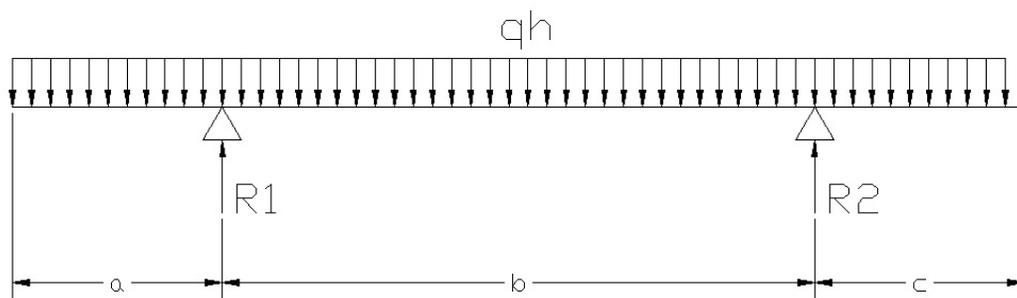
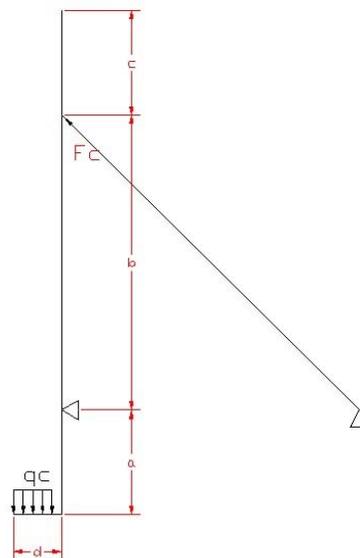


The Pictures below describe the orientation of the block raiser and the dimensions/variables which will be used for the analysis.



Beam Loading in the Horizontal Position



## 1.0 Define Inputs

$\text{tons} := 2000\text{lb}$	$\text{plf} := \frac{\text{lb}}{\text{ft}}$	$\text{psf} := \frac{\text{lb}}{\text{ft}^2}$	$\text{pcf} := \frac{\text{lb}}{\text{ft}^3}$	$\text{kips} := 1000\text{lb}$
$\text{ksi} := 1000\text{psi}$				
$f_y := 36\text{ksi}$		Yield strength of material		
$E_s := 29000\text{ksi}$		Youngs modulus of steel		
$W := 200\text{tons}$		Weight of the Block and block raiser table		
$W_t := 50\text{tons}$		Weight of BR Table		
$L := 53\text{ft}$		Length and width of the BR table		
$a := 11\text{ft}$		Distance from the end of the table to the first support/pivot point		
$b := 33\text{ft}$		Distance between supports.		
$c := 11\text{ft}$		Distance from support/cylinder to end of table		
$t_e := 66\text{mm}$		Thickness of Extrusions		
$N_p := 31$		Number of planes in a block		
$d := t_e \cdot N_p$		Length of forks		
$d = 6.71\text{ft}$				
$N_f := 24$		Number of forks		
$N_b := 24$		Number of beams		

## 2.0 Determination of Distributed Loading

$$q_h := \frac{W}{N_b \cdot L} \quad \text{Loading on Table in the horizontal position}$$

$$q_h = 314.47 \frac{\text{lb}}{\text{ft}}$$

$$q_c := \frac{W - W_t}{N_f \cdot d} \quad \text{Loading on Forks in the Vertical Position}$$

$$q_c = 1862.17 \frac{\text{lb}}{\text{ft}}$$

### 3.0 Calculation of Critical Moments

Examine the table moments in the horizontal position first.

$$R_n := \frac{q_h \cdot L}{2} \quad \text{Reaction force at support points}$$

$$R_n = 8.33 \text{ kips}$$

$$M_n(x) := \begin{cases} \left( \frac{q_h \cdot x^2}{2} \right) & \text{if } a > x \\ \left[ R_n \cdot (x - a) - \frac{q_h \cdot x^2}{2} \right] & \text{if } a \leq x < a + b \\ \left( R_n(x - a) + R_n(x - a - b) - \frac{q_h \cdot x^2}{2} \right) & \text{otherwise} \end{cases}$$

