



Polarized Positrons

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ILC Positron Source Group Meeting, ANL

Outline

ILC physics after LHC: need polarized positrons

Current status: $P_{e+} \approx 30\%$ (baseline design)

- utilize the 30% for physics
- helicity reversal

Status G4 with polarization

Polarimetry at low energies

- Update of Bhabha polarimeter studies
- Compton polarimetry after DR?

Summary and outlook

Physics between 200 GeV and 500 GeV

Luminosity: Year 1-4: $L_{\text{int}} = 500 \text{ fb}^{-1}$

1. year 10% $\rightarrow L_{\text{int}} \approx 50 \text{ fb}^{-1}$

2. year 30% $\rightarrow L_{\text{int}} \approx 150 \text{ fb}^{-1}$

3. Year 60% $\rightarrow L_{\text{int}} \approx 300 \text{ fb}^{-1}$

4. year 100% $\rightarrow L_{\text{int}} \approx 500 \text{ fb}^{-1}$

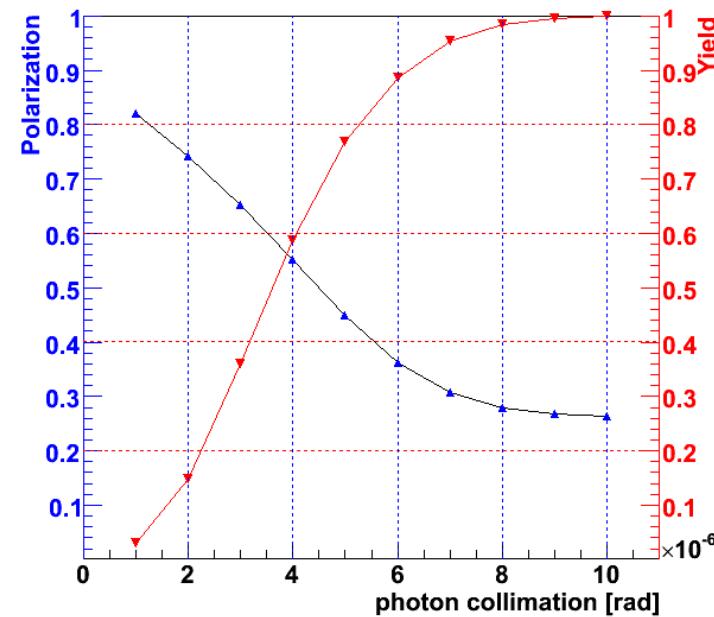
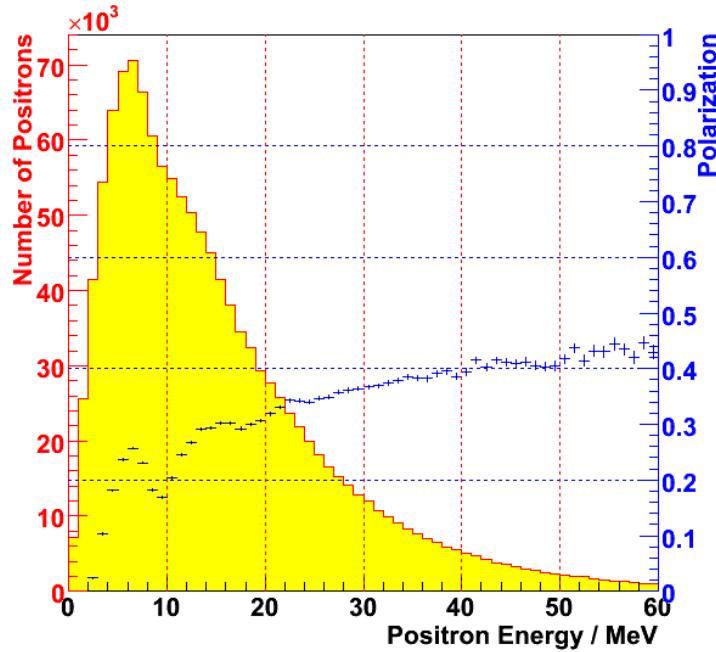
$\rightarrow ee \rightarrow HZ$	at 350 GeV ($mH \approx 120 \text{ GeV}$)	few 10^4
$ee \rightarrow tt$	at 350 GeV	10^5
$ee \rightarrow qq (\mu\mu)$	at 500 GeV	$5 \cdot 10^5 (1 \cdot 10^5)$
$ee \rightarrow WW$	at 500 GeV	10^6

\rightarrow statistical uncertainties at per-mille level !!

Uncertainties: $\Delta\sigma \propto \frac{1}{\sqrt{N}} \oplus \frac{\Delta L}{L} \oplus \frac{\Delta P}{P}$  $\longrightarrow O(10^{-3})$

RDR: helical undulator → ~30% e+ polarization

e+ spectrum



photon beam: distance undulator center ↔ target ~ 500m

s-channel cross sections with pol beams

Perform 4 independent measurements (s-channel vector exch.)

$$\left. \begin{aligned} \sigma_{++} &= \sigma_u \left[1 - \mathbf{P}_{e^+} \mathbf{P}_{e^-} + A_{LR} (+\mathbf{P}_{e^+} - \mathbf{P}_{e^-}) \right] \\ \sigma_{--} &= \sigma_u \left[1 - \mathbf{P}_{e^+} \mathbf{P}_{e^-} + A_{LR} (-\mathbf{P}_{e^+} + \mathbf{P}_{e^-}) \right] \end{aligned} \right\}$$

=0 (SM) if both beams
100% polarized

$$\left. \begin{aligned} \sigma_{-+} &= \sigma_u \left[1 + \mathbf{P}_{e^+} \mathbf{P}_{e^-} + A_{LR} (-\mathbf{P}_{e^+} - \mathbf{P}_{e^-}) \right] \\ \sigma_{+-} &= \sigma_u \left[1 + \mathbf{P}_{e^+} \mathbf{P}_{e^-} + A_{LR} (+\mathbf{P}_{e^+} + \mathbf{P}_{e^-}) \right] \end{aligned} \right\}$$

SLC: σ_{-0} and σ_{+0} used for A_{LR} measurement

$$\begin{aligned} ILC: \quad A_{LR} &= \frac{\sigma_{-+} - \sigma_{+-}}{\sigma_{-+} + \sigma_{+-}} \cdot \frac{1 + \mathbf{P}_{e^-} \mathbf{P}_{e^+}}{\mathbf{P}_{e^-} + \mathbf{P}_{e^+}} \\ &= \frac{\sigma_{-+} - \sigma_{+-}}{\sigma_{-+} + \sigma_{+-}} \cdot \frac{1}{\mathbf{P}_{eff}} \end{aligned}$$

$$A_{LR} = \frac{\sigma_{-0} - \sigma_{+0}}{\sigma_{-0} + \sigma_{+0}} \cdot \frac{1}{\mathbf{P}_{e^-}}$$

Error propagation
 $\rightarrow \Delta \mathbf{P}_{eff} / \mathbf{P}_{eff} < \Delta \mathbf{P}_{e+,e-} / \mathbf{P}_{e+,e-}$

