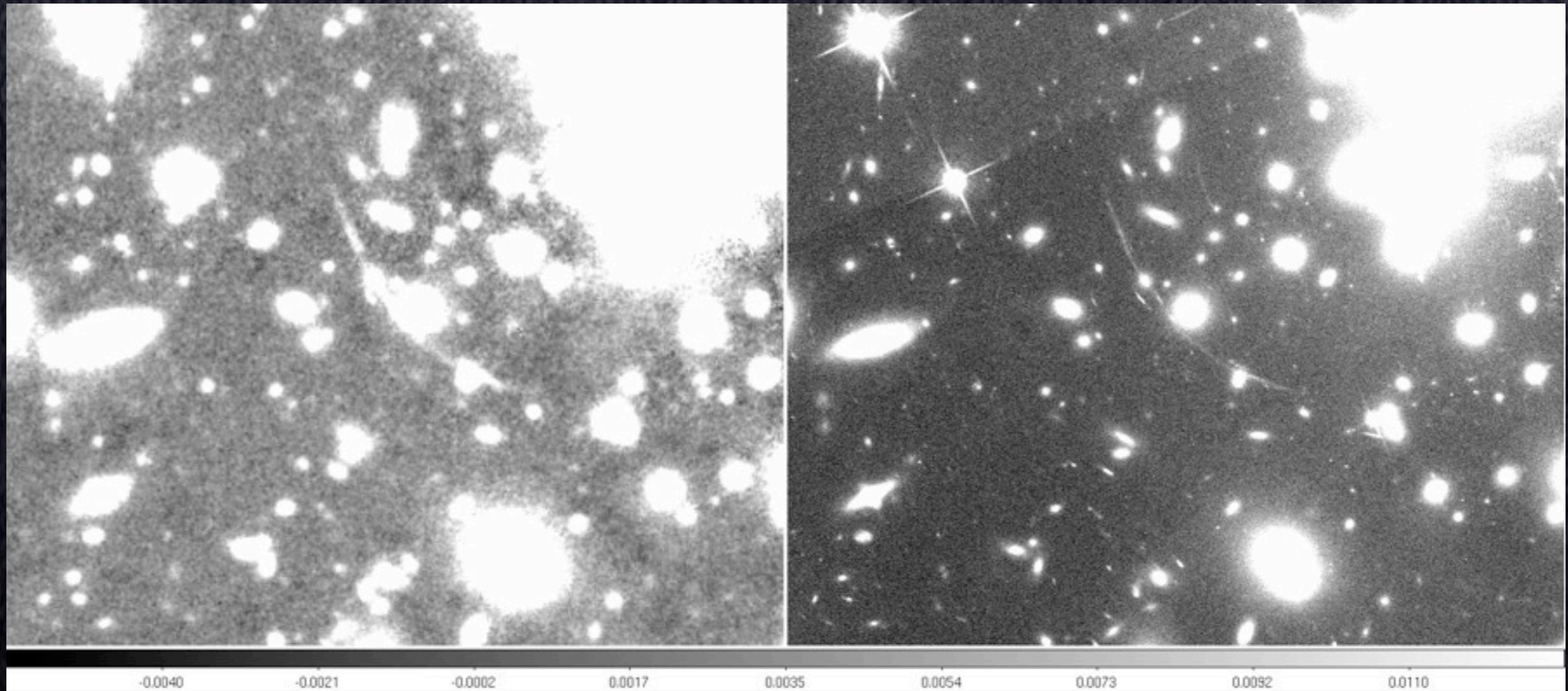
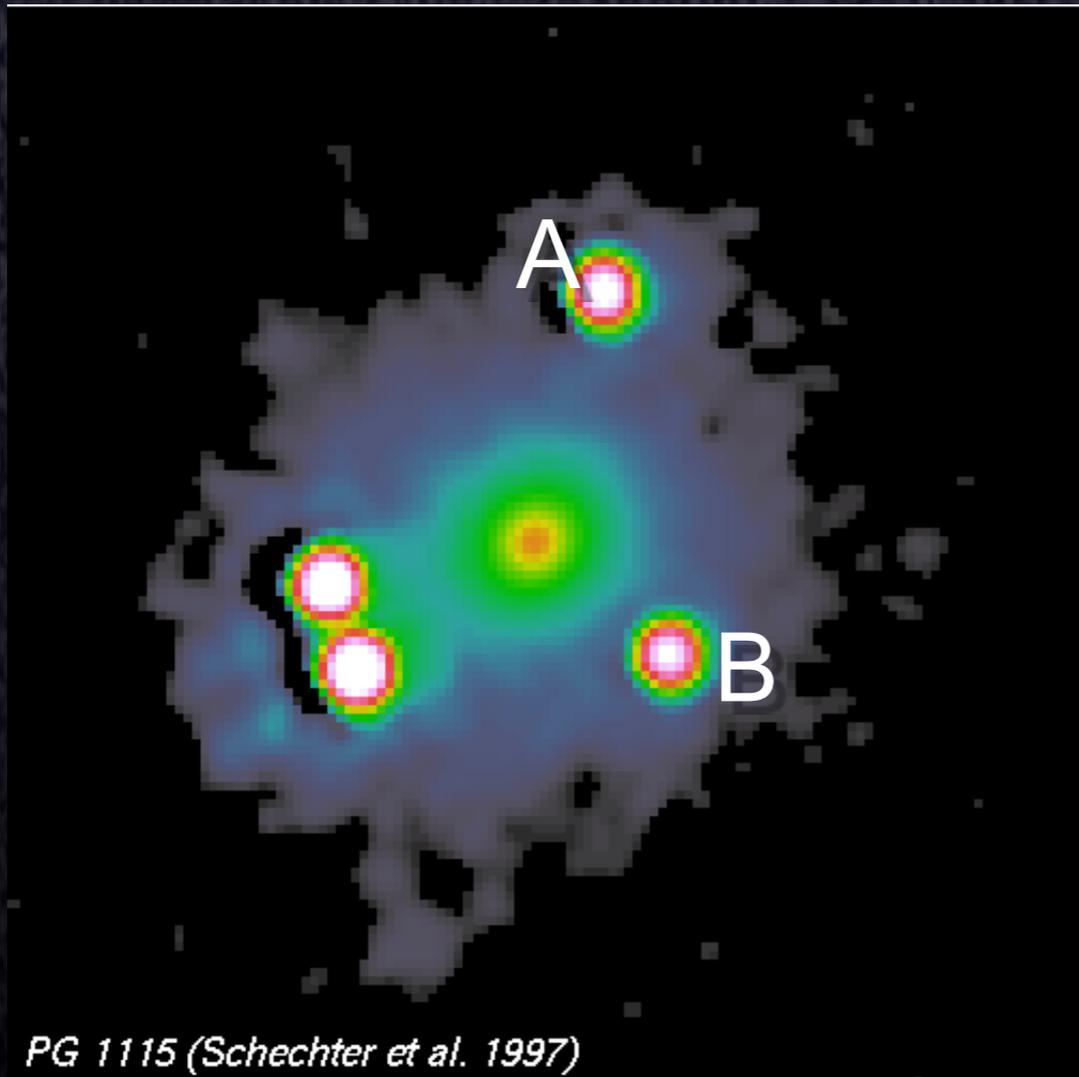


Image also
contains noise

Comparison of Space vs Ground: A1689



Strong Lensing



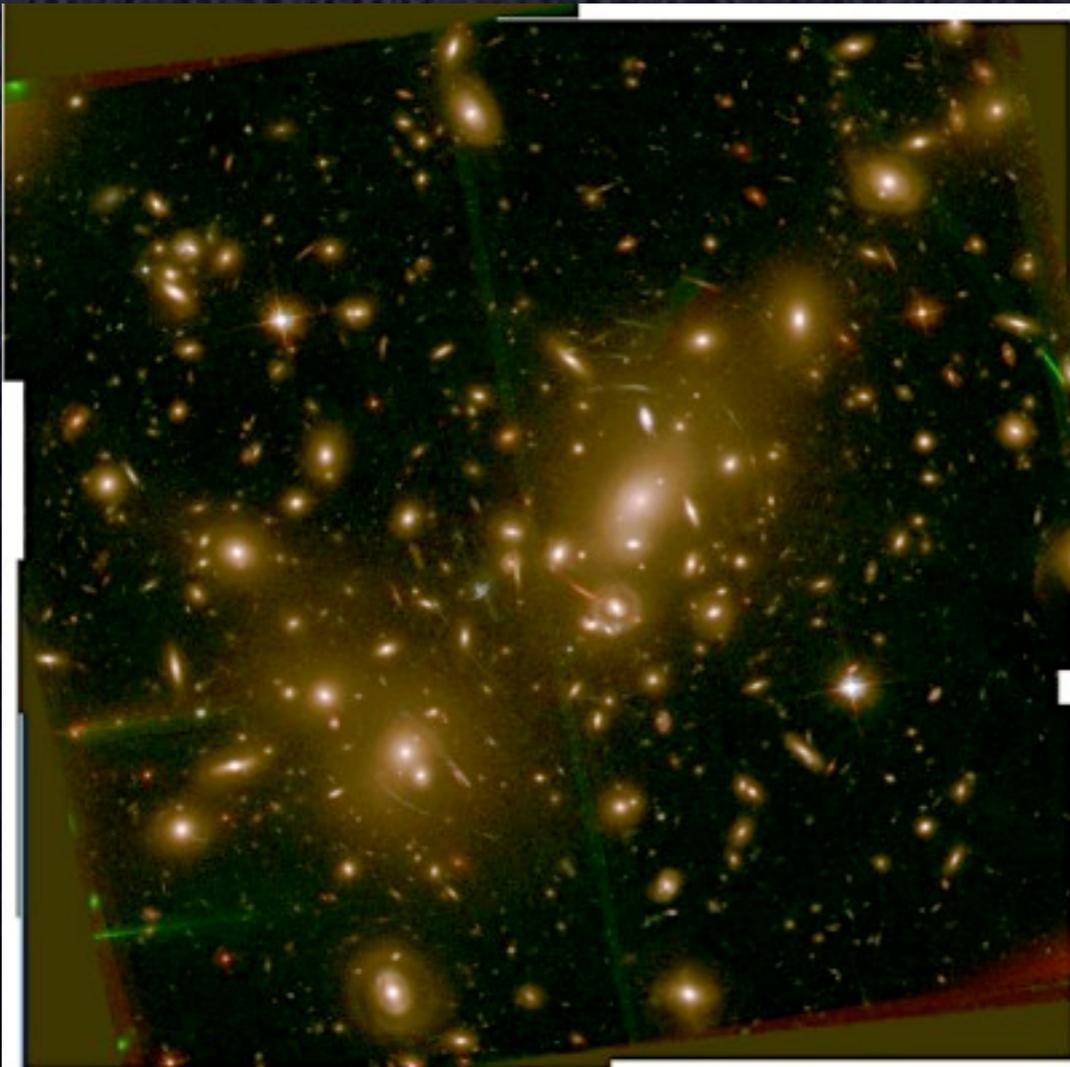
$$\alpha_i = \psi_i$$

$$\alpha_A - \alpha_B = \theta_A - \theta_B$$

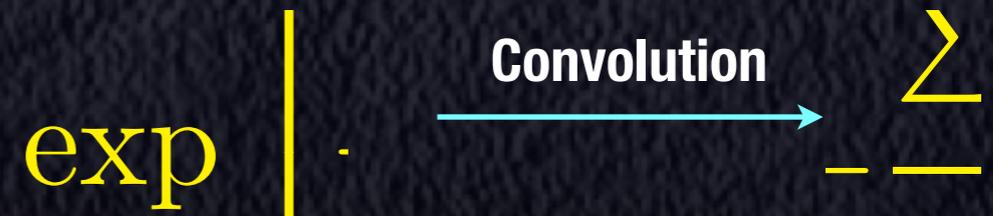
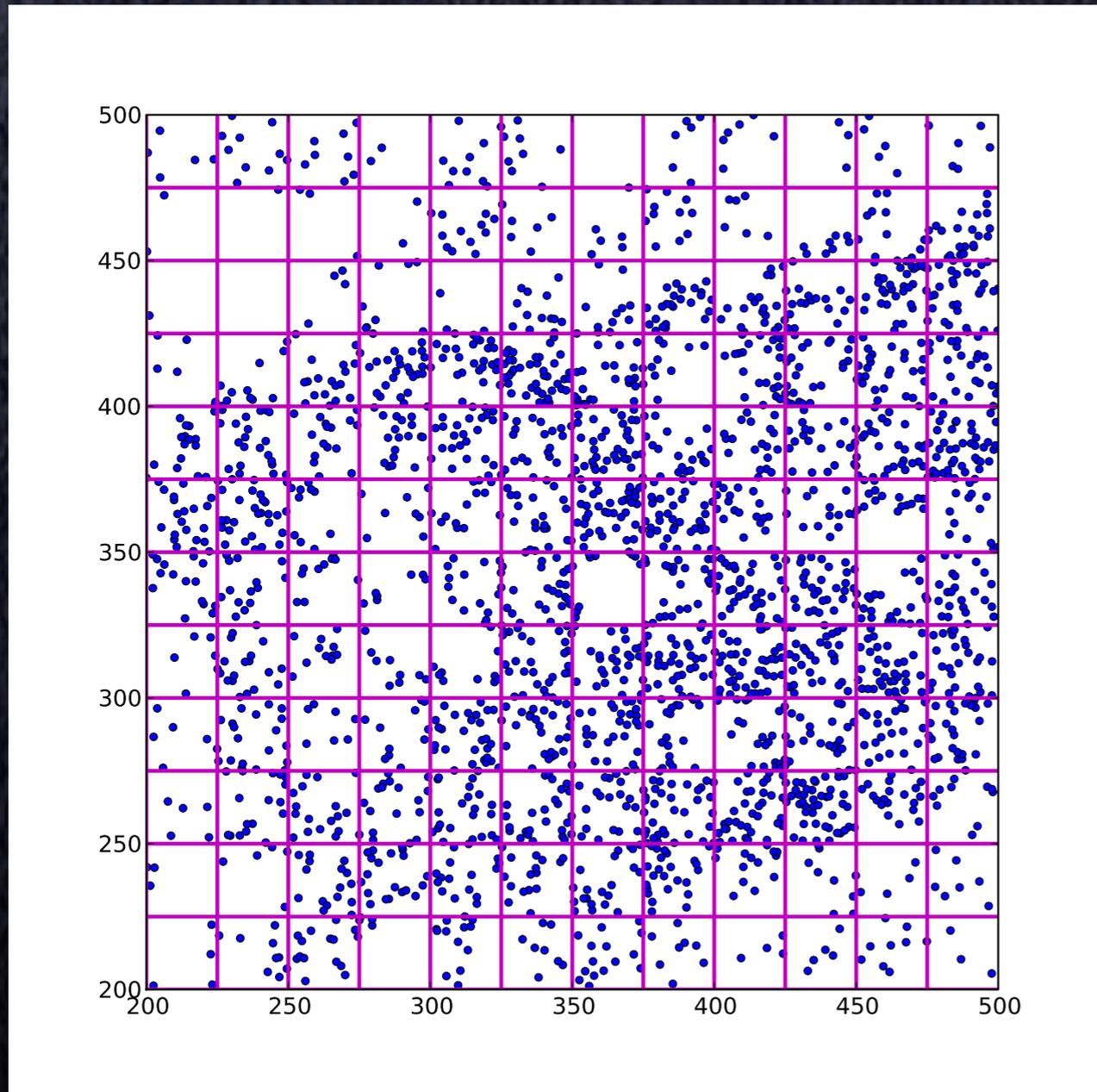
Parametric technique