$$M_n(a) = -19.03 \text{ kips} \cdot \text{ft}$$

$$M_n\left(a + \frac{b}{2}\right) = 18.59 \text{ kips} \cdot \text{ft}$$

$$x := 0, L \dots 1.0 \text{ in}$$

Calculate the maximum moment and reaction force on the forks in the vertical position

$$M_f := \frac{q_c \cdot d^2}{2} \quad \text{Maximum moment at end of forks}$$

$$M_f = 41.95 \text{ kips} \cdot \text{ft}$$

$$R_{nf} := q_c \cdot d \quad \text{Reaction force at end of forks}$$

$$R_{nf} = 12.50 \text{ kips}$$

### 4.0 Calculate the required sections for beam and forks based on moment.

$$S_{x1} := \frac{|M_n(a)|}{f_y}$$

$$S_{x1} = 6.34 \text{ in}^3$$

$$S_{x2} := \frac{M_f}{f_y}$$

$$S_x = 13.98 \text{ in}^3 \quad \text{Use a HSS20x8x5/16 at 48.8lbs/ft. and } S_x = 78.6 \text{ in}^3 \text{ and } I_x = 786 \text{ in}^4$$

$$I_x := 786 \text{ in}^4$$

### 5.0 Calculate the deflections

Table in the horizontal position

$$\Delta_{\text{end}} := \frac{q_h \cdot a}{24 \cdot E_s \cdot I_x} \cdot [3 \cdot a^2 \cdot (a + 2 \cdot b) - b^3] \quad \text{Deflection at end of beam in the horizontal position}$$

$$\Delta_{\text{end}} = -0.09 \text{ in}$$

$$\Delta_{\text{mid}} := \frac{q_h \cdot b^2}{384 \cdot E_s \cdot I_x} \cdot (5 \cdot b^2 - 24 \cdot a^2)$$

$$\Delta_{\text{mid}} = 0.17 \text{ in}$$

Deflection of Forks when Table is in the Vertical Position

$$\Delta_f := \frac{q_c \cdot d^2 \cdot a \cdot b}{6 E_s \cdot I_x} + \frac{q_c \cdot d^2 \cdot a^2}{6 E_s \cdot I_x}$$

$$\Delta_f = 0.51 \text{ in}$$

Horizontal Deflection of fork

$$\Delta_{fv} := \frac{q_c \cdot d^4}{8 \cdot E_s \cdot I_x} + \frac{q_c \cdot d^3 \cdot b}{6 E_s \cdot I_x} + \frac{q_c \cdot d^3 \cdot a}{2 \cdot E_s \cdot I_x}$$

$$\Delta_{fv} = 0.51 \text{ in}$$

Vertical Deflection of Tip of Fork

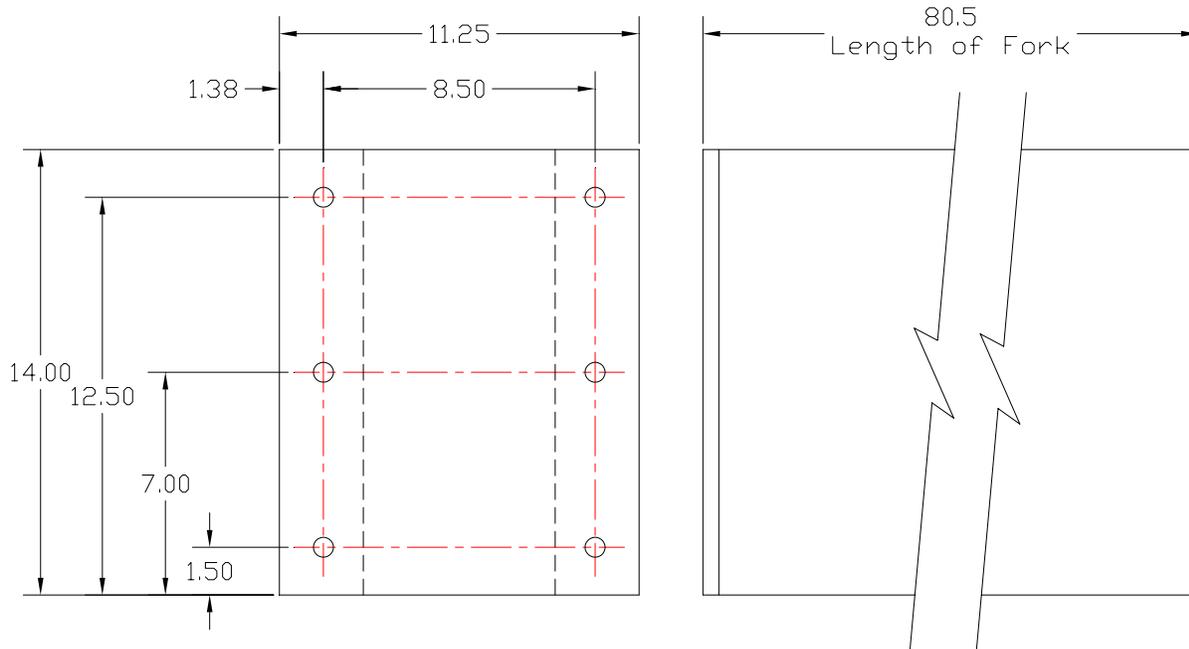
$$\Delta_{tv} := \frac{q_c \cdot d^2 \cdot b^2}{32 \cdot E_s \cdot I_x}$$