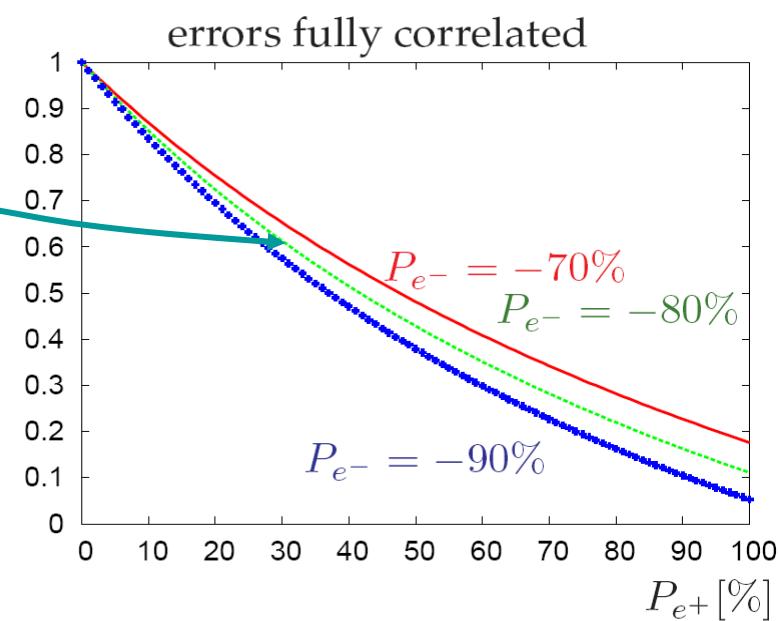
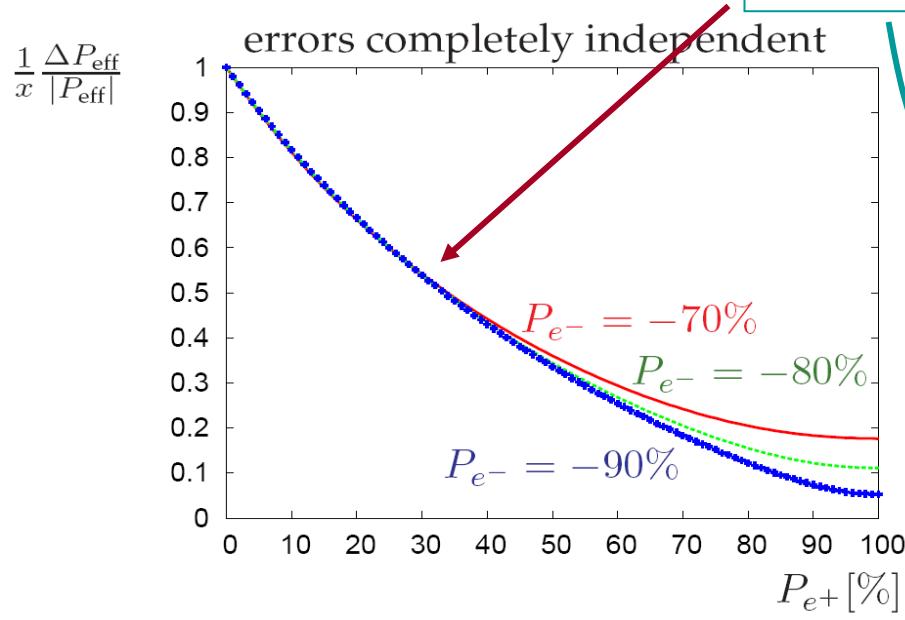
Cross section enhancement $\sim (1 + \mathbf{P}_{e^-} \mathbf{P}_{e^+})$

- Decrease of error on $P_{\text{eff}} = (P_{e^-} + P_{e^+}) / (1 + P_{e^-} P_{e^+})$

$$\frac{\Delta P_{\text{eff}}}{P_{\text{eff}}} = x \frac{\sqrt{(1 - P_{e^+}^2)^2 P_{e^-}^2 + (1 - P_{e^-}^2)^2 P_{e^+}^2}}{(P_{e^+} + P_{e^-})(1 + P_{e^+} P_{e^-})}$$

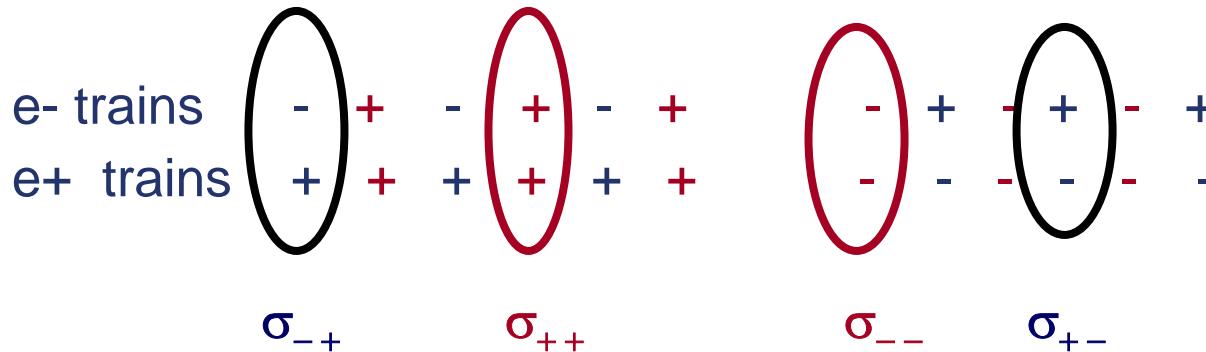
$$x \equiv \frac{\Delta P_{e^-}}{P_{e^-}} = \frac{\Delta P_{e^+}}{P_{e^+}}$$

30%: Improvement by factor 2 (1.5)



e+ Helicity Reversal

e+ helicity flip less frequent than e- helicity reversal ?!



50% spent to ‘inefficient’ helicity pairing σ_{--} and σ_{++} →

- gain due to xs enhancement for J=1 processes with e+ pol is lost
- Improvement of ΔP_{eff} remains only for quite frequent reversal – if systematic errors known and small (intensity/polarisation tolerances)
- Corresponds to ‘slow’ Blondel scheme ⇔ determine P and A_{LR} simultaneously

$$\frac{\sigma_{-+} + \sigma_{--} - \sigma_{++} - \sigma_{+-}}{\sigma_{-+} + \sigma_{--} + \sigma_{++} + \sigma_{+-}} = P_{e^-} A_{LR}$$

$$\frac{\sigma_{+-} + \sigma_{--} - \sigma_{++} - \sigma_{-+}}{\sigma_{+-} + \sigma_{--} + \sigma_{++} + \sigma_{-+}} = P_{e^+} A_{LR}$$

Polarization is an issue:

- The 30% positron polarization has to be brought to IP and used for physics (rotators, helicity reversal, design optimization for e+ pol)
- small polarization → no physics gain but more complicated measurement/analysis
- Collaboration with other groups necessary
- Spin tracking studies necessary



Geant4 with polarized processes

- Polarization has to be taken into account for
 - Pair-production
 - Bremsstrahlung
 - Compton scattering
 - Moller/Bhabha scattering
 - Positron annihilation into 2 photons
- Included since Geant4 release 8.2 (Dec 06)
 - Main focus: longitudinal (or circular) polarization (extension to transversal is foreseen)
 - Energy range of interest: MeV ... ~5 GeV
- Applications:
 - Polarization transfer (target, E166)
 - Polarimetry (Bhabha/Moller, Compton transmission – e.g. E166)
 - ILC polarized positron source

Authors: A. Schälicke, K. Laihem, P. Starovoitov

Official Geant4 release



first appeared in version 8.2

- ▶ December 15th 2006

available at

- ▶ <http://geant4.web.cern.ch/>

includes

- ▶ polarised QED processes
- ▶ documentation available in
Geant4 Physics Reference Manual
- ▶ usage illustrated in a simple example
examples/extended/polarisation/Pol01/

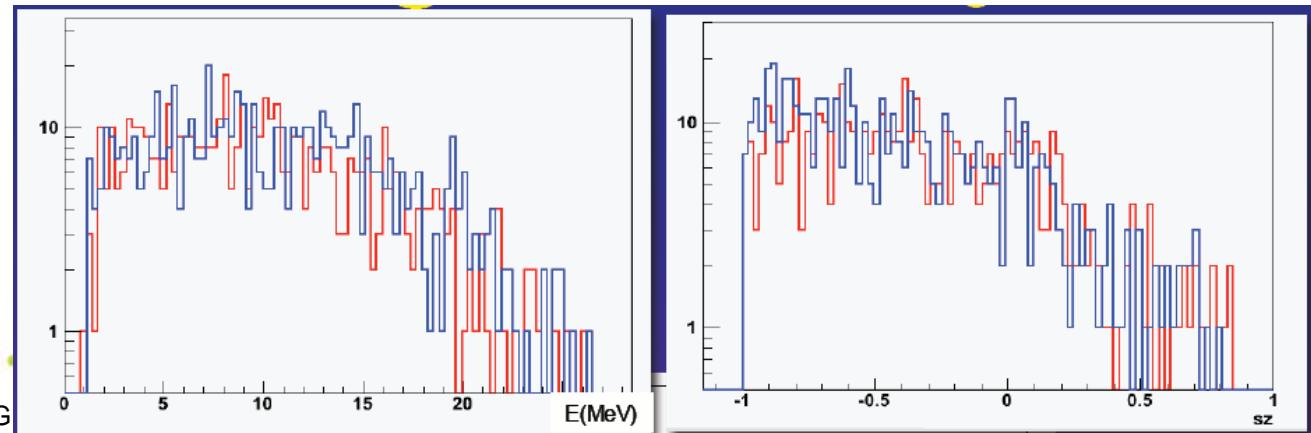
11 Polarized Electron/Positron/Gamma Incident