Assumption: Light traces mass

- Place galaxy sized halos at the location of Cluster Members.
- Have one or more dark matter halos with free parameters that are fit from data.

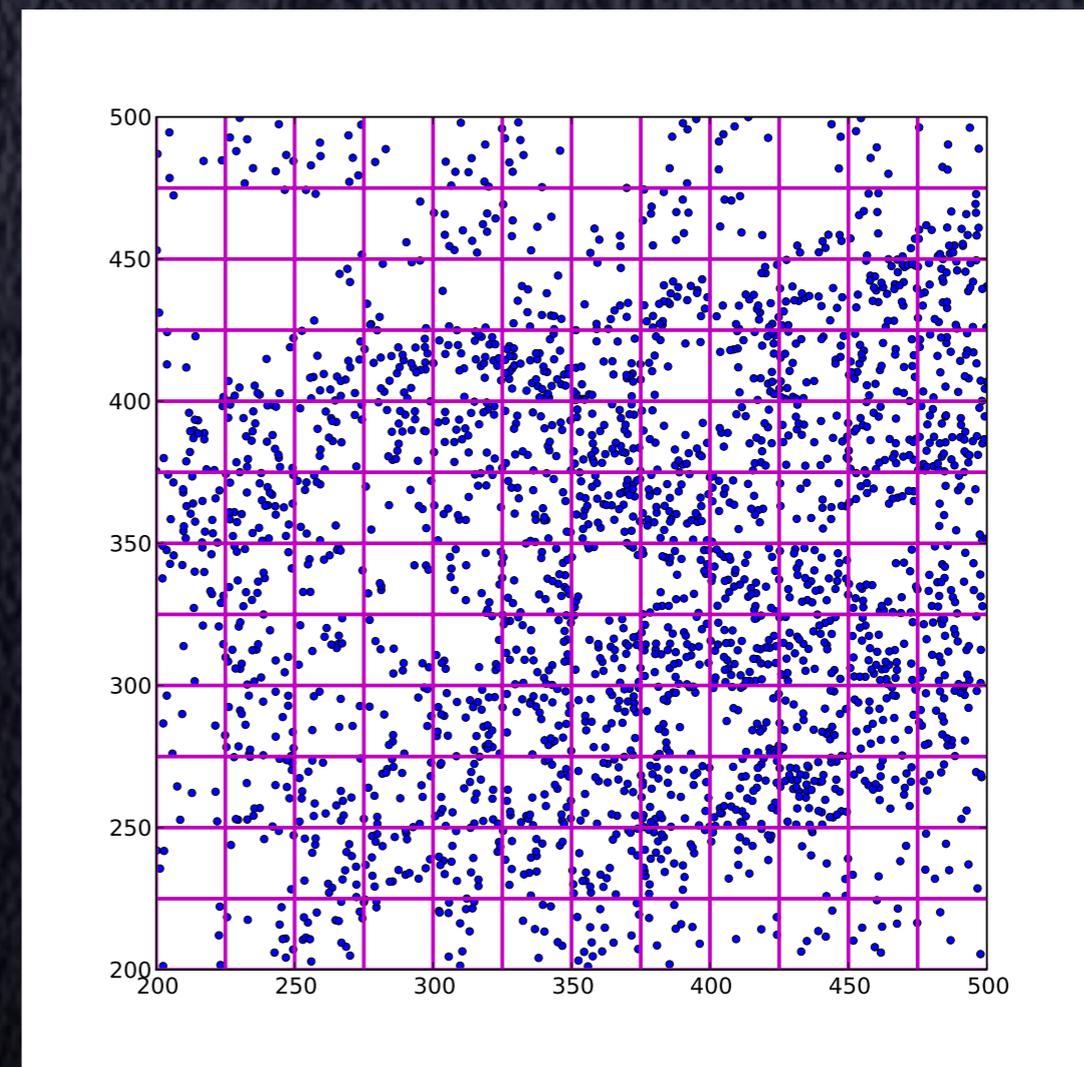
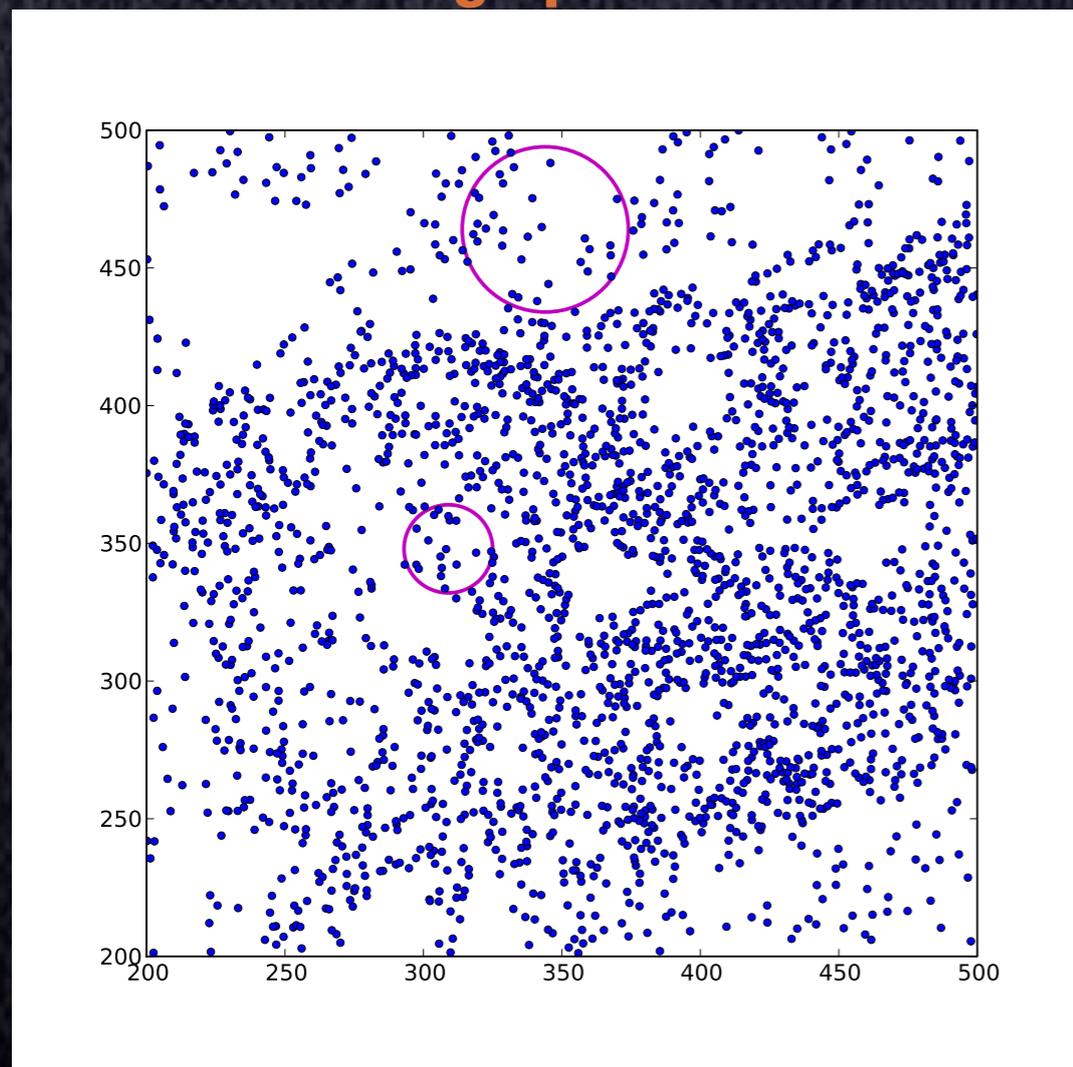


Grid Based Lensing



Particle Based Lensing

Particles → lensed
image positions



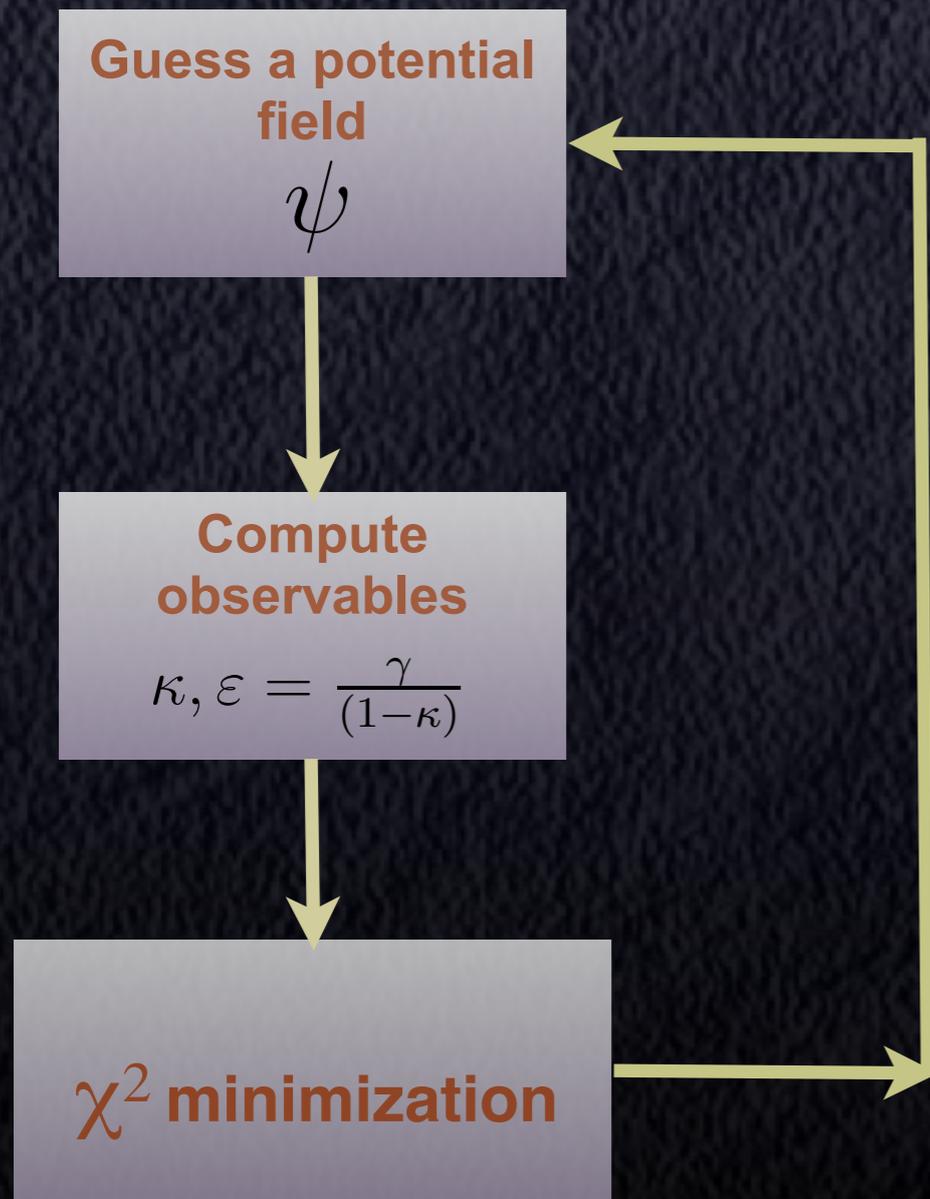
- Variable Resolution with the same complexity as finite differencing on a regular grid.
- No empty grid cells.