$$\Delta_{tv} = 0.22 \text{ in}$$

Horizontal Deflection of the table between supports

### 6.0 Calculations on Fork Design.

The forks will be constructed from rectangular tubes that are 14x6x3/8. The tubes are welded to a 1/2" thick plate which is 11.25" wide and 14" long. This plate has six holes for bolting 5/8" diameter bolts to the block raiser surface. The stresses in the tube, the stresses in the welds of the tube to the plate and the stresses in the bolts have to be calculated. The welds and bolts are subjected to a bending moment as well as a shearing force.



**6.1 Stresses in the Rectangular Tube of Fork**

$S_{xf} := 45.3 \text{ in}^3$                       Inertia of Tube

$\sigma_f := \frac{M_f}{S_{xf}}$                       Maximum Tensile Stress at End of Tube

$\sigma_f = 11.11 \text{ ksi}$

**6.2 Stress in Welds Attaching Tube to 1/2" Plate**

$\underline{d} := 14 \text{ in}$                       Length of vertical weld

$\underline{b} := 6 \text{ in}$                       Length of horizontal weld

$S_x := b \cdot d + \frac{d^2}{3}$                       Section modulus of weld

$S_x = 149.33 \text{ in}^2$

$\mu_u := 1.4 \cdot M_f$                        $M_f = 41.95 \text{ kips} \cdot \text{ft}$                       Factored moment acting on weld

$$R_v := \frac{1.4 \cdot R_{nf}}{2 \cdot d} \quad R_v = 0.63 \frac{\text{kips}}{\text{in}} \quad \text{Factored shear load on weld per unit length of weld (ignore contribution from top/bottom welds)}$$

$$R_t := \frac{M_u}{S_x} \quad R_t = 4.72 \frac{\text{kips}}{\text{in}} \quad \text{Factored tensile load on weld per unit length of weld}$$

$$R_u := \sqrt{R_v^2 + R_t^2} \quad R_u = 4.76 \frac{\text{kips}}{\text{in}} \quad \text{Factored combined loading on weld per unit length of weld}$$

$$\phi_w := 0.75 \quad \text{Strength reduction factor of weld}$$

$$F_{exx} := 70 \text{ksi} \quad \text{Yield strength of weld material}$$

$$t_w := \frac{R_u}{\phi_w \cdot 0.707 \cdot (0.60 F_{exx})} \quad t_w = 0.21 \text{ in} \quad \text{Required Weld Size}$$

Use  $t_w=0.375$ " to match the thickness of the tube wall.

For the commonly used grades of steel, only two electrodes need to be considered:

E70XX electrodes with steels that have a yield stress of less than 60ksi

E80XX electrodes with steels that have a yield stress of 60ksi or 65ksi

### 6.3 Analysis of Bolted Connection on Fork

Define Inputs:

$$F_u := 50000 \text{psi} \quad \text{Tensile Strength of Plate Material}$$

$$F_y := 36 \text{ksi} \quad \text{Yield Strength of Plate Material}$$

$$F_{ub} := 120 \text{ksi} \quad \text{Tensile Strength of A325 Bolt Material}$$

$$n := 13 \quad \text{Number of Threads per Inch}$$

$$N := 6 \quad \text{Total Number of Bolts}$$

$$d_b := 0.875 \text{in} \quad \text{Bolt Nominal Diameter}$$

$$d := d_b + \frac{1}{16} \text{in} \quad \text{Clearance hole in plate for bolt}$$

$$m := 1 \quad \text{Number of Shear Planes}$$

$$t := 0.625 \text{in} \quad \text{Thickness of Plate}$$

$$L_e := 1.75 \text{in} \quad \text{Distance along the line of force from edge of the connected part to the center of hole}$$

$$L := 12.25 \text{in} \quad \text{Length of the connection in the direction of shear from the edge of the plate to the last hole}$$