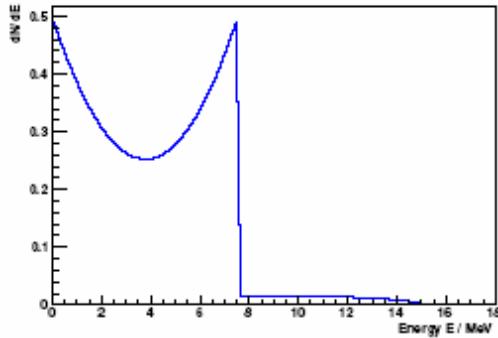
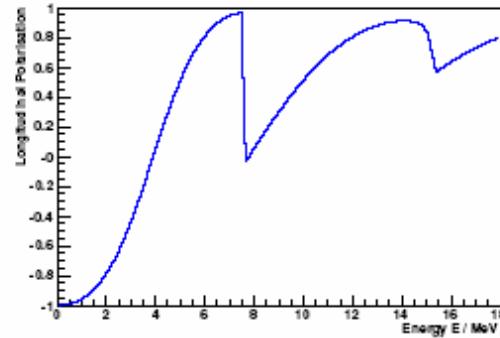
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Verification of ‘Polarized G4’

- Comparison other programs and with experiments
- Comparison with Whizard/O’mega:
 - Checked: pol transfer, asymmetries (Compton, Moller/Bhabha, annihilation)
 - Missing: interaction with nuclei (e.g. pair production)
- Comparisons with EGS
 - EGS: polarization transfer
 - No depolarization via ionization, no target polarization
 - Good agreement for pol transfer to high energetic e+
 - Compton source: tests done/ongoing by O. Dadoun:

e+ @ exit of target
EGS
Geant4
(Dadoun, Posipol 07)

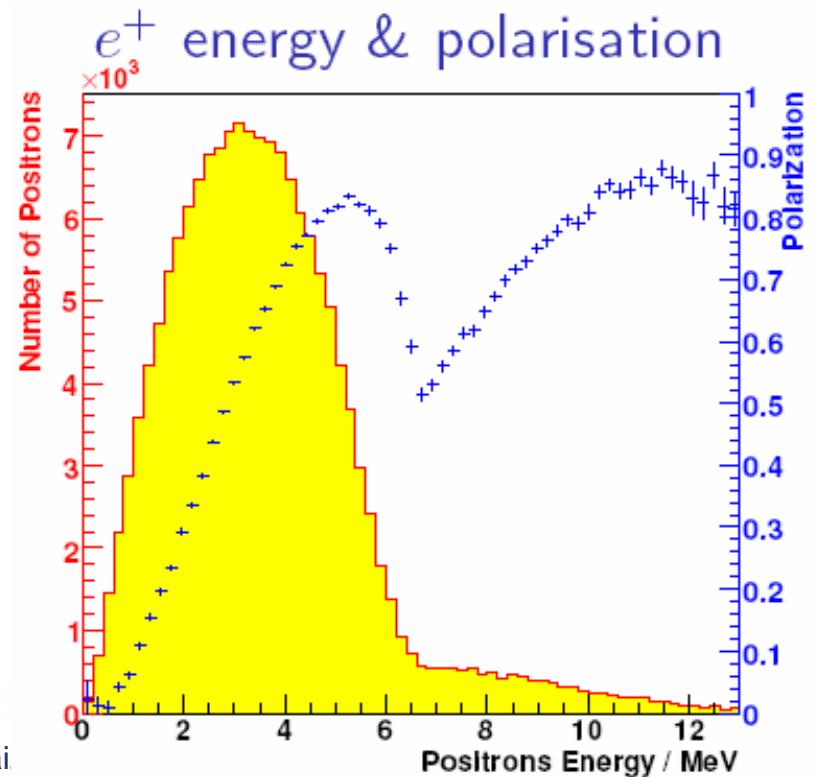


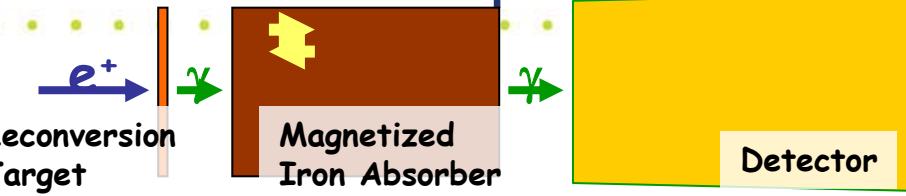
γ energy γ polarisation

Input: energy and polarization of photons generated by helical undulator

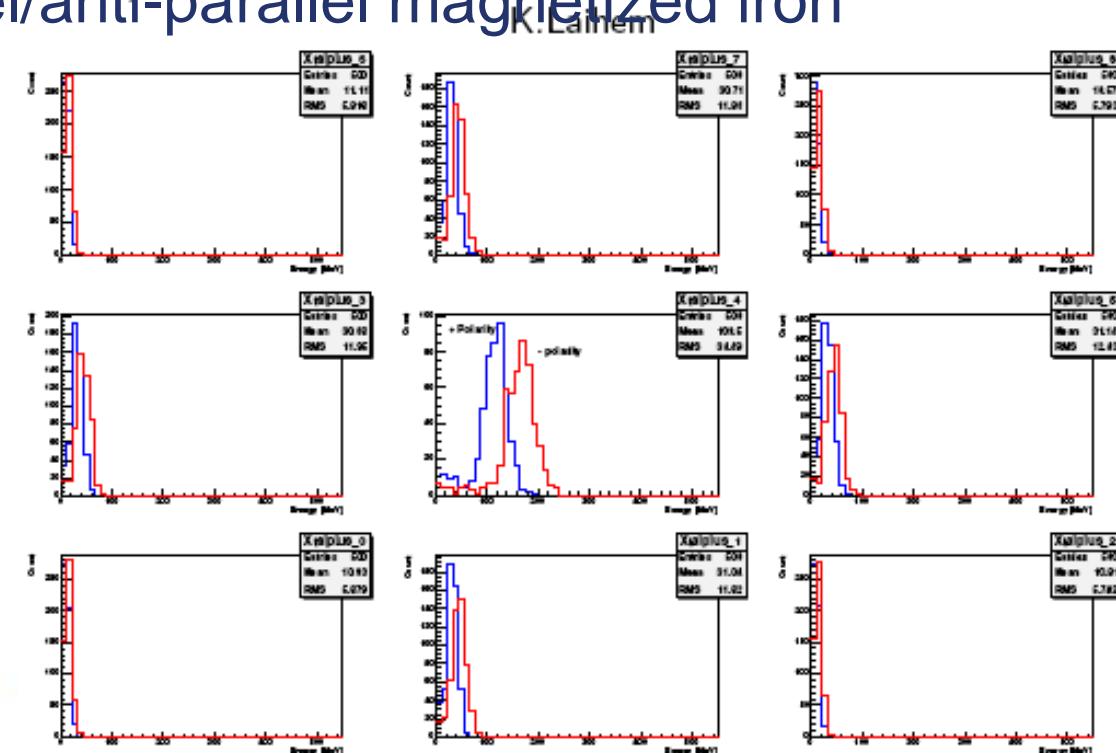
Simulation of

- Conversion into $e^+ e^-$ pairs in thin W target,
- polarization transfer to high energetic leptons





- Reconversion of e^+ to polarized photons (bremsstrahlung, annihilation)
- Transmission of photons through magnetized iron
- Polarization dependent Compton cross section → asymmetry for parallel/anti-parallel magnetized iron
- Measurement of transmission in CsI calorimeter (3x3 crystals)