Reconstruction Procedure

Keep Iterating ...

$$\chi_{\text{weak}}^2 = \sum_i \frac{\left[\varepsilon_i - \frac{\gamma_i}{(1-\kappa_i)} \right]^2}{\sigma_i^2}$$

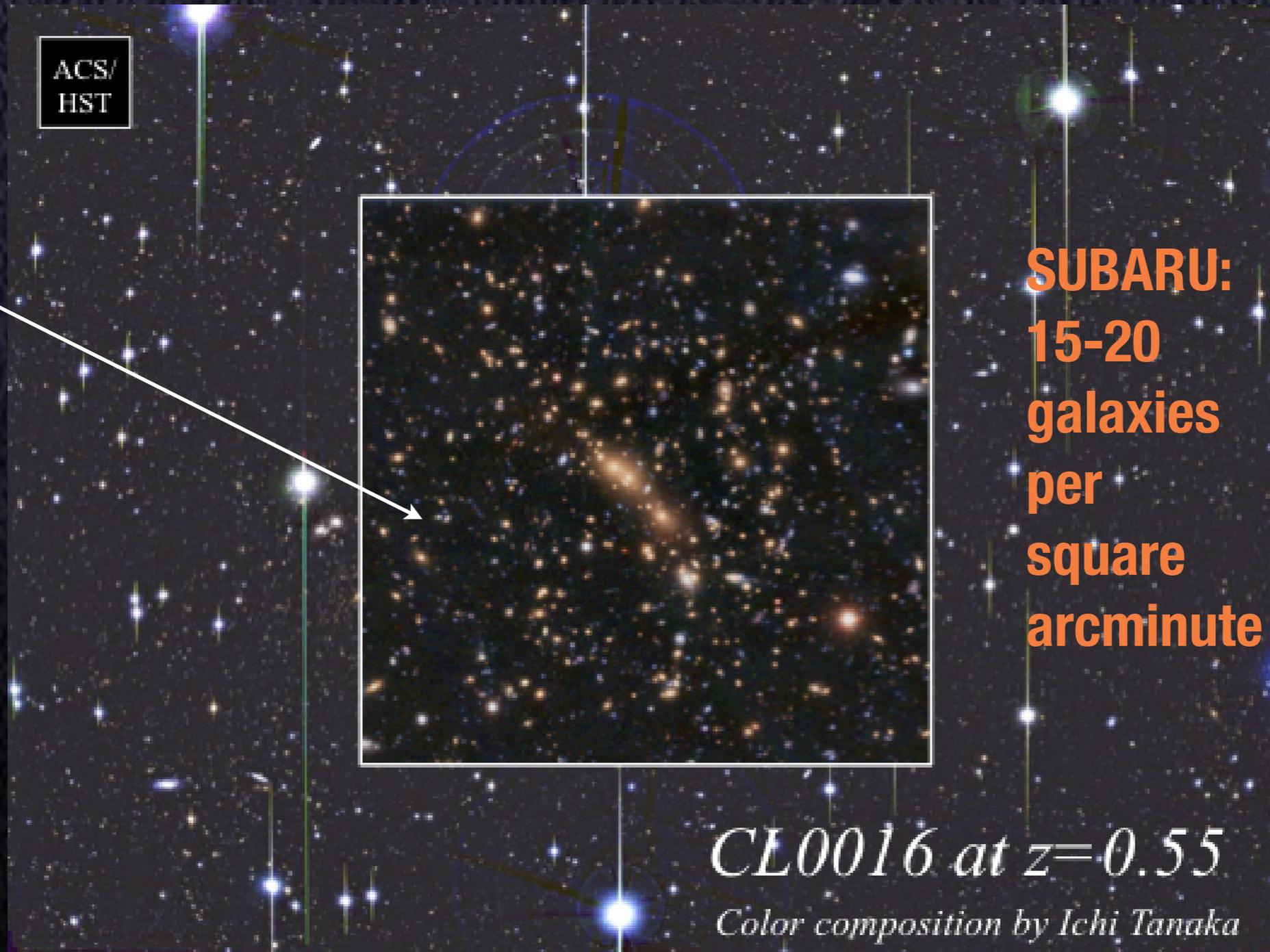
In case of weak lensing, a χ_{w}^2 like this will fit best to noisy data



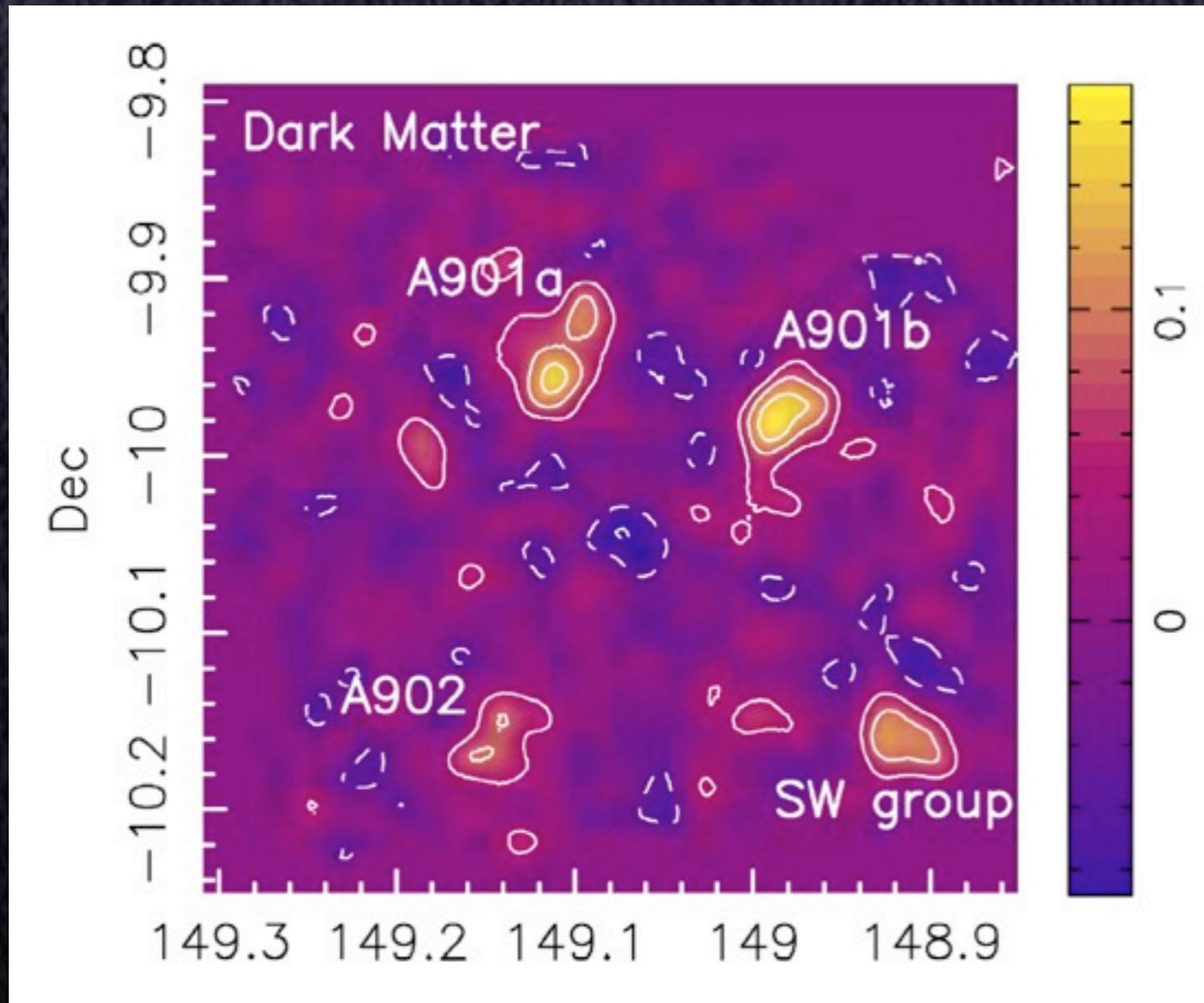
Smoothing the ellipticity field before minimization and using the full covariance matrix in the minimization

Heterogeneous Datasets

HST:
50-60
galaxies
per
square
arcminute



Abell 901/902

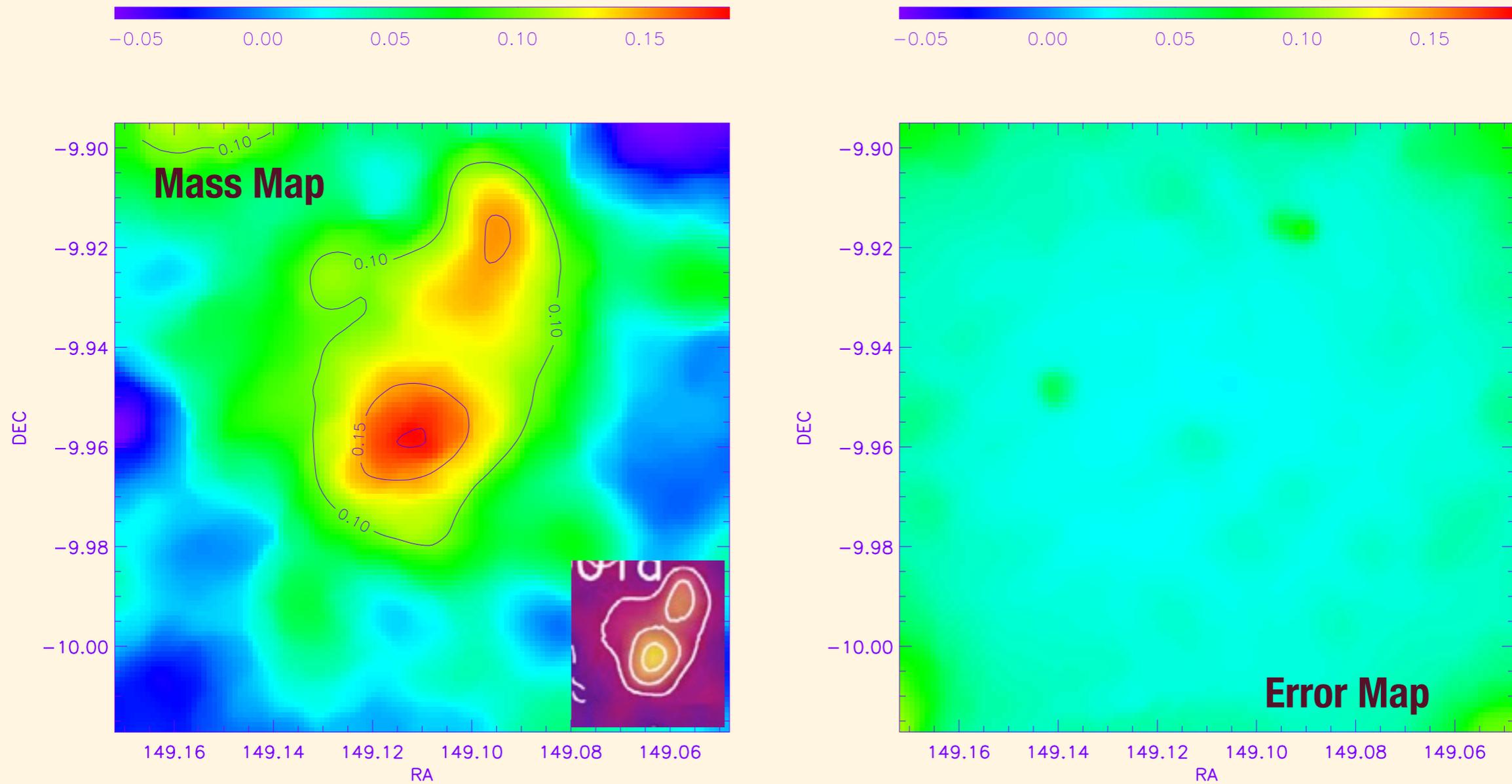


0.5 degree² fov
STAGES HST
survey
60,000 background
images.