$n_3 := 3$	Number of holes in a line in the direction of the shear load
$h := 1.375\text{in}$	Distance from the edge of the plate to the center of the holes perpendicular to the direction of shear
$\phi_s := 0.75$	Strength reduction factor for shear
$\phi_f := 0.75$	Strength reduction factor for fracture
$\phi_b := 0.75$	Strength reduction factor for bearing
$T_b := 28\text{kips}$	Initial Bolt pre-stress used for slip critical connections.

Calculate the factored tensile force in the bolts.

Assume moment is generated about the centroid of the bolts. Calculate the maximum tensile force in top bolt.

$$P_u := \frac{1.4M_f}{2 \cdot (10.5\text{in})} \quad \text{Maximum tensile load in bolt}$$

$$P_u = 33.56 \text{ kips}$$

Calculate the shear load per bolt

$$V_u := \frac{1.4 \cdot R_{nf}}{N}$$

$$V_u = 2.92 \text{ kips} \quad \text{Factored shear force per bolt.}$$

### Calculation of Areas

$$A_b := \frac{\pi d_b^2}{4} \quad \text{Gross Cross-Sectional Area of One Bolt}$$

$$A_b = 0.60 \text{ in}^2$$

$$A_n := 0.785 \cdot \left( d_b - \frac{0.9743\text{in}}{n} \right)^2 \quad \text{Net Cross-Sectional Area of One Bolt}$$

$$A_n = 0.50 \text{ in}^2$$

### Shear Strength through threads of bolt

$$\phi V_n := \phi_s \cdot (0.40 \cdot F_{ub}) \cdot m \cdot A_b$$

$$\phi V_n = 21.6 \text{ kips}$$

### Combined Shear and Tension Loading on Bolts

LRFD Table J3.5 lists the design tension stress limit,  $\phi F'_{ut}$ , in the presence of the factored shear stress  $f_{uv}$ .

Stress variables are  $F$ , and  $f$  and actual load variables are  $R$ . The small  $f$  variable represents the stress due to the factored (applied) loads.

$$C := 1.3$$

$C$  is a constant defined by LRFD to obtain a straight interaction line.

$$f_{uv} := \frac{V_u}{A_b} \quad f_{uv} = 4850.44 \text{ psi}$$

$$\phi F'_{ut} := \phi f \cdot [(0.75 \cdot F_{ub} \cdot C) - (2.5 \cdot f_{uv})]$$

Allowable tensile stress when threads are not in shear plane.

$$\phi F'_{ut} = 78.66 \text{ ksi}$$

$$\phi R_n := \begin{cases} [\phi F'_{ut} \cdot (0.75 \cdot A_b)] & \text{if } \phi F'_{ut} \cdot (0.75 \cdot A_b) < \phi f \cdot F_{ub} \cdot (0.75 \cdot A_b) \\ [\phi f \cdot F_{ub} \cdot (0.75 \cdot A_b)] & \text{otherwise} \end{cases}$$

$$\phi R_n = 35.47 \text{ kips}$$

Maximum Allowable Tensile Force per Bolt

This is less than  $P_u$  (factored tensile load on bolt) so ok.

The value of  $\phi F'_{ut}$  has to be less than the maximum value listed in Table J3.5 in LRFD

The tensile is reduced 75% for the root area, 0.8 for the affect of the connection length  
Shear strength equals  $0.62 F_{ub}$   
( $.75 \cdot .8 \cdot .62 = 0.40$ )

### Bearing Strength of Plate Material

Bearing Strength of the material is dependent upon the amount of hole deformation that is acceptable and the hole spacing.

$$\phi V_n := \phi b \cdot 2.4 \cdot d_b \cdot t \cdot F_u$$

$$\phi V_n = 49.2 \text{ kips}$$

Applies in usual conditions based on deformation limits for the hole. This equation applies for all holse except long slotted holes where the end distance  $L_e$  is at least 1.5 times the bolt diameter, and the center to center spacing  $s$  is at least  $3d$ , and there are two or more bolts in the line of force.