→ Simulation of
analyzing power
for E166



ILC polarized positrons & Geant4

- ILC positron source studies:
**Target, spin transport in capture section
(see Andriy's talk)**
- Positron polarimeter @ source
 - **Bhabha polarimeter design studies**

Ongoing work / Plans:

- Implementation of T-BMT for spin tracking
- implementation of transverse spin polarization
- Validation



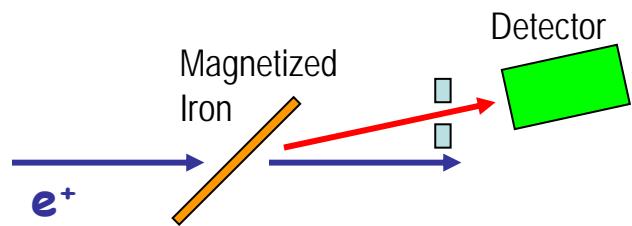
e+ polarimeter at/near the source

- Requirements:
 - Suitable for energy range
 - Suitable for large positron beam size
 - Fast
 - Non-destructive
 - Accuracy O(few %)
- Possibilities:
 - Bhabha polarimeter (125-500 MeV)
 - Compton – after DR (beamsize!)
- People:
 - DESY/HUB: R. Dollan, T. Lohse, S. Riemann, A. Schälicke, P. Schuler, A. Ushakov
 - Minsk: P. Starovoitov, Tel Aviv U: G. Alexander

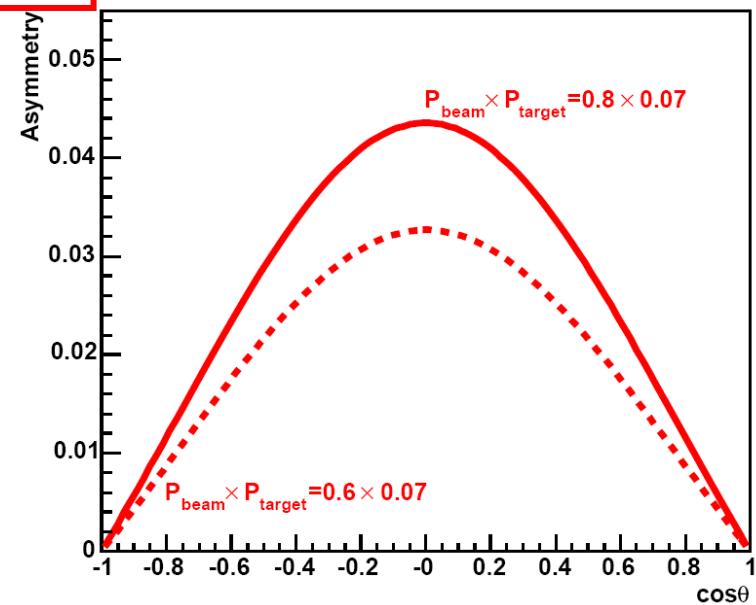
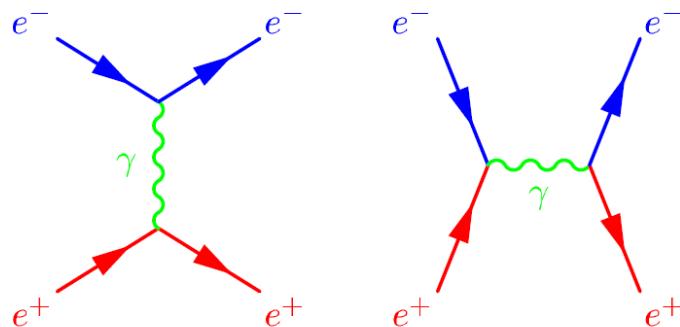
Bhabha Polarimetry

- As Møller polarimeter already widely used
- Cross section:

$$\frac{d\sigma}{d\Omega} = r_0^2 \frac{(1+\cos\theta)^2}{16\gamma^2 \sin^4\theta} \left[(9 + 6\cos^2\theta + \cos^4\theta) - \boxed{\mathbf{P}_{e^+} \mathbf{P}_{e^-}} (7 - 6\cos^2\theta - \cos^4\theta) \right]$$



- e+ and e- must be polarized
- maximal asymmetry at 90°(CMS)
~ 7/9 ≈ 78 %



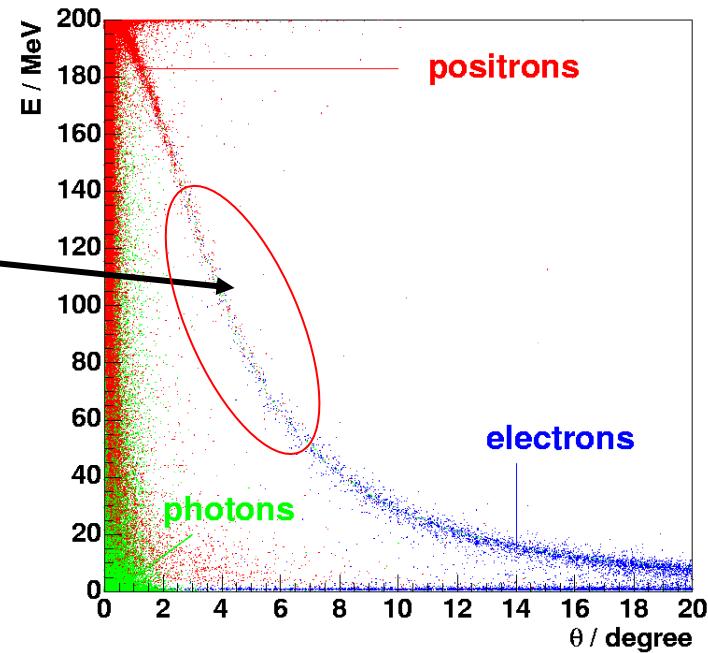
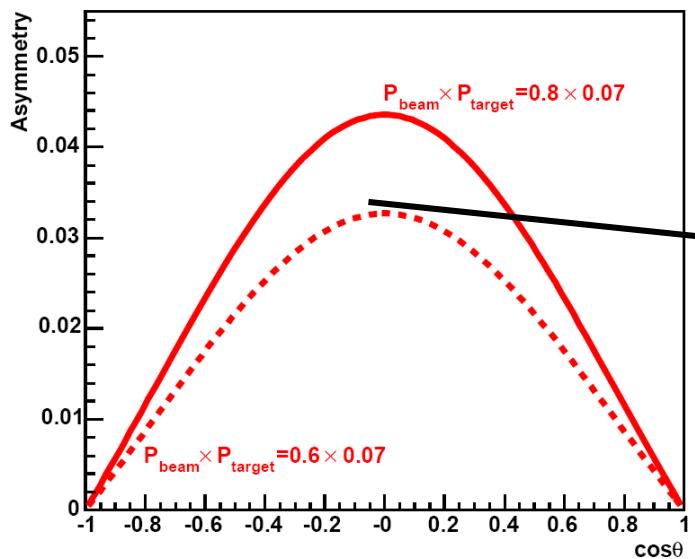
Example: $P_{e^+} = 80\%$, $P_{e^-} = 7\%$ $A_{max} \sim 4.4\%$

Bhabha Polarimetry

Centre-of-mass system



Lab system



Working point:

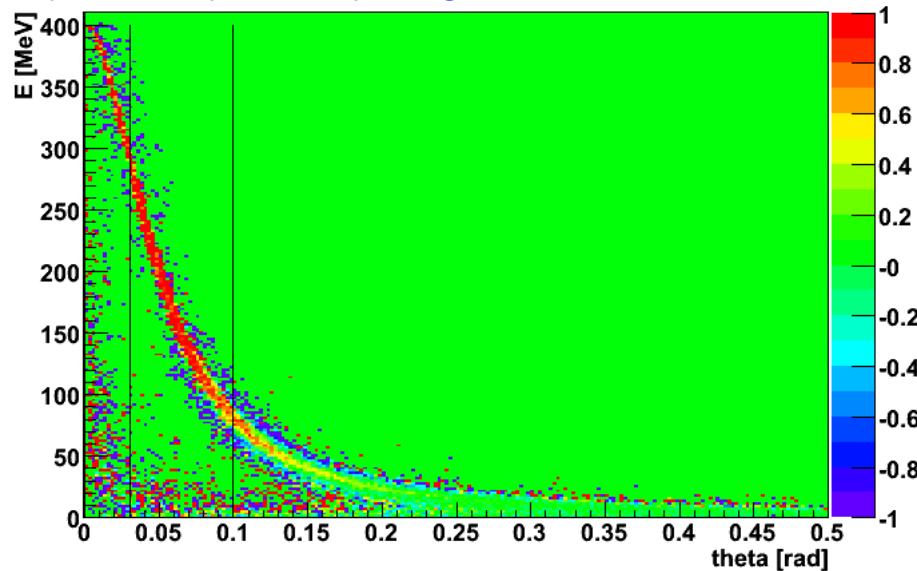
- After pre-acceleration
- First studies done for

(125 MeV –) 400 MeV
200 MeV, 400 MeV

Example: e⁻ distribution and e⁻ asymmetry

- 30 μm magnetized Fe-Foil
- E_{beam} : 400 MeV (10 % spread)
- Ang. Spread: 0.5°
- 100% e+ and e- polarisation assumed

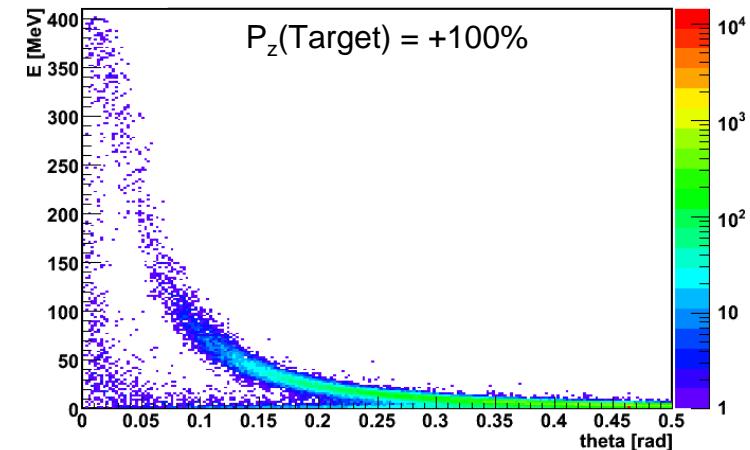
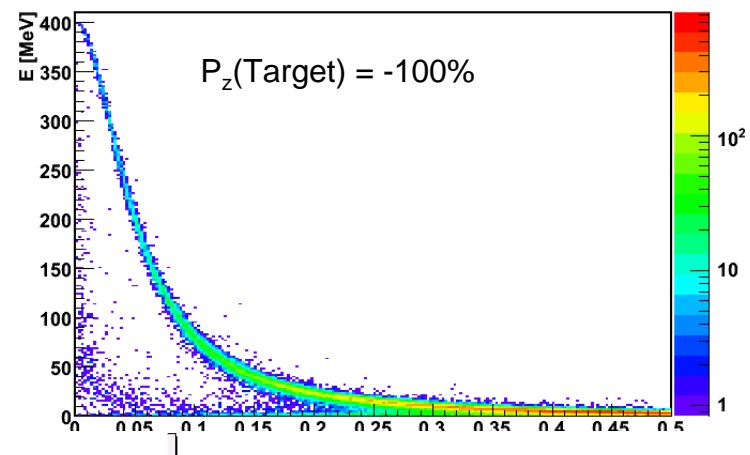
asymmetry (analyzing power)



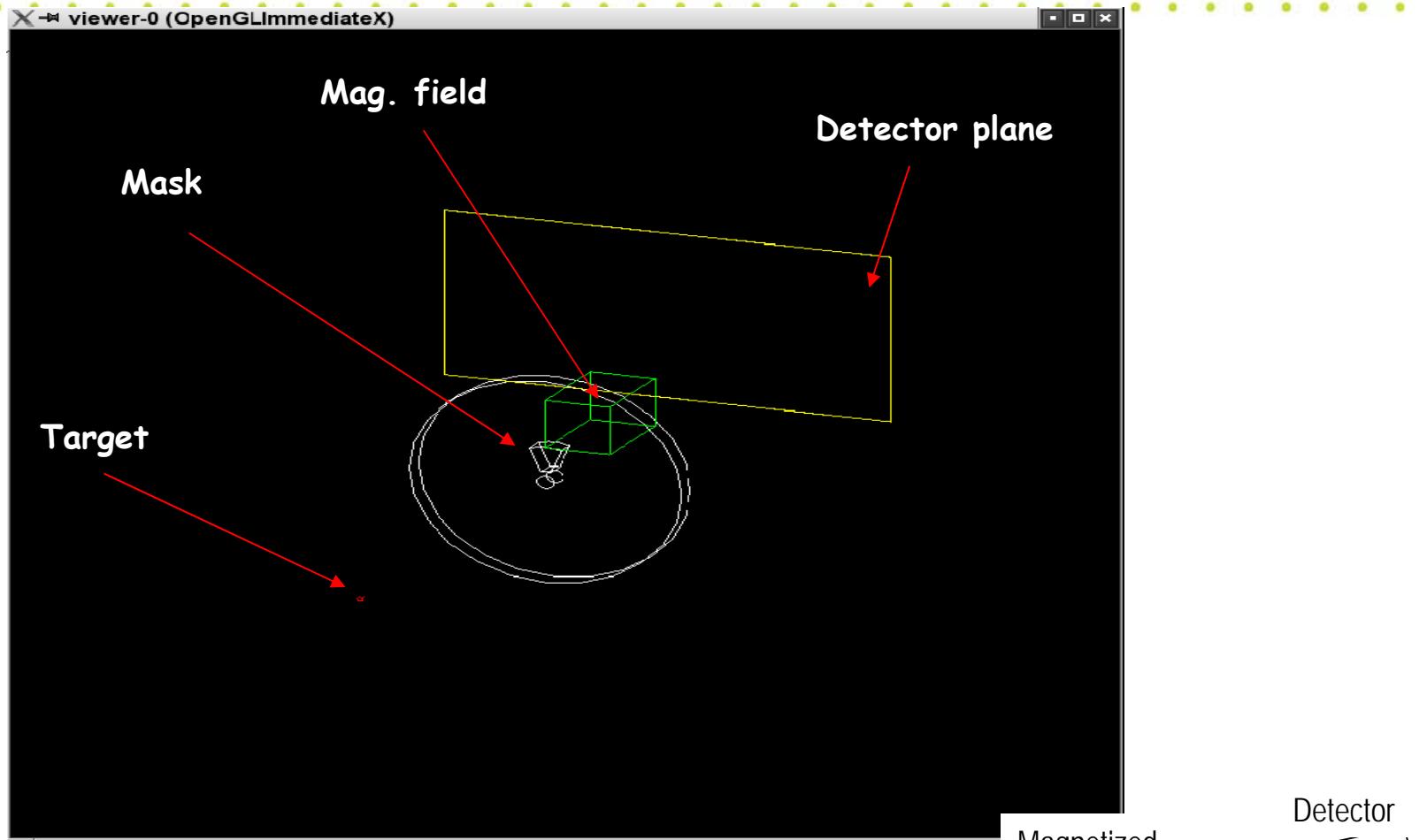
ang. range of interest: 0.03 – 0.1 rad

→ Asymmetry in the ang. range: $A_{e^-} \sim 50\%$ ($A_{e^+} \sim 5\%$, $A_\gamma \sim -15\%$)

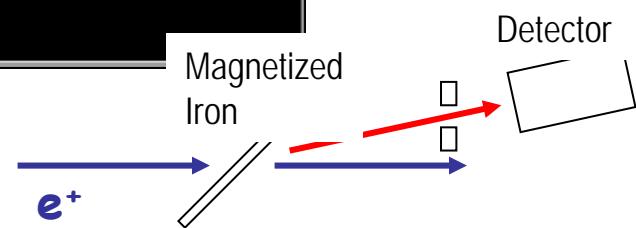
e⁻ distribution



Geometry



- detector ?
- mask ?
- magnet ?