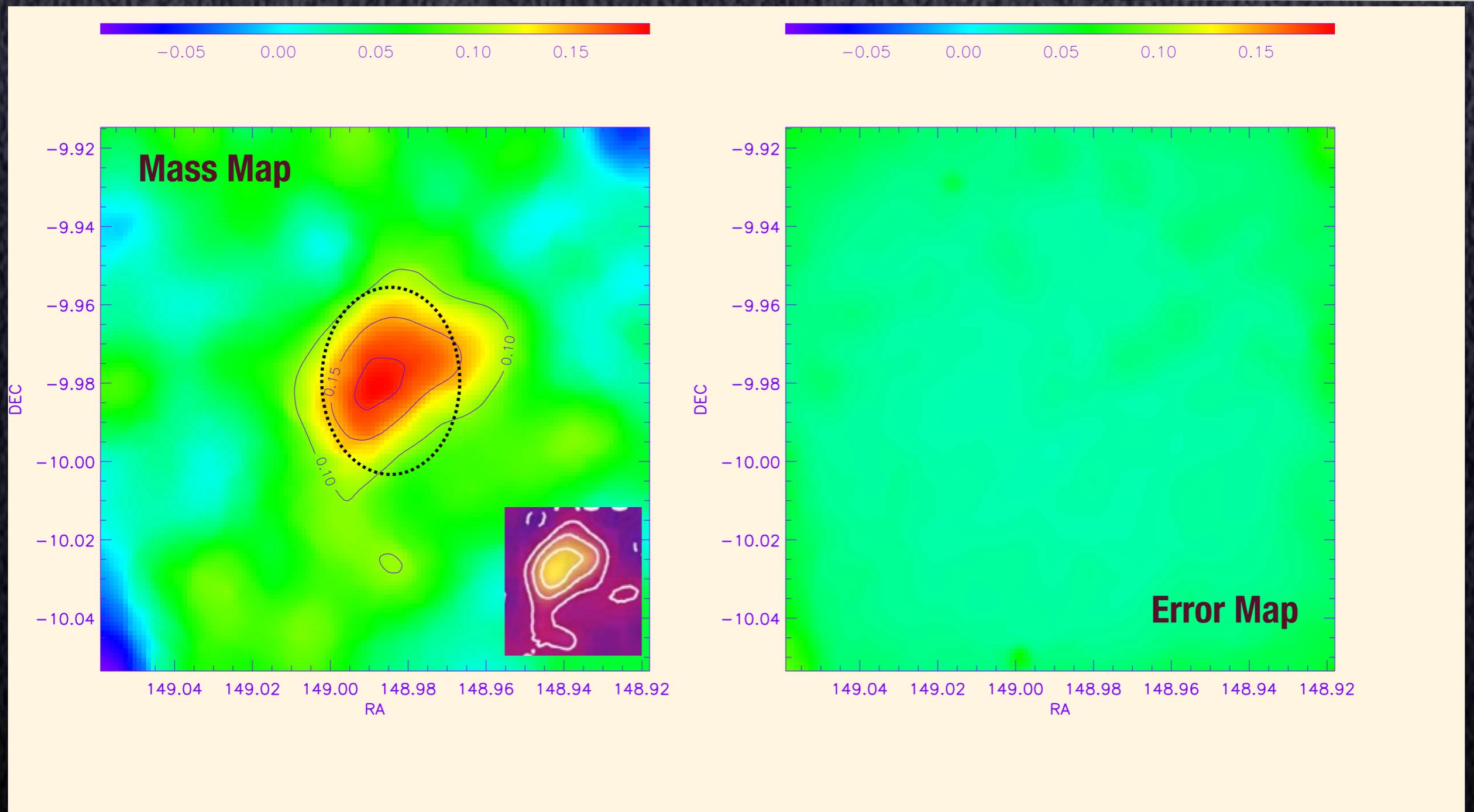
Heymans et. al. 2008.

A901a

From Deb et al. 2009



A901b

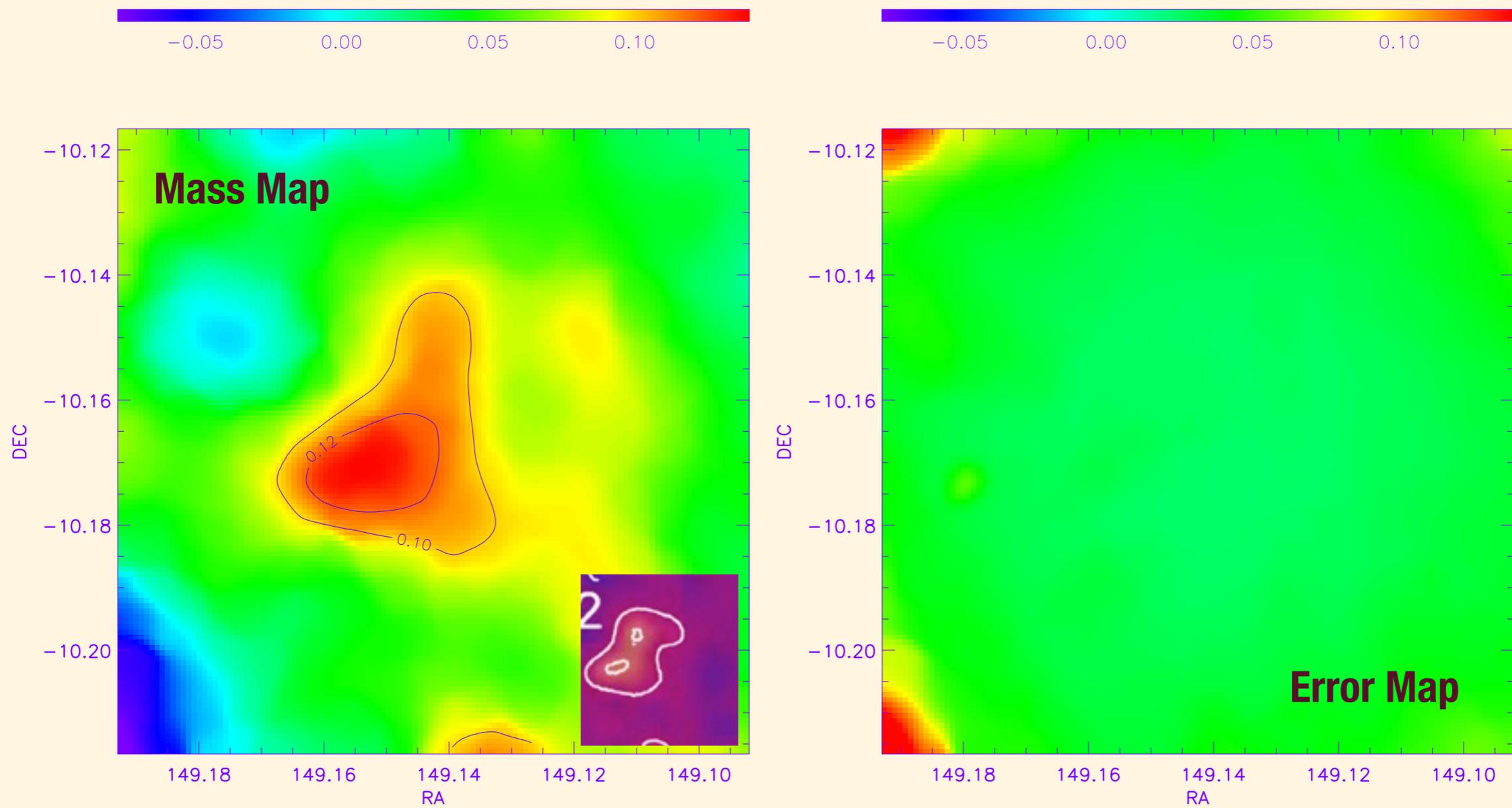


From Deb et al. 2009

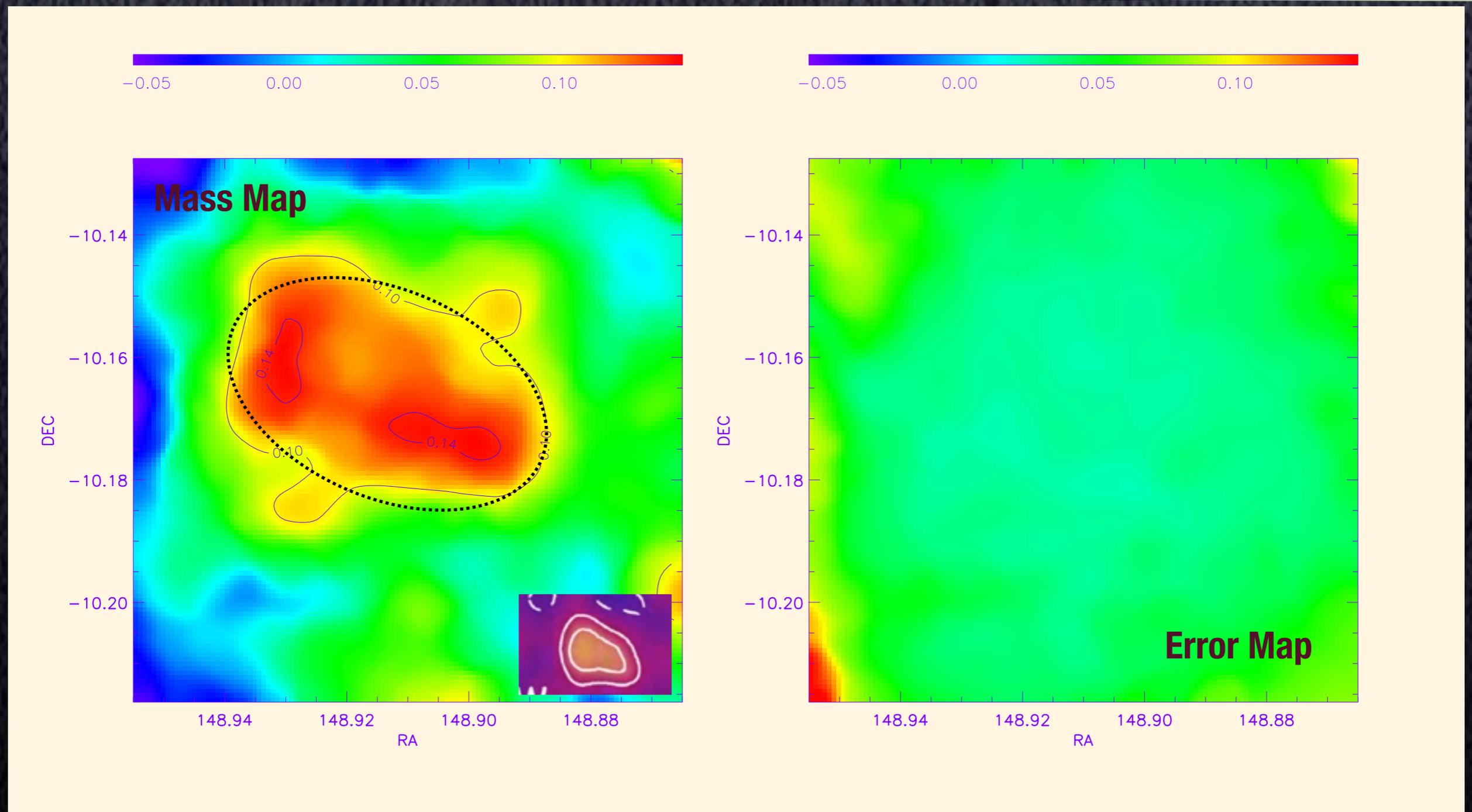
	Axis Ratio	Position angle		Axis Ratio	Position angle
Non-Parametric:	$0.37^{+0.1}_{-0.1}$	$91.4^{+8.2}_{-8.2}$	Parametric:	$0.437^{+0.1}_{-0.087}$	$90.0^{+2.25}_{-2.25}$

A902

From Deb et al. 2009



Southwest Group

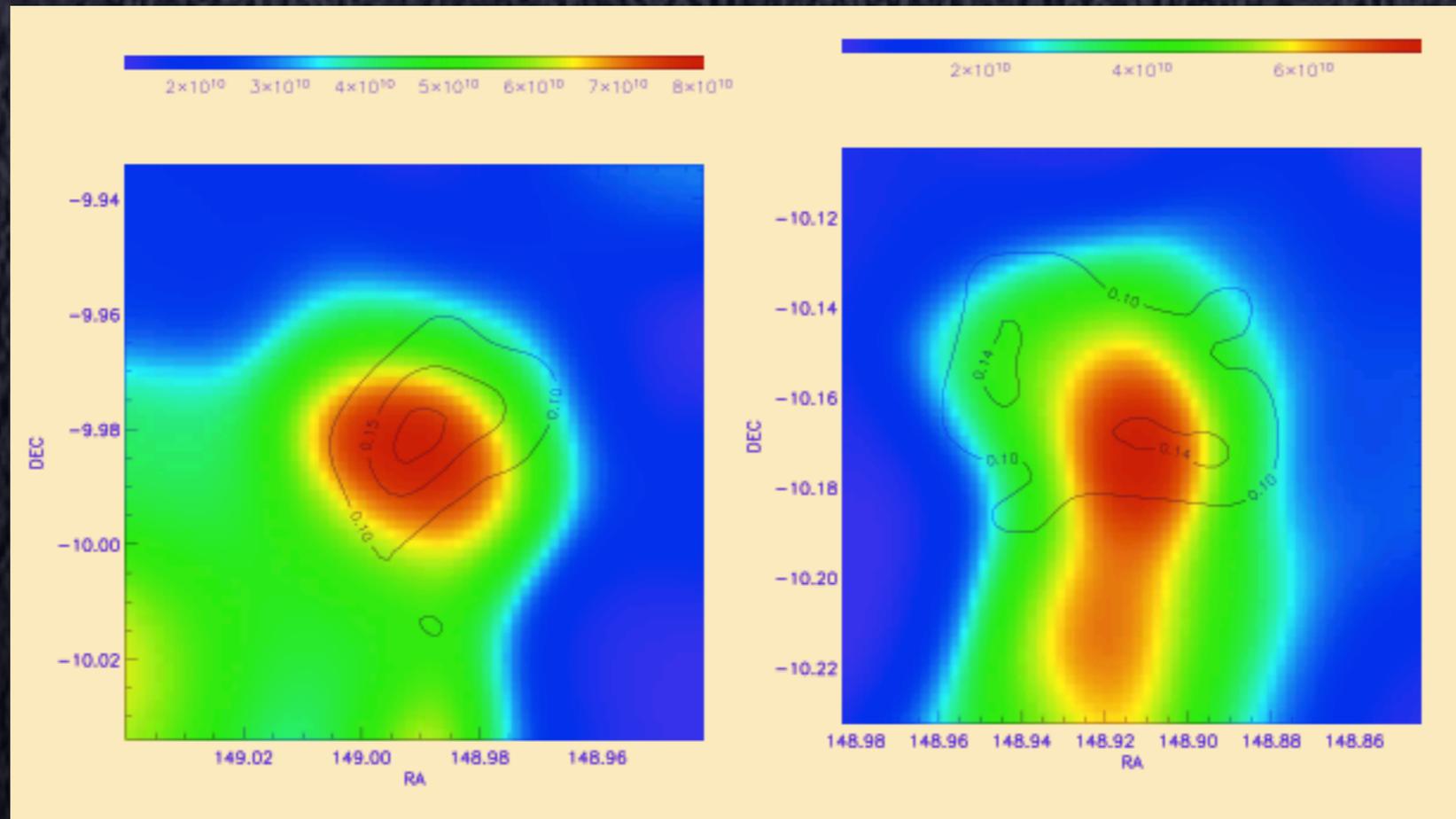


From Deb et al. 2009

	Axis Ratio	Position angle		Axis Ratio	Position angle
Non-Parametric:	$0.54^{+0.08}_{-0.09}$	$120.0^{+4.8}_{-4.8}$	Parametric:	$0.42^{+0.18}_{-0.12}$	$180.0^{+7.73}_{-5.15}$