$$\phi V_n := \phi b \cdot L_e \cdot t \cdot F_u$$

$$\phi V_n = 41.0 \text{ kips}$$

Strength limit state for the bolt nearest the edge, according to LRFD formulas J3-1b, J3-2a and J3-2c

Traditionally the center to center spacing of bolts is a minimum of 2 2/3 diameters and Le is a minimum of 2.67 times the bolt diameter

**Minimum Spacing of Bolts**

$$s := \frac{V_u}{\phi_b \cdot F_u \cdot t} + \frac{d_b}{2}$$

s is the minimum spacing between bolts and should be more than the calculated value. LRFD recommends 3 bolt diameters and shall not be less than 2 2/3 diameters

$$s = 0.56 \text{ in}$$

$$L_{min} := \frac{V_u}{\phi_b \cdot F_u \cdot t}$$

L is the calculated minimum end distance in the direction of the transmitted force.

$$L_{min} = 0.12 \text{ in}$$

**Calculate Block Shear in Plate**

Block shear Failure can occur in two methods: First, by shear yield and tension fracture. Second, shear fracture and tension yield.

$$A_{gv} := t \cdot L$$

A<sub>gv</sub> is the gross shear area not accounting for holes along the length of the connection. This is in the direction of the tension force.

$$A_{nv} := A_{gv} - [(n_3 - .5) \cdot d \cdot t]$$

A<sub>nv</sub> is the net shear area that subtracts the hole area

$$A_{nv} = 6.19 \text{ in}^2$$

$$A_{gt} := h \cdot t$$

A<sub>gt</sub> is the gross tension area that does not account for the holes. This area is in the direction perpendicular to the direction of tension loading

$$A_{nt} := A_{gt} - \frac{d \cdot t}{2}$$

A<sub>nt</sub> is the net tension area that subtracts the hole area

$$\phi R_u := \phi_f \cdot [(.6 \cdot F_u \cdot A_{nv}) + (F_u \cdot A_{nt})]$$

$$\phi R_u = 160546.87 \text{ lbf}$$

Upper Limit AISC

$$\phi R_1 := \begin{cases} \phi_f \cdot [(.6 \cdot F_y \cdot A_{gv}) + (F_u \cdot A_{nt})] & \text{if } \phi_f \cdot [(.6 \cdot F_y \cdot A_{gv}) + (F_u \cdot A_{nt})] \leq \phi R_u \\ \phi R_u & \text{otherwise} \end{cases}$$

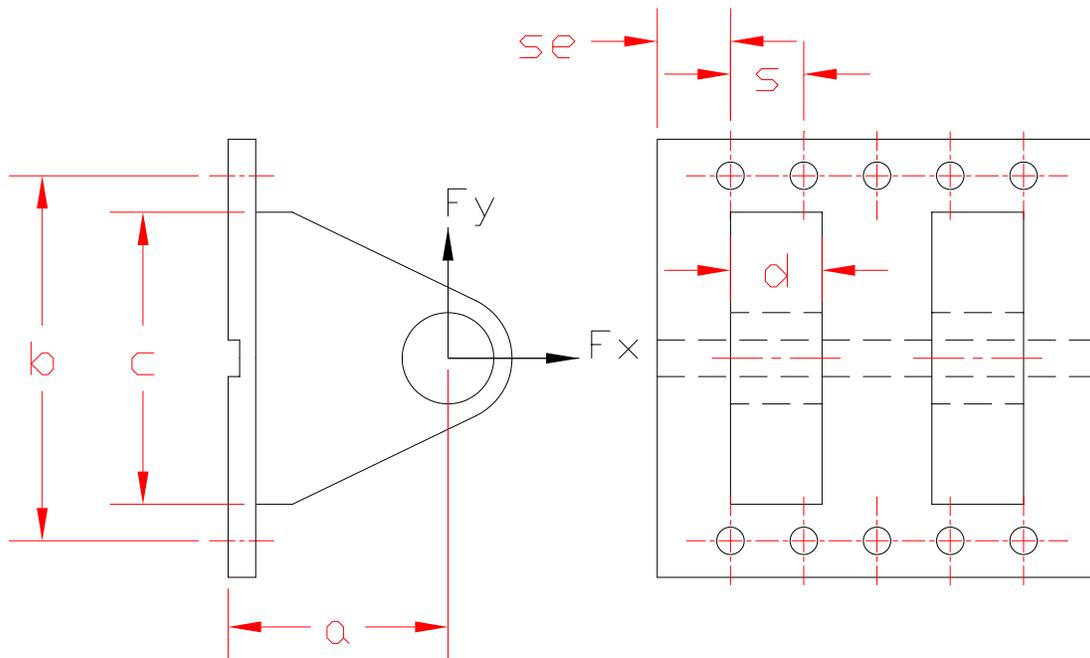
$$\phi R_2 := \begin{cases} \phi_f \cdot [(.6 \cdot F_u \cdot A_{nv}) + (F_y \cdot A_{gt})] & \text{if } \phi_f \cdot [(.6 \cdot F_u \cdot A_{nv}) + (F_y \cdot A_{gt})] \leq \phi R_u \\ \phi R_u & \text{otherwise} \end{cases}$$