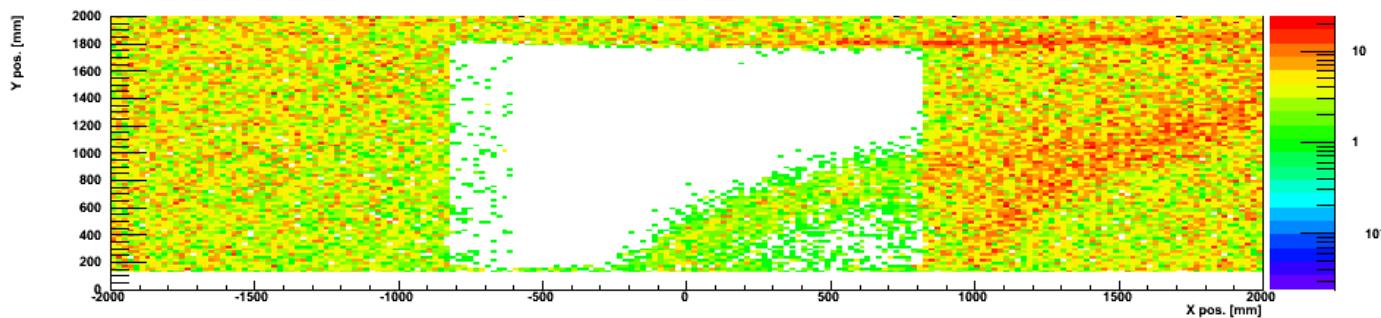


Detector plane, int. B-field 0.1 Tm

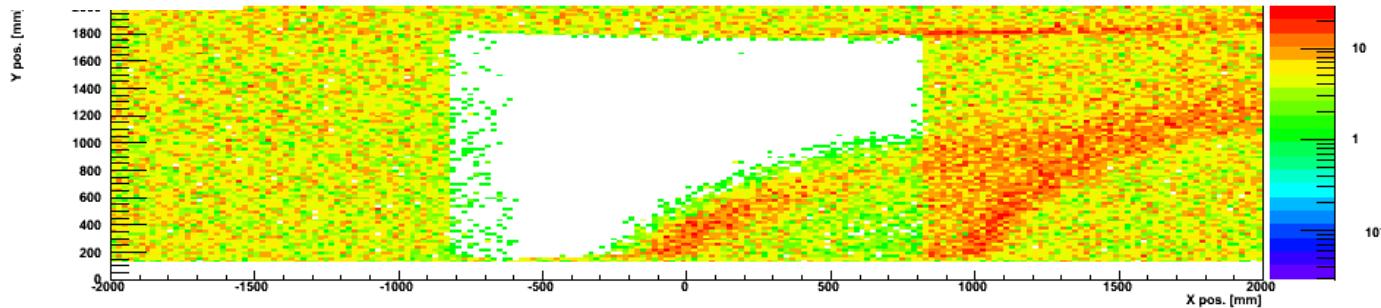
e⁻ distribution

Distance analyzing magnet – detector ~ 5m

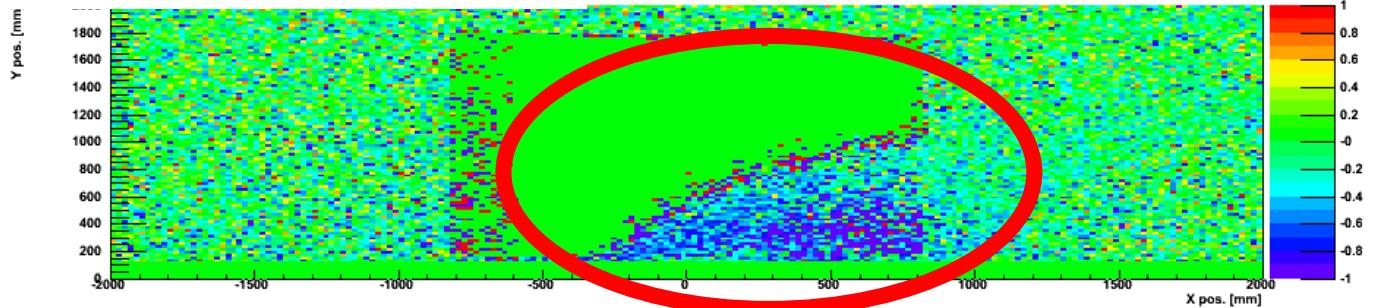
- run



+ run



asymmetry (analyzing power)



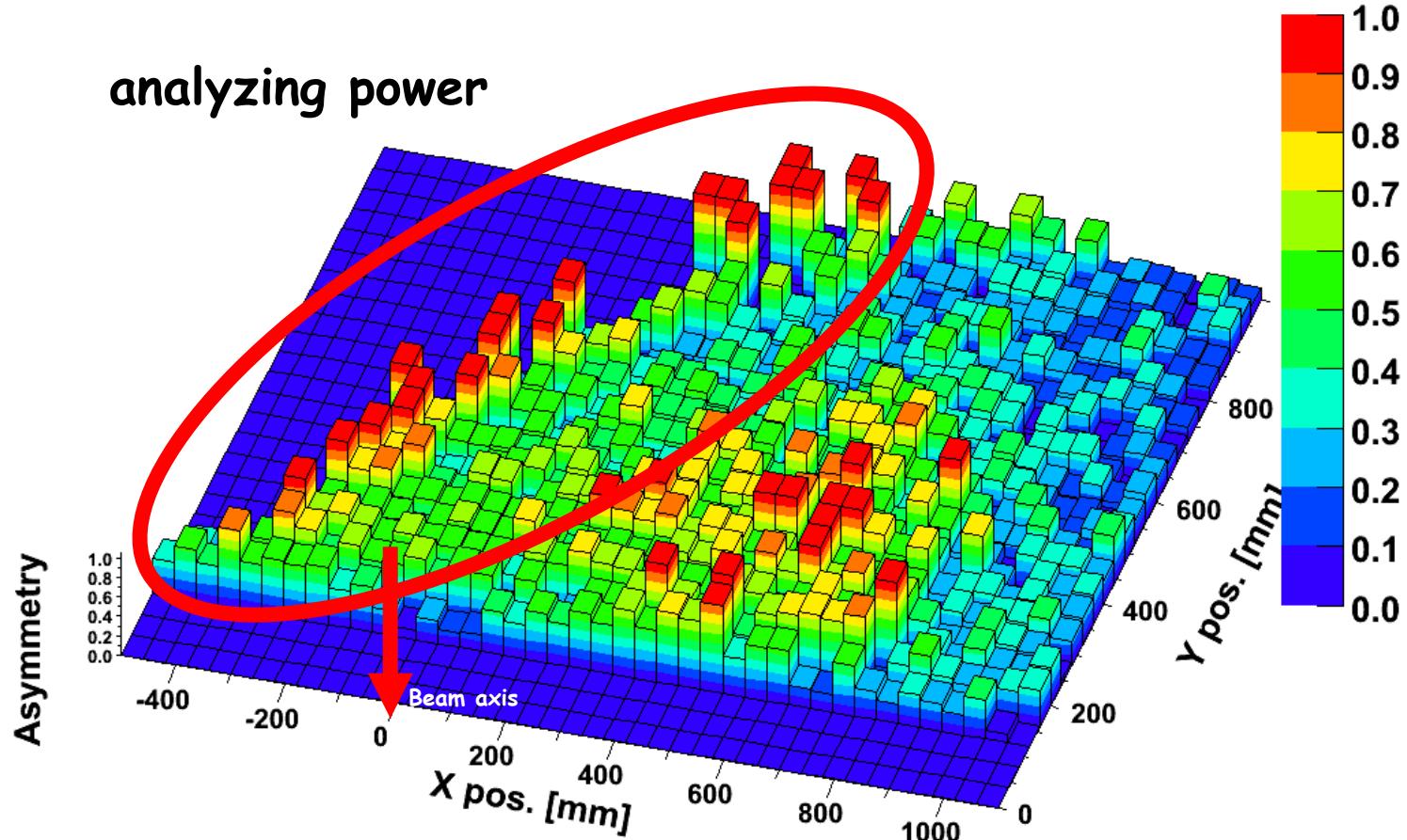
(beam: 1×10^9 e⁺, E: 400 MeV (10 % spread), ang spread: 0.5°)

