



# Photoinjector Beam Dynamics Simulation Using an Improved Quasi-Static Model

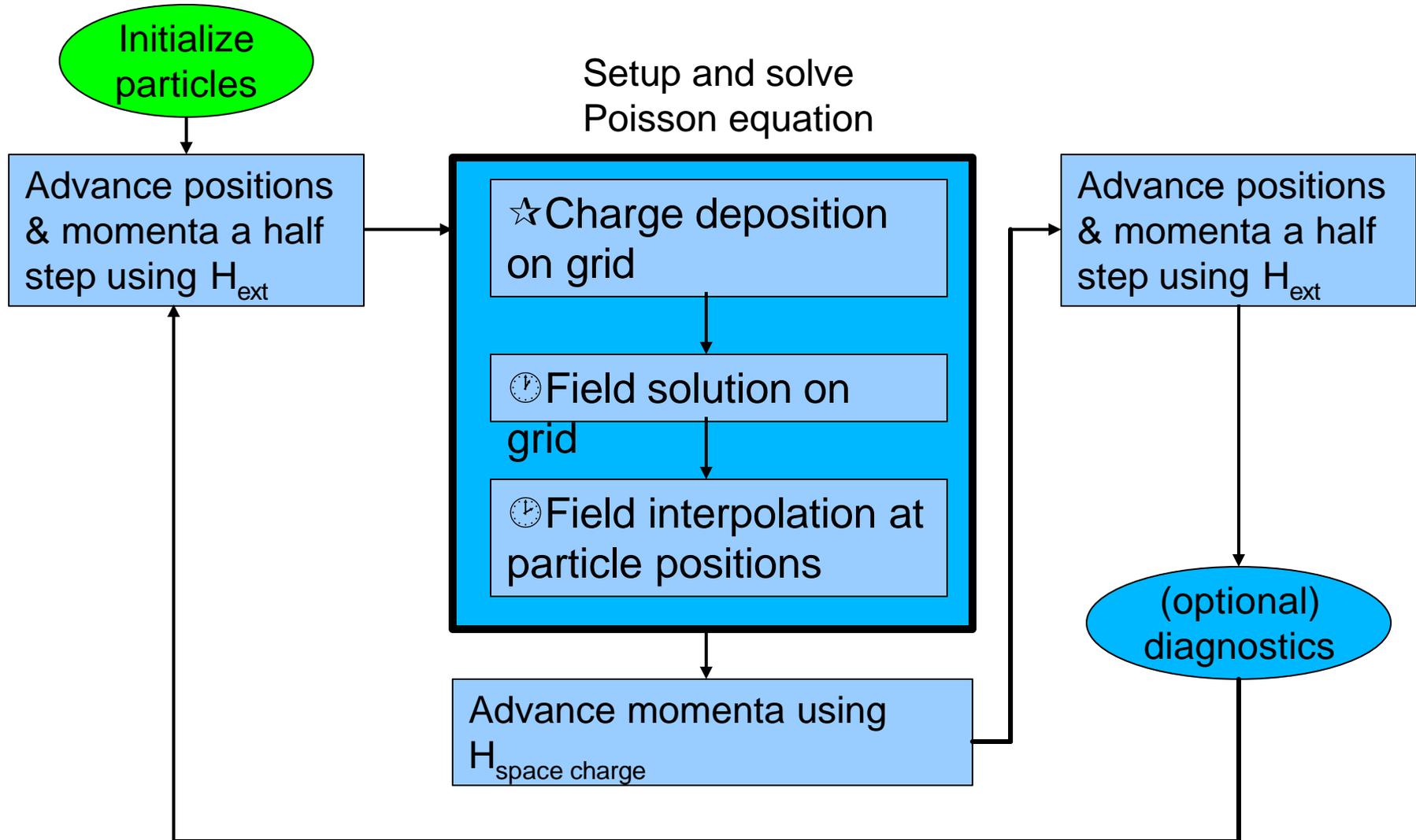
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**DOE Advanced Computing for 21st Century Accelerator Science and  
Technology Project** using resources at the  
**Center for Computational Sciences and the  
National Energy Research Scientific Computing Center**