$$\phi R_n := \begin{cases} \phi R_1 & \text{if } F_u \cdot A_{nt} \geq .6 \cdot F_u \cdot A_{nv} \\ \phi R_2 & \text{otherwise} \end{cases}$$

$\phi R_n = 160.55$  kips

### 7.0 Calculation on the Bearing Support Plate

The bearing support plate geometry is shown in the figure below. This plate supports the bearing which allows the BR to rotate. The welds between the gussets housing the bearing and the main plate must be examined, the bolts attaching the Bearing Support Plate to the Table Top and the keyway which carries the shear ( $F_y$ ) force. The maximum loading on this plate occurs when the BR is in the vertical position because it must support 1/2 of the total weight of the block and table. This plate is designed so that the shearing force,  $F_y$ , is carried entirely through a key and that the bolts must only resist the bending moment caused by the application of the force a distance "a" from the bottom of the plate.



### 7.1 Loads on Bearing Plate

$F_y := 1.4 \cdot 231171.7 \text{ lbf}$

Factored shearing force on bearing with BR in Vertical position from Excel spreadsheet calculation of BR forces.

$F_y = 323.64 \text{ kips}$

$F_x := 1.4 \cdot 173631 \text{ lbf}$

Factored normal force on bearing with BR in Vertical position from Excel Spreadsheet calculation of BR forces

### 7.2 Calculations on Keyway

$f_y := 36 \text{ ksi}$

$t_k := 0.50\text{in}$  Depth of keyway

$w := 1.0\text{in}$  Width of keyway

$L_k := 24\text{in}$  Length of key

$\sigma_b := \frac{F_y}{t_k \cdot L_k}$   $\sigma_b = 26.97\text{ ksi}$  Bearing stress on Key -- less than  $f_y$  so ok

$\tau_k := \frac{F_y}{L_k \cdot w}$   $\tau_k = 13.49\text{ ksi}$  Shear stress through key -- less than  $0.6f_y$  so ok

### 7.3 Calculation of Welds Between Bearing Gusset and Plate.

$c := 28\text{in}$  Length of vertical weld

$d := 5\text{in}$  Length of horizontal weld

$a := 17\text{in}$  Distance from bearing center to welds

$S_x := c \cdot d + \frac{c^2}{3}$  Section modulus of weld

$S_x = 401.33\text{ in}^2$

$M_u := \frac{F_y \cdot a}{2}$   $M_f = 41.95\text{ kips} \cdot \text{ft}$  Factored moment acting on weld

$R_v := \frac{F_y}{4 \cdot c}$   $R_v = 2.89 \frac{\text{kips}}{\text{in}}$  Factored shear load on weld per unit length of weld (ignore contribution from top/bottom welds)

$R_t := \frac{M_u}{S_x}$   $R_t = 6.85 \frac{\text{kips}}{\text{in}}$  Factored tensile load on weld per unit length of weld

$R_u := \sqrt{R_v^2 + R_t^2}$   $R_u = 7.44 \frac{\text{kips}}{\text{in}}$  Factored combined loading on weld per unit length of weld

$\phi_w := 0.75$  Strength reduction factor of weld

$F_{exx} := 70\text{ksi}$  Yield strength of weld material

$t_w := \frac{R_u}{\phi_w \cdot 0.707 \cdot (0.60F_{exx})}$   $t_w = 0.33\text{ in}$  Required Weld Size