e⁻ asymmetry in detector pads

Pad size: 4cm x 4cm

- run

analyzing power



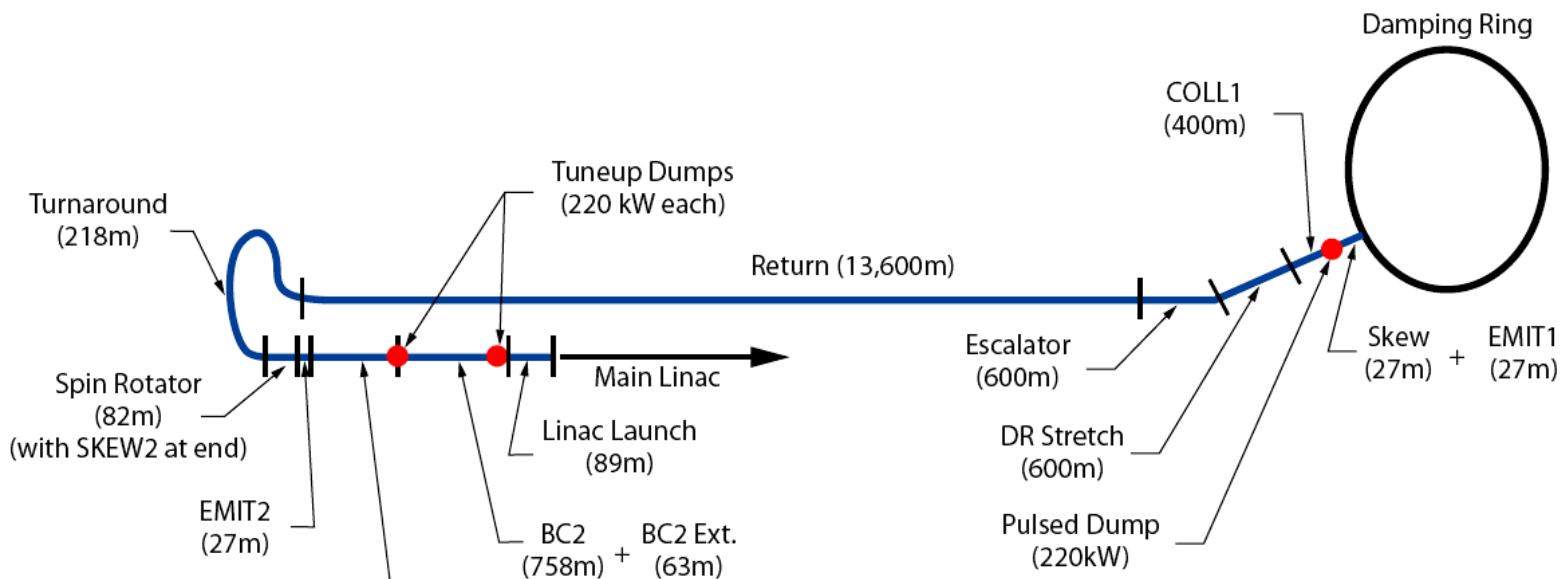
Compton Polarimetry after DR

Large e+ beam size → no Compton polarimetry before the DR

After DR: → small beam size, 5GeV,

→ transverse pol (DR...Turnaround)

→ ~longitudinal pol (spin rotation after turnaround)
taking into account earth curvature



Compton scattering on polarized lepton beam:

- Transverse polarization
 - **Asymmetry in scattered azimuthal distribution**
- longitudinal polarization
 - **asymmetry in energy distribution**
- Asymmetry measured using scattered photons
- Detection of e-, e+ more complicated, separation by chicane

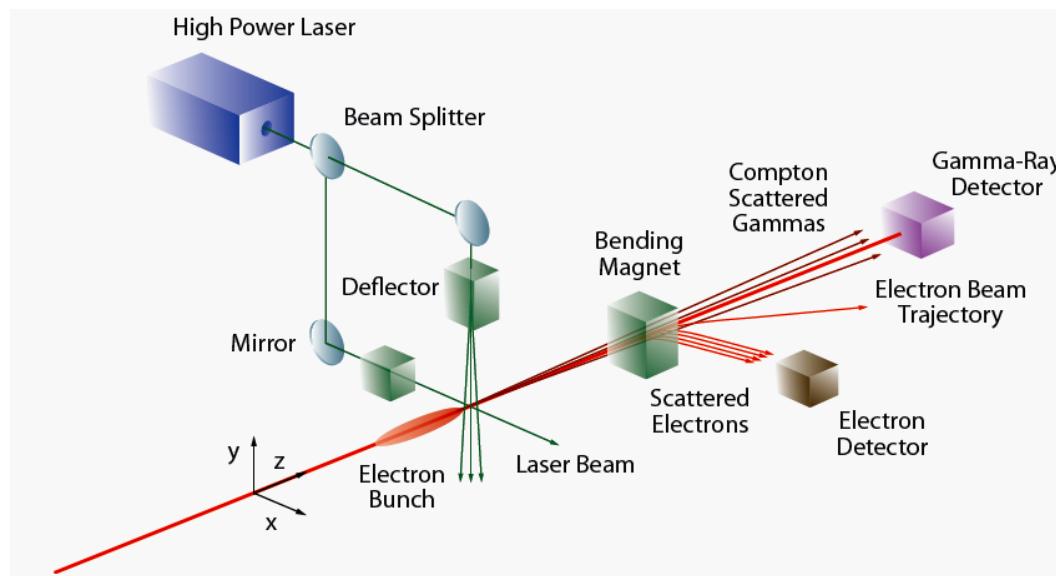
Needs:

- Large Rate (Rate = Lumi • cross section)
- ‘reasonable’ asymmetry

Could the laser wire be used??

Laser wire:

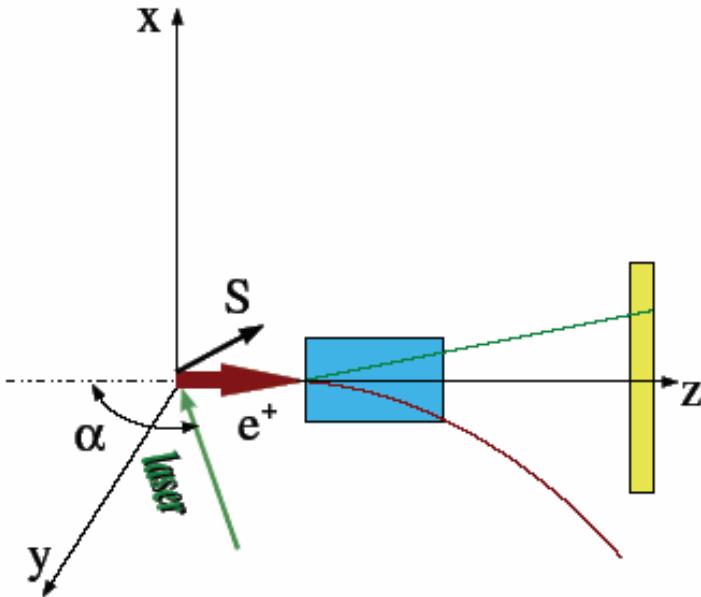
- $\pi/2$ crossing angle between e and γ
- e beam size larger than laser beam waist



'Normal' Compton crossing angle: π

Use of LW facilities for polarimetry ??