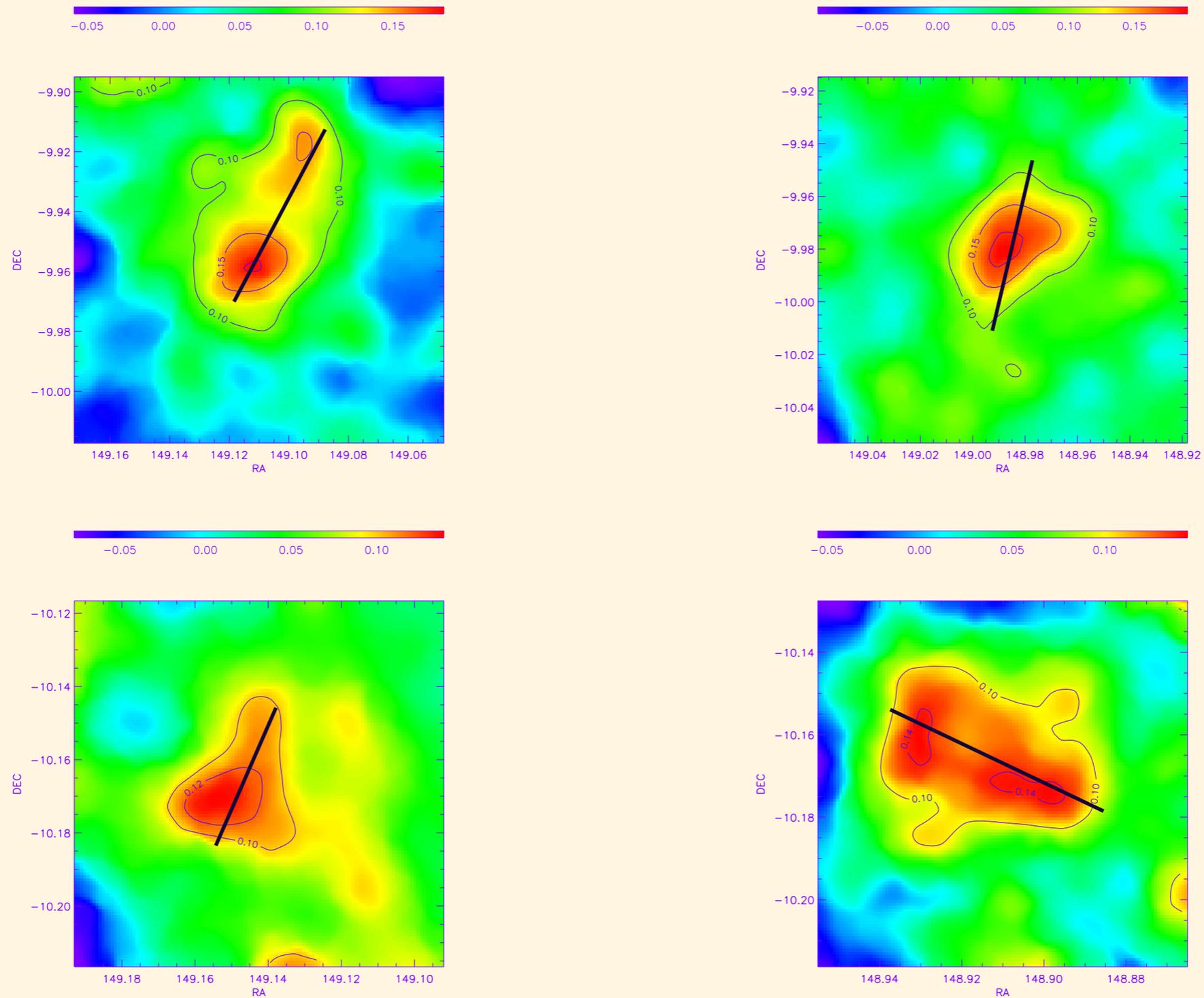
Dark Matter vs Light

From Deb et al. 2009



Alignment

From Deb et al. 2009



Reconstruction Methods

Parametric:

Strong Lensing

GRAVLENS - Keeton et al., 2001

LENSTOOL - Jullo et al., 2007

Galaxy-Galaxy

Lensing

Natarajan et al. 2005

Hybrid

LENSTOOL -
Jullo et al., 2009

Non-Parametric

Strong Lensing

Jullo & Kneib 2009,

LENSPERFECT -Coe et al, 2008,2010 (Mesh Free)

Weak Lensing

Kaiser 1995, Seitz & Schneider 1995-2001

Strong+Weak Lensing

Finite Differencing Based

Bradac et al. 2004,

(ADAPTIVE) - Diego et al. , Cacciato et al.

Merten et al., Saha et. al. Pixelens

and more

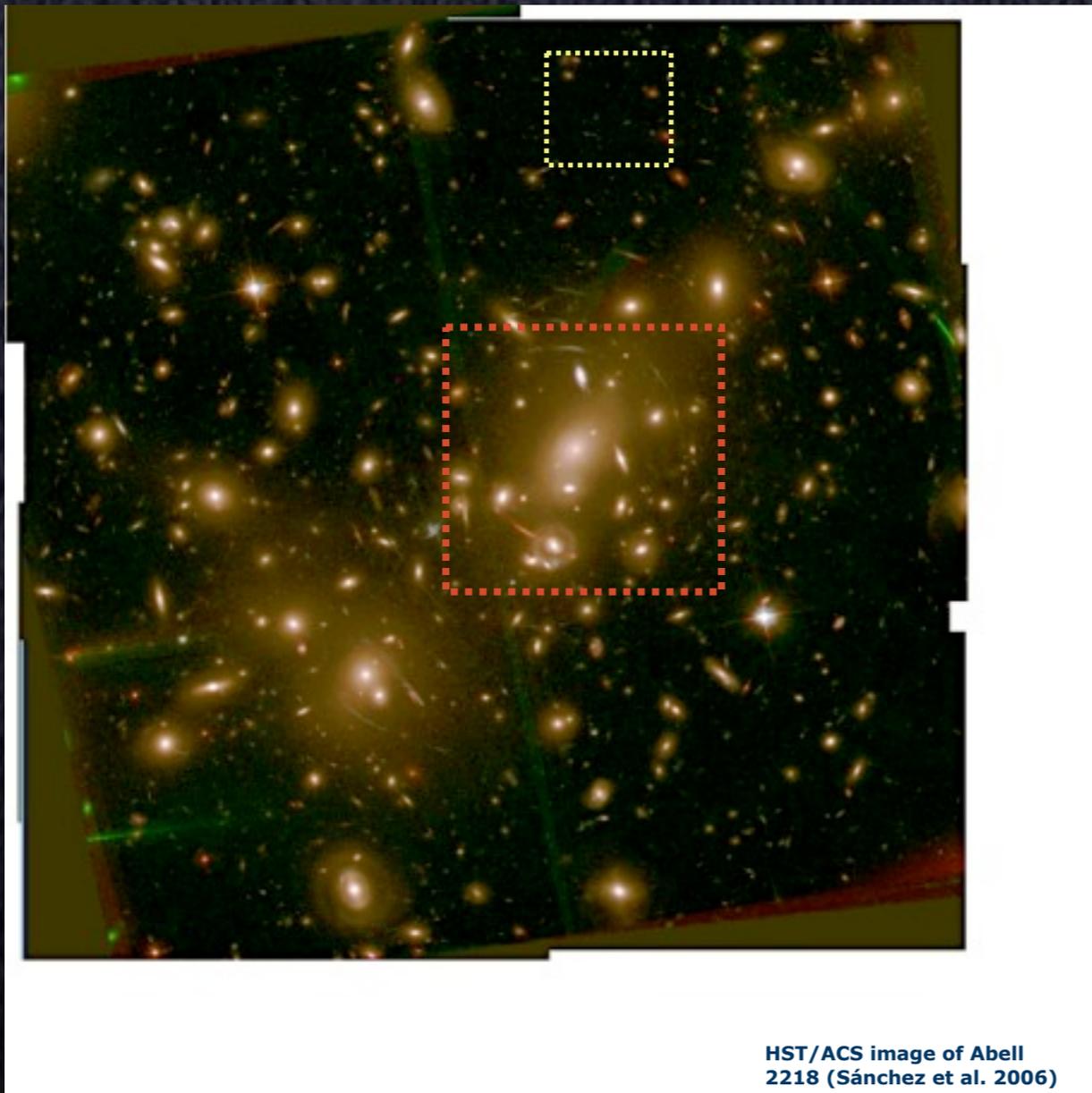
Mesh-Free Technique

Particle Based Lensing

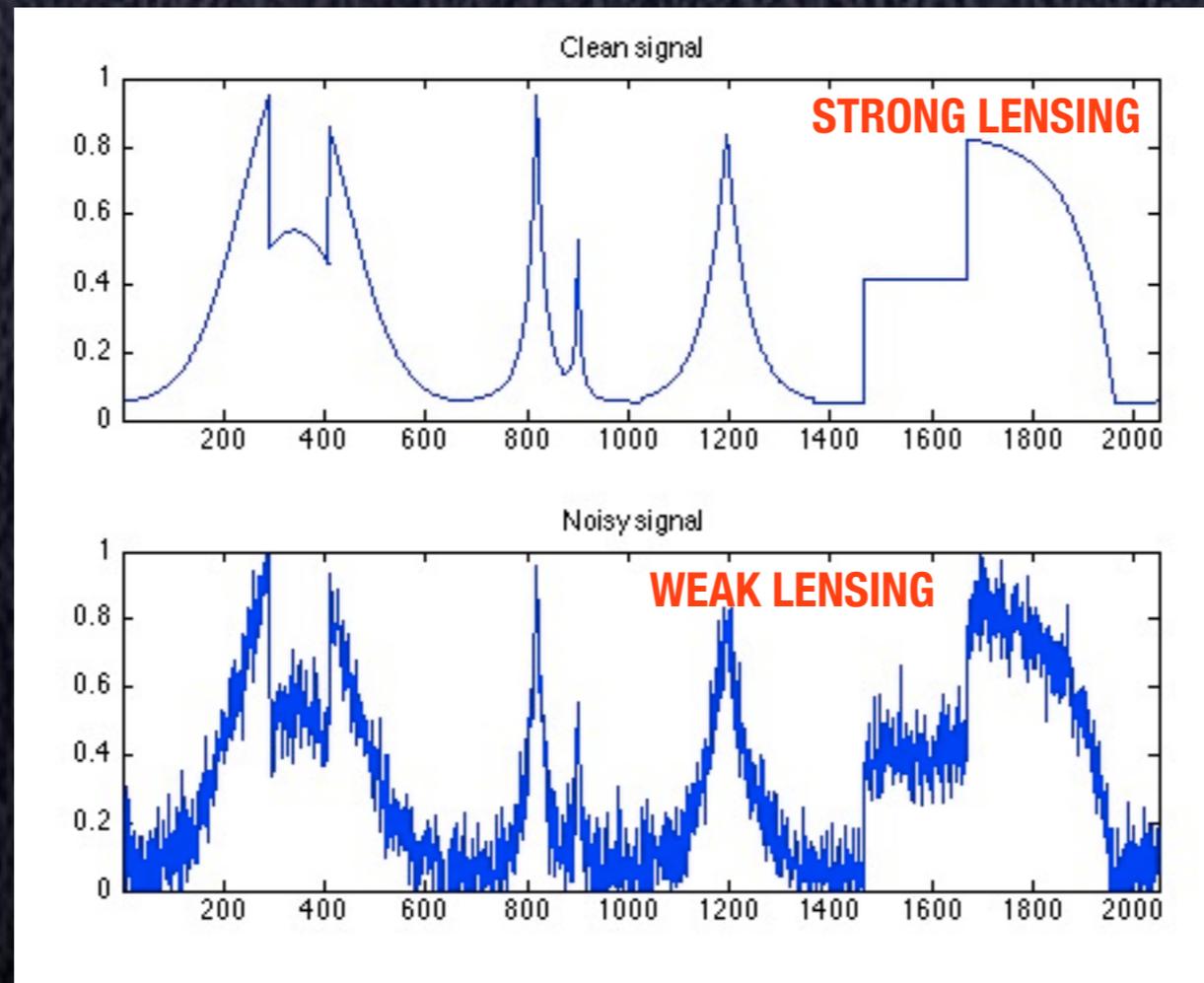
(PBL)