Use  $t_w=0.5$ :

#### 7.4 Calculation of Required Bolts

$N := 6$  Number of bolts per row

$d_b := 0.875 \text{ in}$  Diameter of Bolts

$F_{ub} := 120 \text{ ksi}$  Strength of A325 Bolt Material

$A_b := \frac{\pi d_b^2}{4}$  Gross Cross-Sectional Area of One Bolt

$A_b = 0.60 \text{ in}^2$

$b := 38 \text{ in}$  Distance between rows of bolts

$R_u := \frac{F_y \cdot a}{b \cdot N} + \frac{F_x}{2 \cdot N}$  Tensile Force per bolt

$R_u = 26.16 \text{ kips}$

$\phi R_n := \phi f \cdot F_{ub} \cdot (0.75 \cdot A_b)$  Bolt Strength

$\phi R_n = 40.59 \text{ kips}$  Since  $\phi R_n$  is greater than  $R_u$  the strength of the bolts is ok.

#### 8.0 Calculations on the Telescoping Tube.

Inputs

$P := 2000 \text{ psi}$  Working Pressure of cylinder

$f_y := 50 \text{ ksi}$  Yield stress of cylinder material

$F_1 := 75 \text{ kips}$  Extension force

$F_2 := 25 \text{ kips}$  Retraction Force

$SF_p := 3.0$  Safety factor to resist pressure

$SF_b := 5.0$  Safety factor to resist buckling

$L_t := 9 \text{ ft}$  Length of Telescoping Tube Section

#### 8.1 Sizing the smallest section

$Do_1 := \sqrt{\frac{4 \cdot F_1}{\pi \cdot P}}$   $Do_1 = 6.91 \text{ in}$  Required Outer Diameter for F1

Calculate the required inner diameter

$$Di1 := \sqrt{Do1^2 - \frac{4 \cdot F2}{\pi \cdot P}} \quad Di1 = 5.64 \text{ in}$$

Calculate required wall thickness:

$$t1 := \frac{P \cdot Di1 \cdot SFp}{2 \cdot fy + 2 \cdot P \cdot SFp} \quad t1 = 0.30 \text{ in} \quad \text{Required wall thickness of inner section}$$

$$t1 := 0.5 \text{ in}$$

Check buckling of a tube that is  $Lt$  long and has a diameter of  $Di1$  and thickness of  $t1$

$$I := \pi (Do1 - Di1)^3 \cdot t1 \quad I = 3.20 \text{ in}^4 \quad \text{Moment of Inertia of tube}$$

$$Pcr := \frac{\pi^2 \cdot Es \cdot I}{Lt^2} \quad Pcr = 78.58 \text{ kips} \quad \text{Critical buckling Load}$$

## 8.2 Calculation on wall thicknesses/diameters of sections

$$t2 := \frac{P \cdot Do1 \cdot SFp}{2 \cdot fy} \quad t2 = 0.41 \text{ in} \quad \text{Required wall thickness to resist internal pressure}$$

$$Di2 := 2 \cdot t2 + Do1 \quad Di2 = 7.74 \text{ in} \quad \text{Inner diameter of 2nd section}$$

$$Do2 := \sqrt{\frac{4 \cdot F2}{\pi \cdot P} + Di2^2} \quad Do2 = 8.71 \text{ in} \quad \text{Required outer diameter to provide } F2$$

---

$$t3 := \frac{P \cdot Do2 \cdot SFp}{2 \cdot fy} \quad t3 = 0.52 \text{ in} \quad \text{Required wall thickness to resist internal pressure}$$

$$Di3 := 2 \cdot t3 + Do2 \quad Di3 = 9.75 \text{ in}$$

$$Do3 := \sqrt{Di3^2 + \frac{4 \cdot F2}{\pi \cdot P}} \quad Do3 = 10.54 \text{ in}$$

---

$$t4 := \frac{P \cdot Do3 \cdot SFp}{2 \cdot fy} \quad t4 = 0.63 \text{ in}$$

$$Di4 := 2 \cdot t4 + Do3 \quad Di4 = 11.80 \text{ in}$$

$$Do4 := \sqrt{Di4^2 + \frac{4 \cdot F2}{\pi \cdot P}} \quad Do4 = 12.46 \text{ in}$$