Done by P. Starovoitov



$$\gamma(k_1, \zeta) + e^+(k_2, s) \rightarrow \gamma(p_1) + e^+(p_2)$$

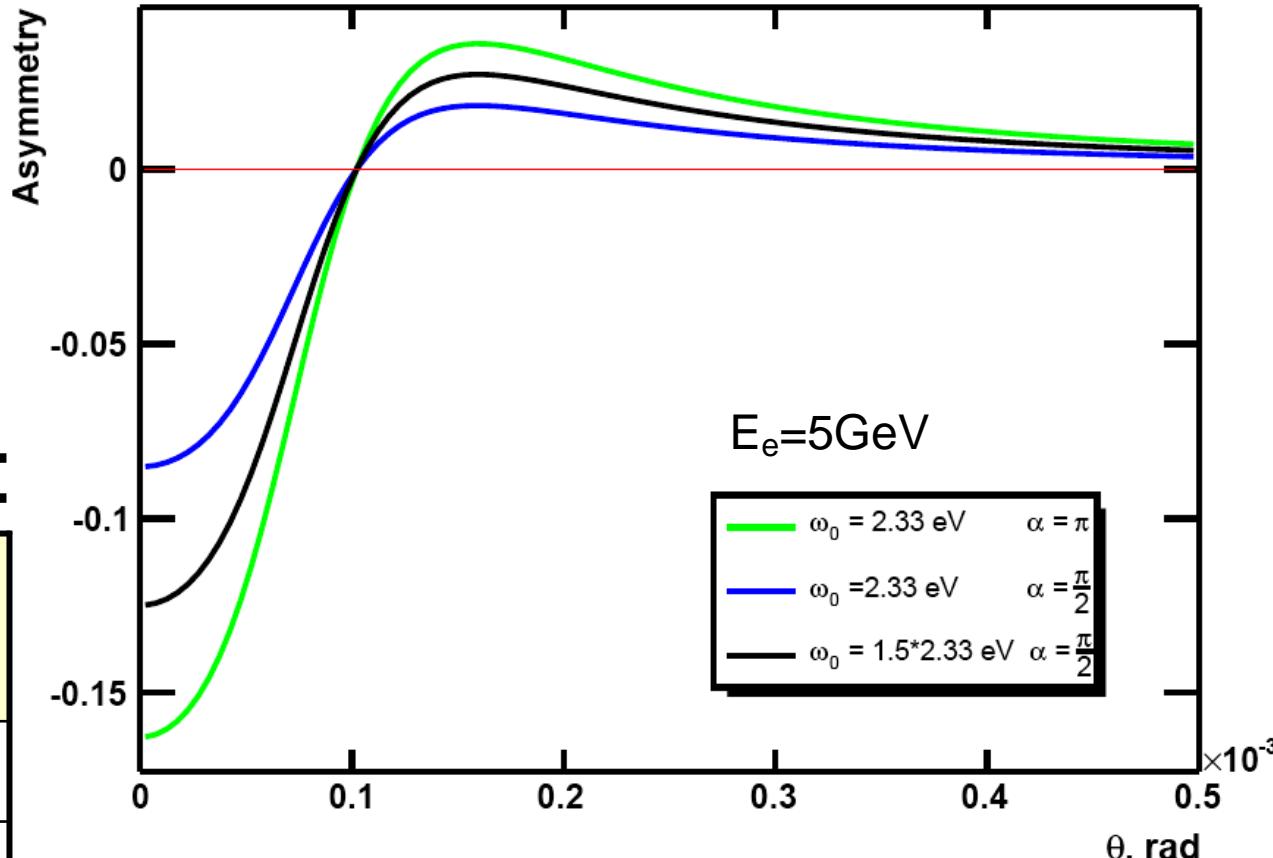
Laser energy: $\omega_0 = 2.33$ eV
Crossing angle: $0 < \alpha < \pi$
Positron energy: $E_0 = 5$ GeV
Positron spin: $\vec{S} = (s_1, s_2, s_3)$

- Asymmetry dependence on crossing angle α of laser and lepton beam
- Asymmetries for trans/long polarization

Longitudinal Positron Beam Polarization

Total asy [%]:

ω_0 [eV]	$\alpha = \pi/2$	$\alpha = \pi$
1.165	2	4
2.33	4	7.4
4.66	7.4	12



$2 \cdot A(\alpha = \pi/2) \sim A(\alpha = \pi)$

Total asy [%]:

ω_0 [eV]	$\alpha=\pi/2$	$\alpha=\pi$
1.165	1	2
2.33	2	3.7
4.66	3.7	6.5

$$A(\text{trans}) \sim 0.5 A(\text{long})$$

→ should measure with longitudinal polarized e+

Rough error estimate:

Assumptions: long. polarization

e-beam: $\sigma_x = 130\mu$ $\sigma_y = 6.5\mu$

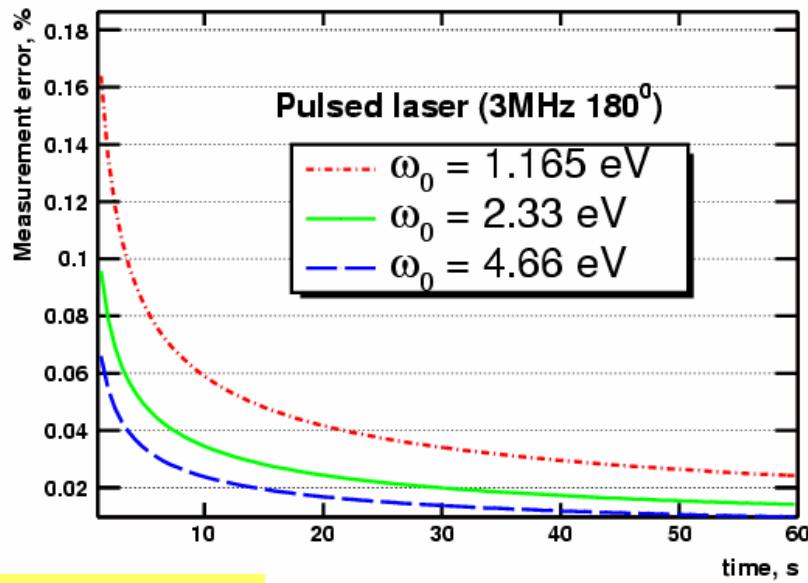
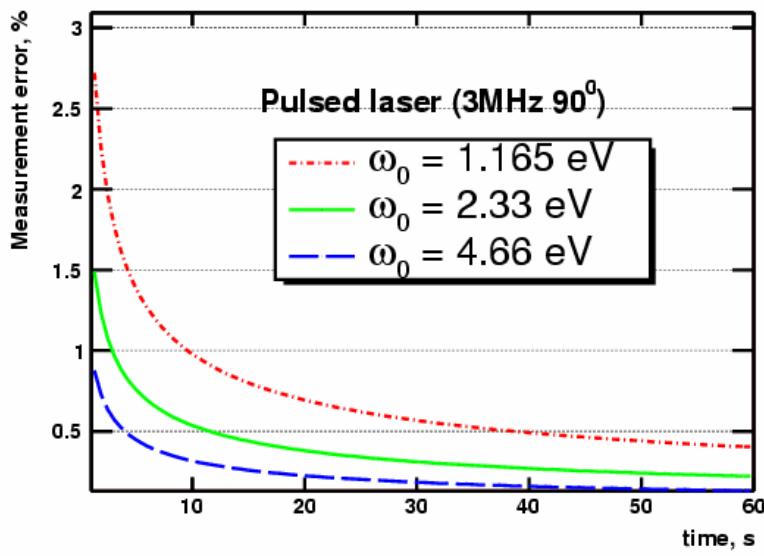
γ -beam: $\sigma_e \ll \sigma_\gamma$

100% efficiency

calorimeter: 10% / \sqrt{E}

Laser: 3MHz

ω_0 (eV)	λ (nm)	Energy (μJ)	Pulse (ps)	$\mathcal{L}\text{umi}$ ($\text{cm}^{-2}\text{s}^{-1}$)
1.66	1064	10	10	1.4×10^{31}
2.33	532	10	10	7.2×10^{30}
4.66	266	10	10	3.6×10^{30}



$$\Delta(\alpha=\pi/2) \approx 15 \cdot \Delta(\alpha=\pi)$$

e+ Compton Polarimetry after DR (~turnaround) is an option

Summary & Conclusion

- machine will be polarized
 - consequences for design:
≥30% e+ polarization have to be kept
 - interaction with IP (polarimeter, physics):
 - frequency of helicity reversal,
 - stability of intensity and polarization
- Tools for design/performance studies:
 - G4 with polarization extension:
 - validation,
 - spin tracking,
 - transverse pol.
- e+ polarimeter:
 - Bhabha (~400 MeV),
 - Compton (5GeV, long polarization)
 - Further studies in cooperation with machine and Lw people