Deb et al. ,2008, 2009

Strong+Weak Lensing: Challenges



Strong+Weak Lensing



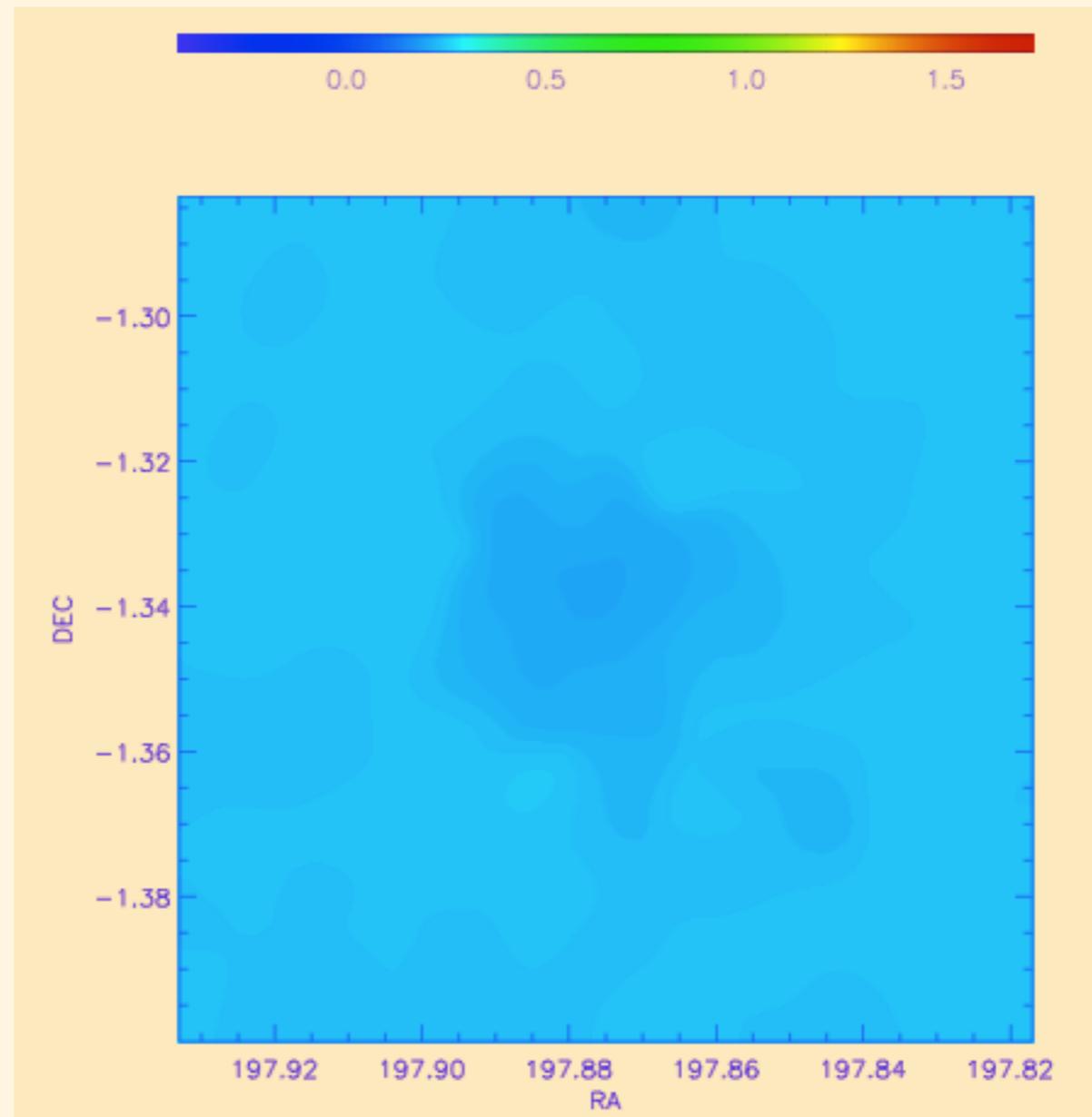
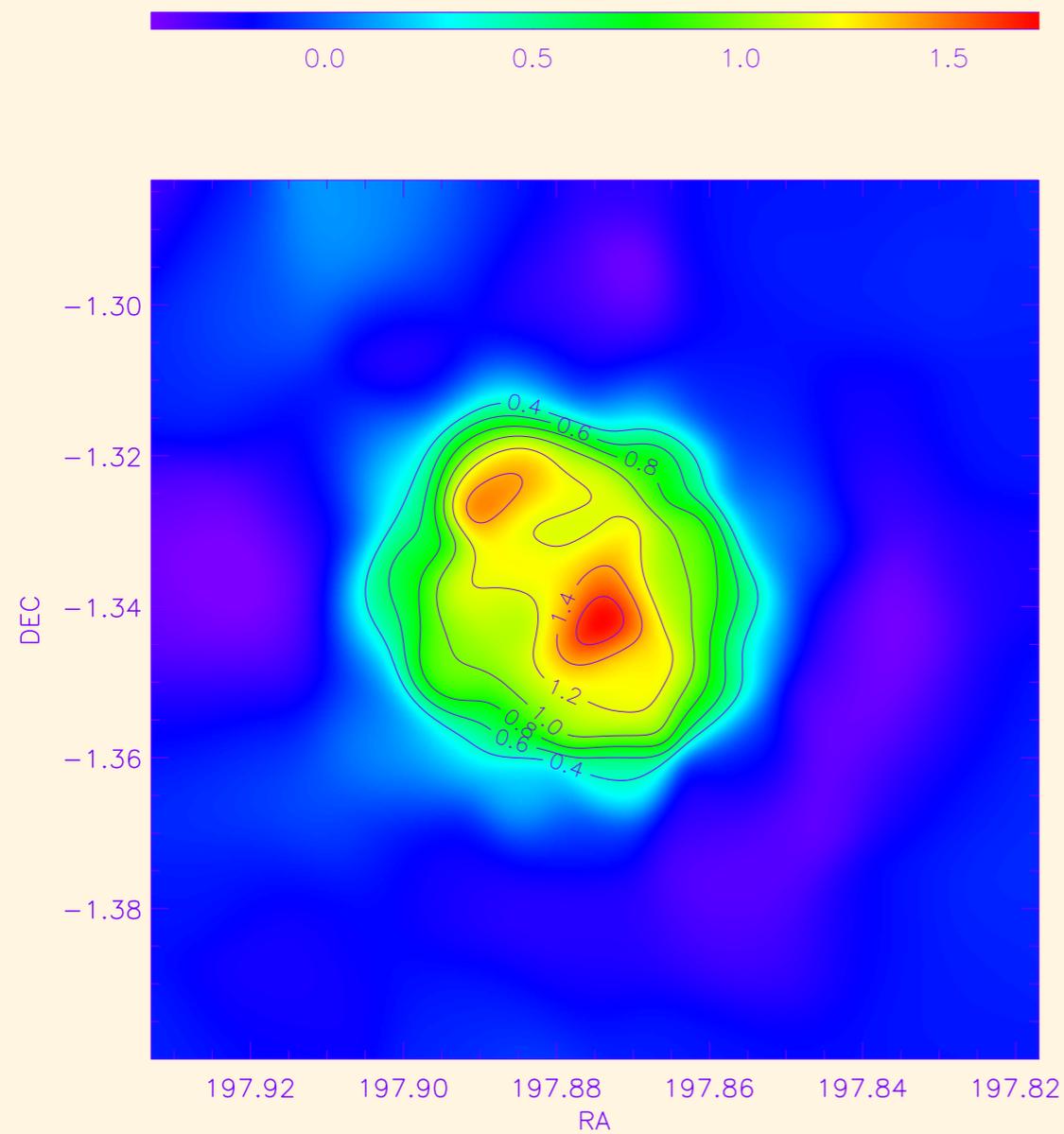
+

A1689

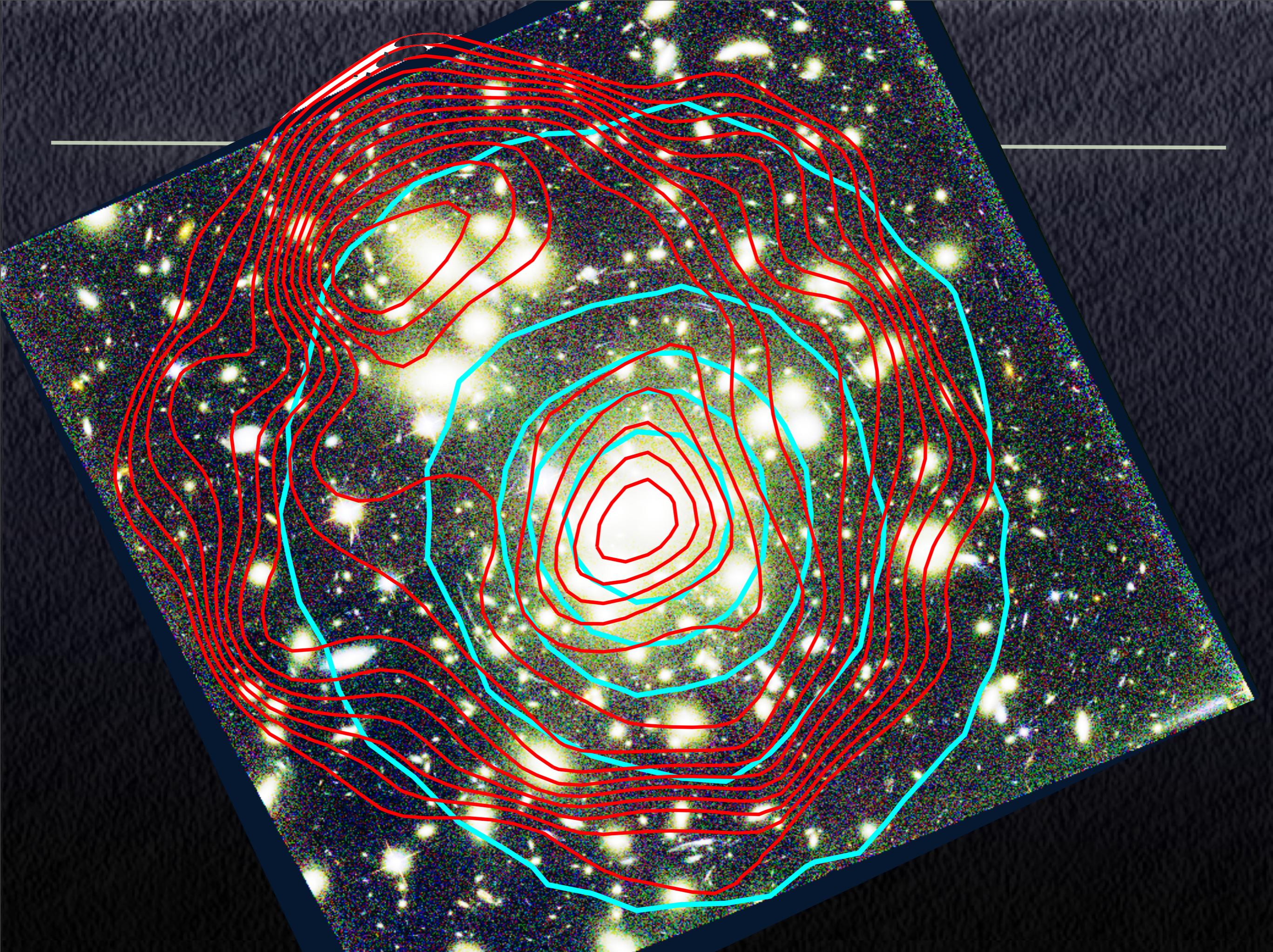


<http://chandra.harvard.edu/photo/2008/a1689/>

Mass Map

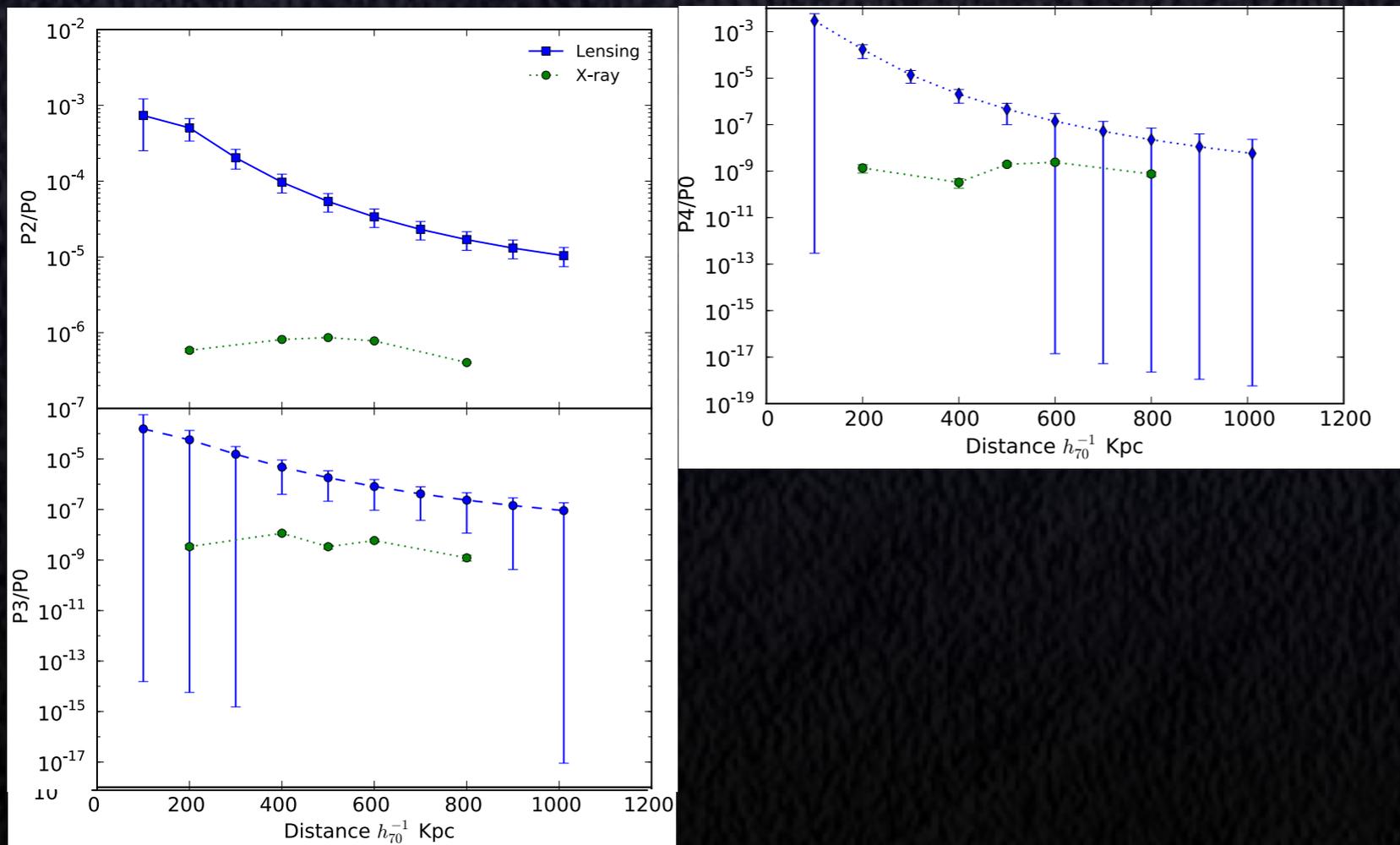


Error Map

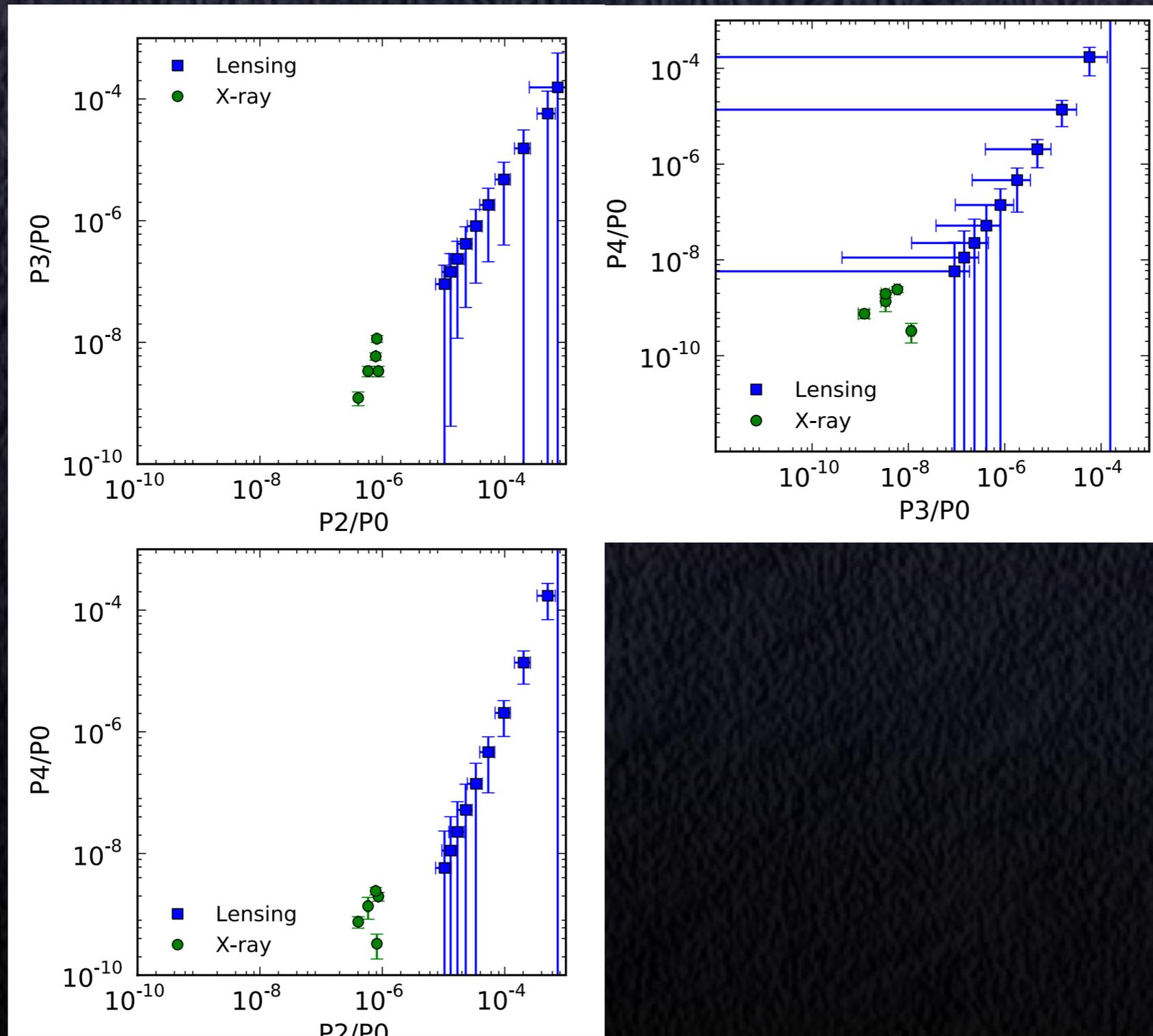


Power Ratios

Moments of the mass distribution characterize the morphology and substructure in dark matter distribution.

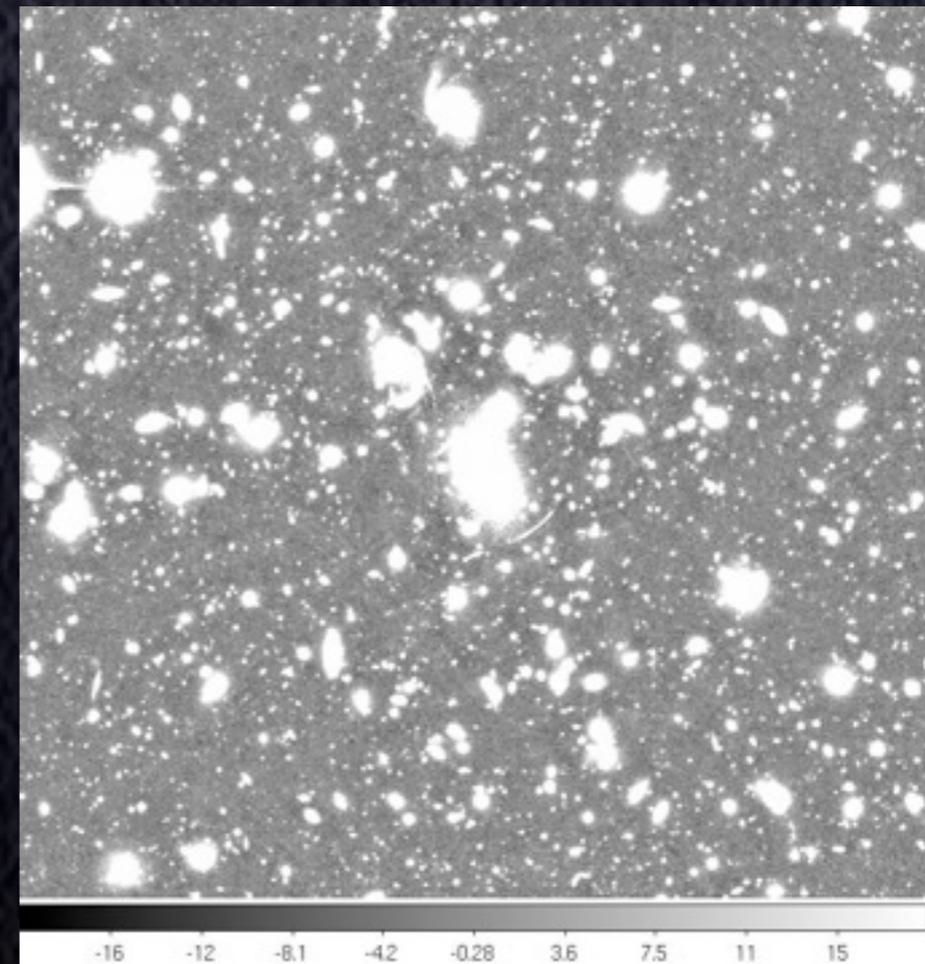
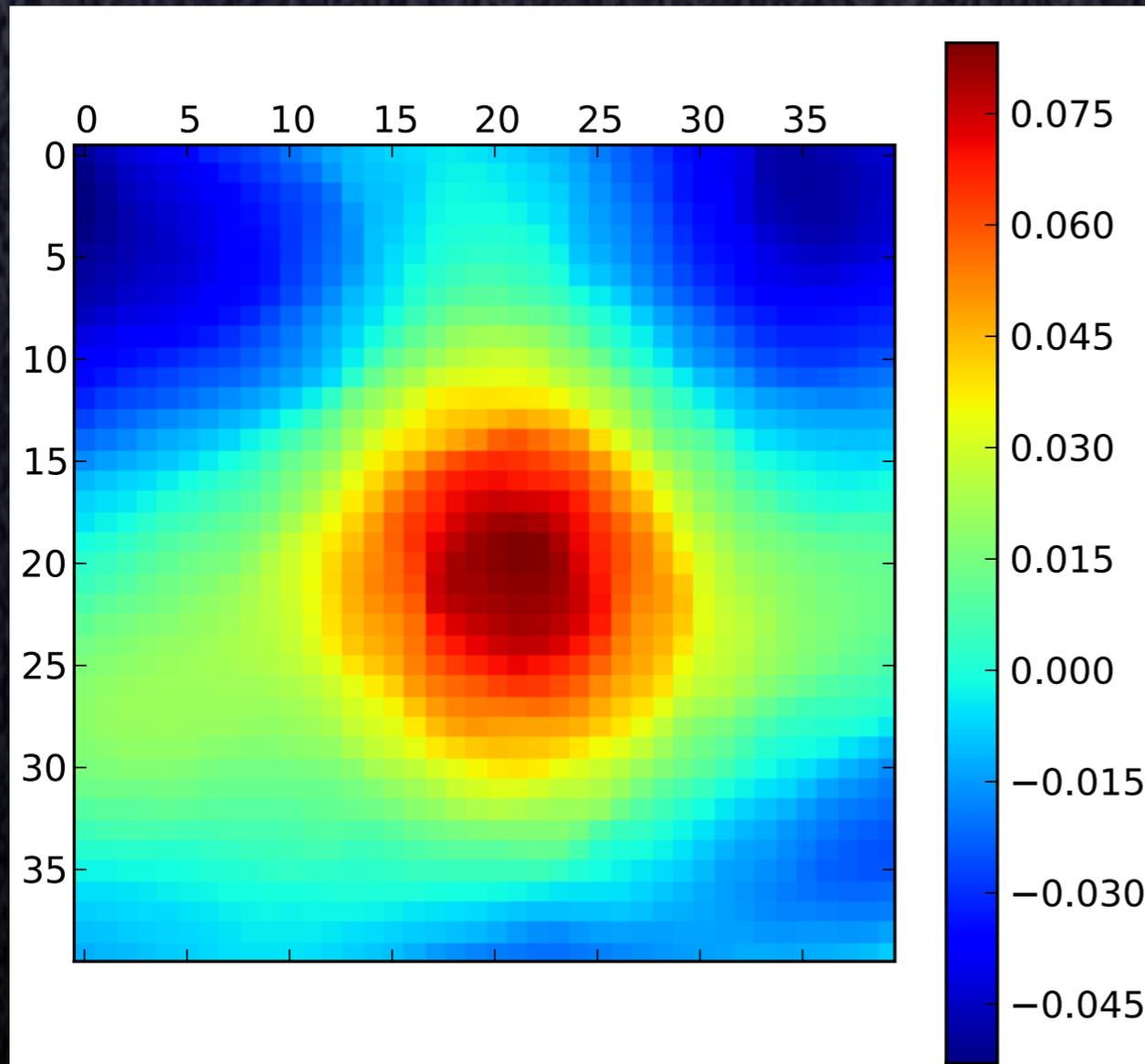


Cross-Correlations



Current Research

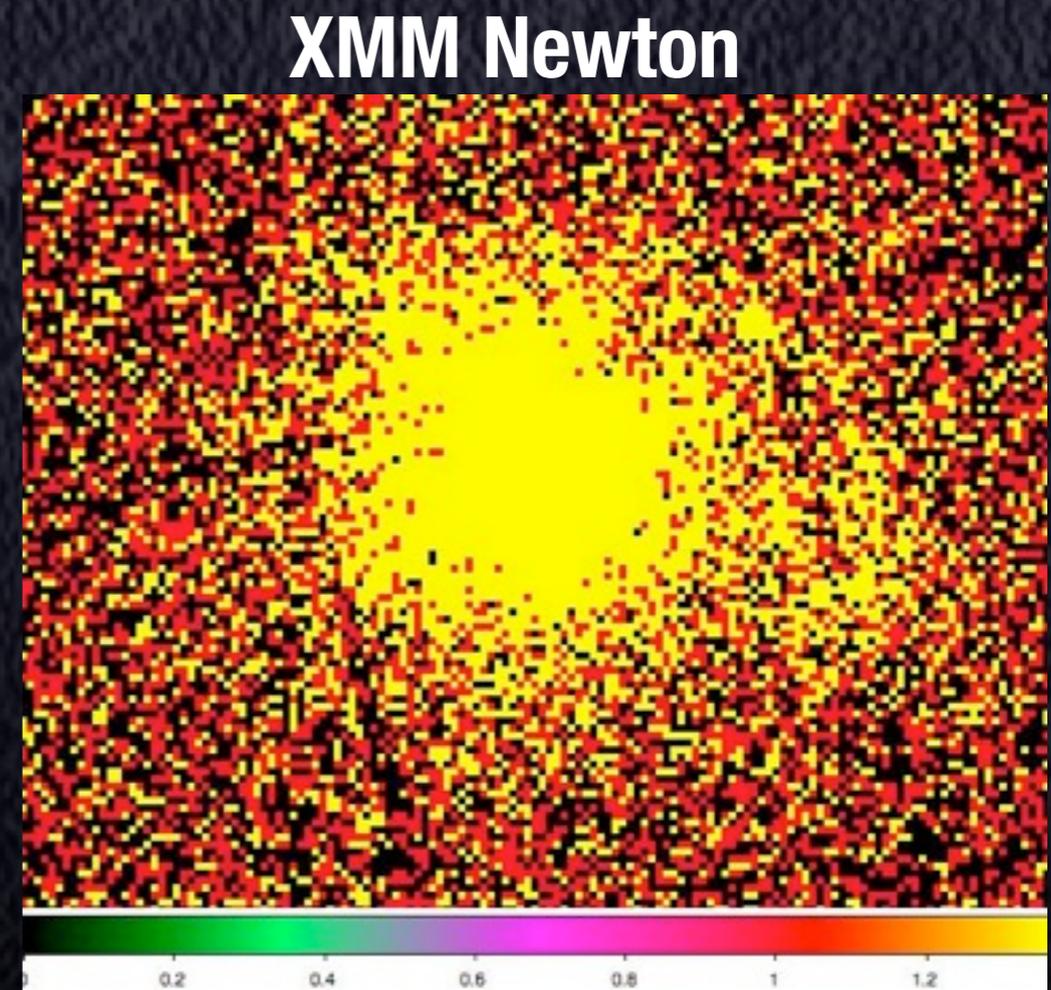
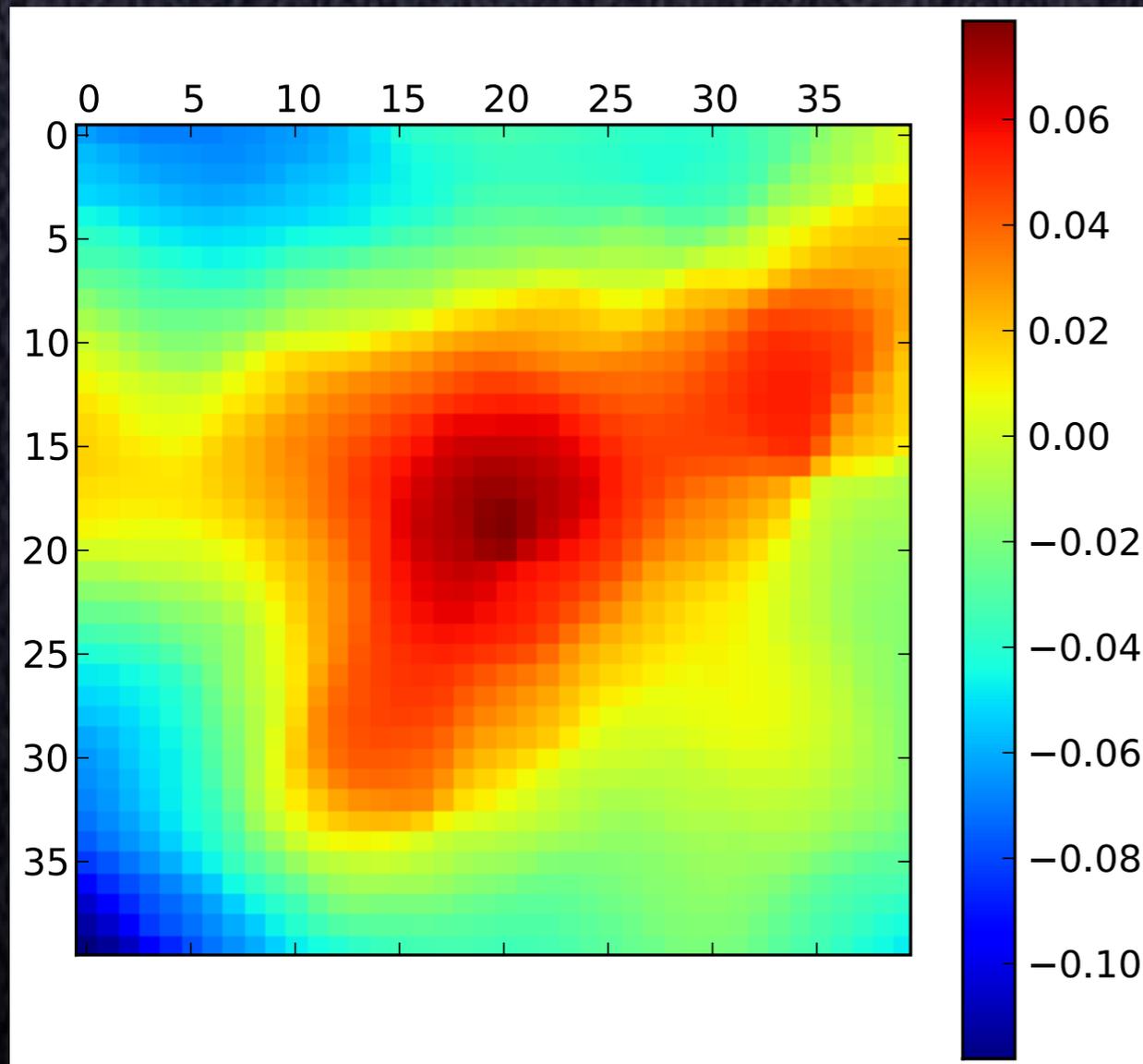
A2219: Optical vs Lensing mass reconstruction



PRELIMINARY

Current Research

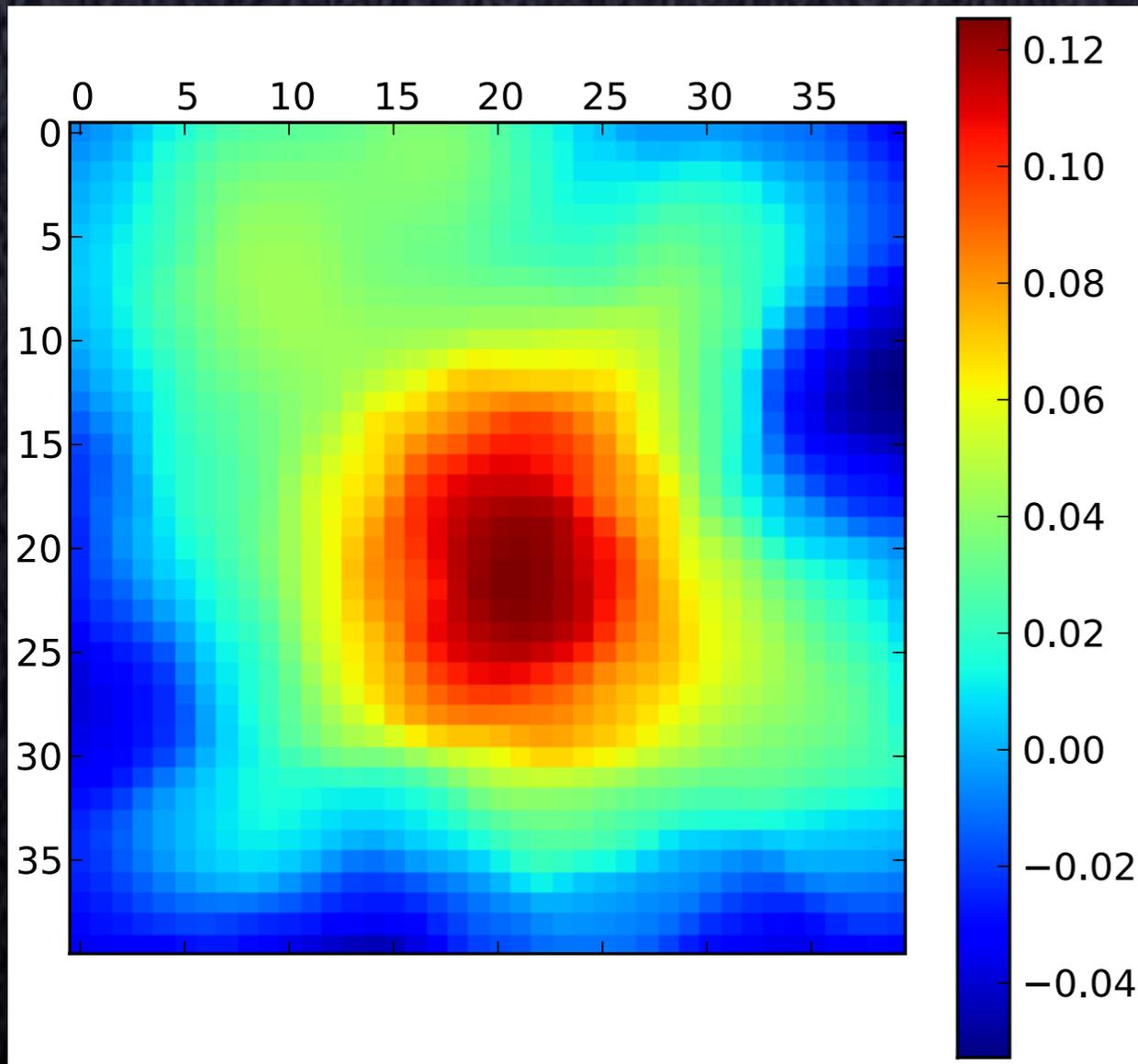
A2261: X-ray vs Lensing mass reconstruction



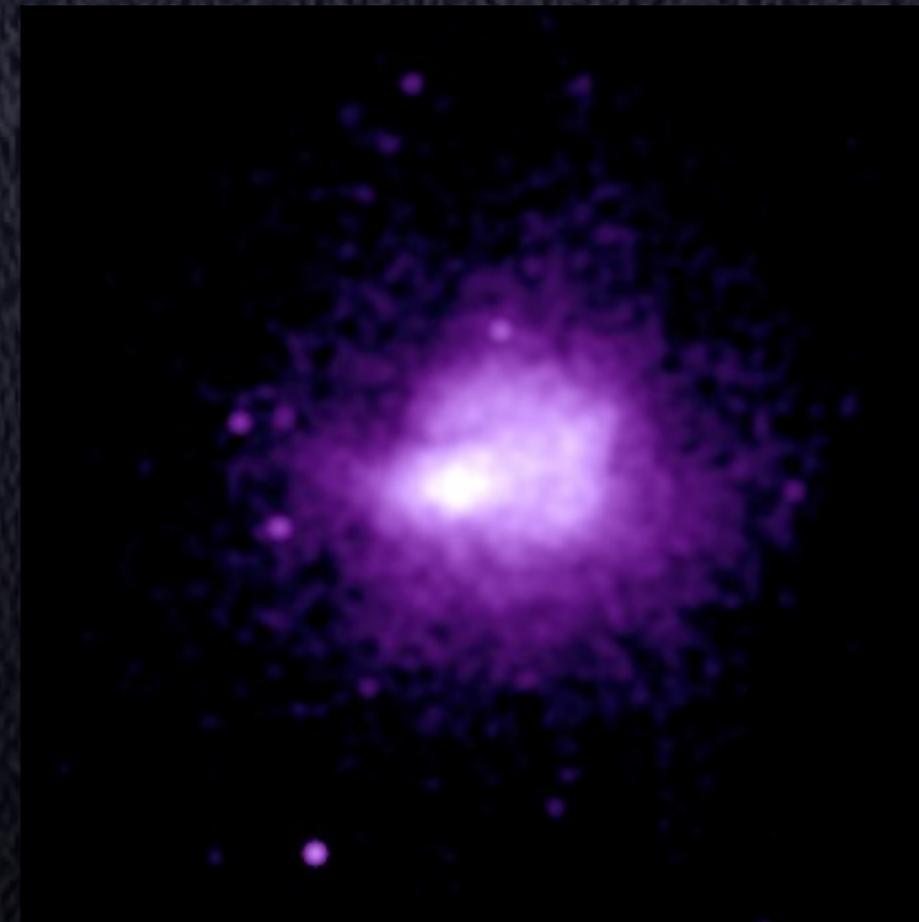
PRELIMINARY

Current Research

A1914: X-ray vs Lensing mass reconstruction



Chandra data



<http://chandra.harvard.edu/photo/2006/clusters/>

PRELIMINARY

Summary

METHOD

Developed a non-parametric mass reconstruction technique “Particle Based Lensing” (PBL).

PBL is applied to compute mass maps of variable resolution and signal-to-noise.

RESULTS

- * The **ellipticity** for the light distribution is smaller than the ellipticity of the dark matter distribution for A901b and the Southwest Group.
- * A901a, A901b and A902 have **strong alignment** whereas the Southwest group is not aligned with the rest of the peaks.
- * The **gas** distribution of A1689 **is smoother** than the **dark matter** distribution.

Future Research

Mutiwavelength analysis for a sample of 20 Supermassive Clusters.