# Particle-In-Cell (PIC) Simulation



# Green Function Solution of Poisson's Equation



$$\mathbf{f}(r) = \int G(r, r') \mathbf{r}(r') dr' ; r = (x, y, z)$$

$$\mathbf{f}(r_i) = h \sum_{i'=1}^N G(r_i - r_{i'}) \mathbf{r}(r_{i'})$$

$$G(x, y, z) = 1 / \sqrt{(x^2 + y^2 + z^2)}$$

Direct summation of the convolution scales as  $N^6$  !!!!  
 $N$  – grid number in each dimension

Hockney's Algorithm:- scales as  $(2N)^3 \log(2N)$

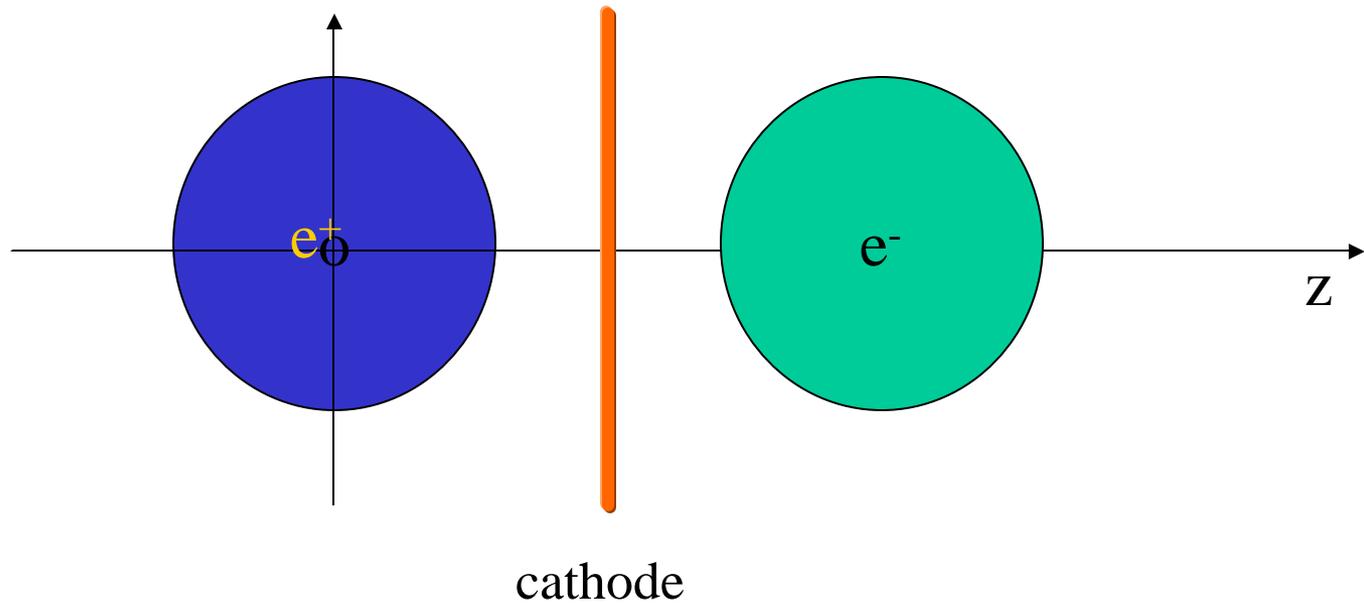
- Ref: Hockney and Easwood, *Computer Simulation using Particles*, McGraw-Hill Book Company, New York, 1985.

$$\mathbf{f}_c(r_i) = h \sum_{i'=1}^{2N} G_c(r_i - r_{i'}) \mathbf{r}_c(r_{i'})$$
$$\mathbf{f}(r_i) = \mathbf{f}_c(r_i) \quad \text{for } i = 1, N$$

Shifted Green function Algorithm:

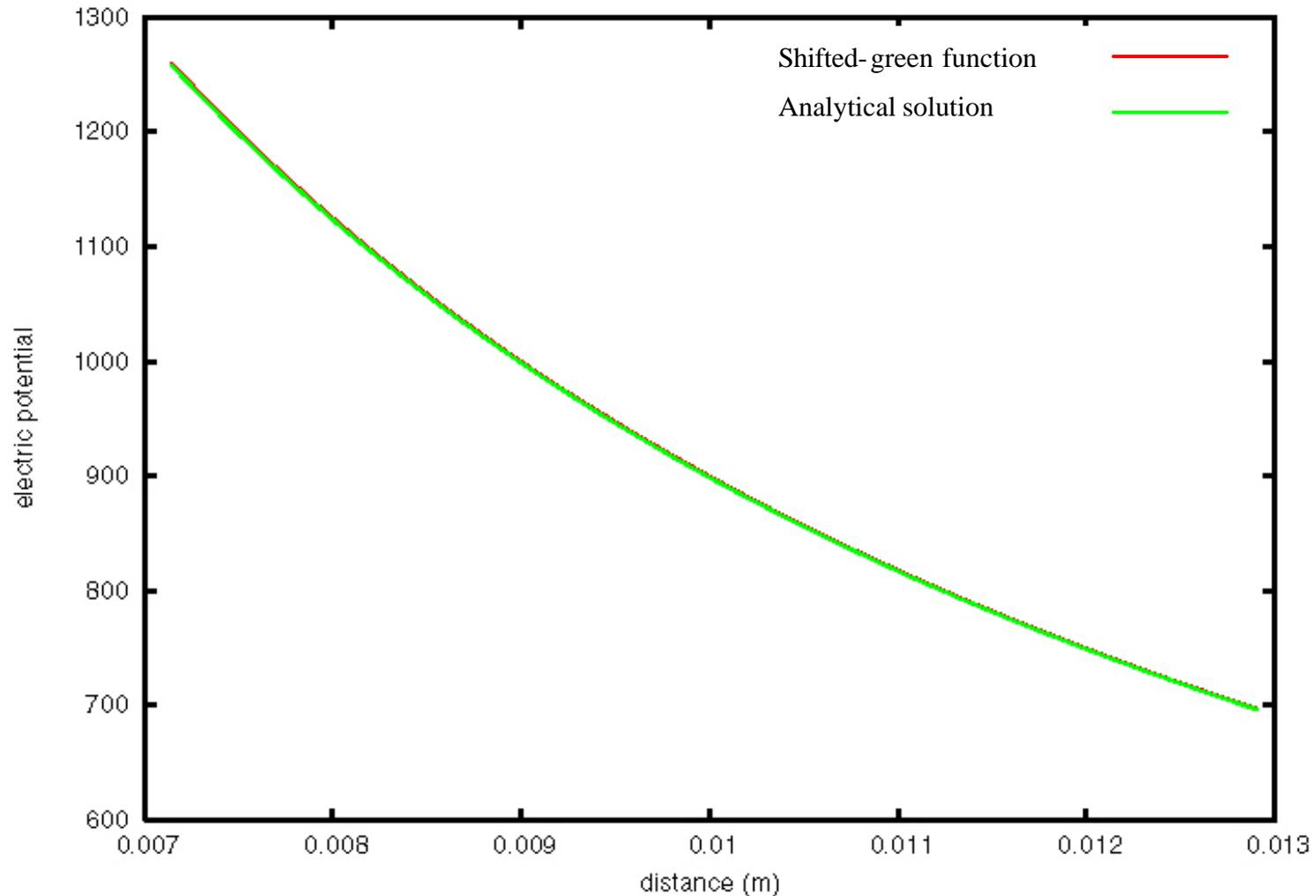
$$\mathbf{f}_F(r) = \int G_s(r, r') \mathbf{r}(r') dr'$$
$$G_s(r, r') = G(r + r_s, r')$$

# A Schematic Plot of an $e^-$ Beam and Its Image Charge



# Test of Image Space-Charge Calculation

## Numerical Solution vs. Analytical Solution

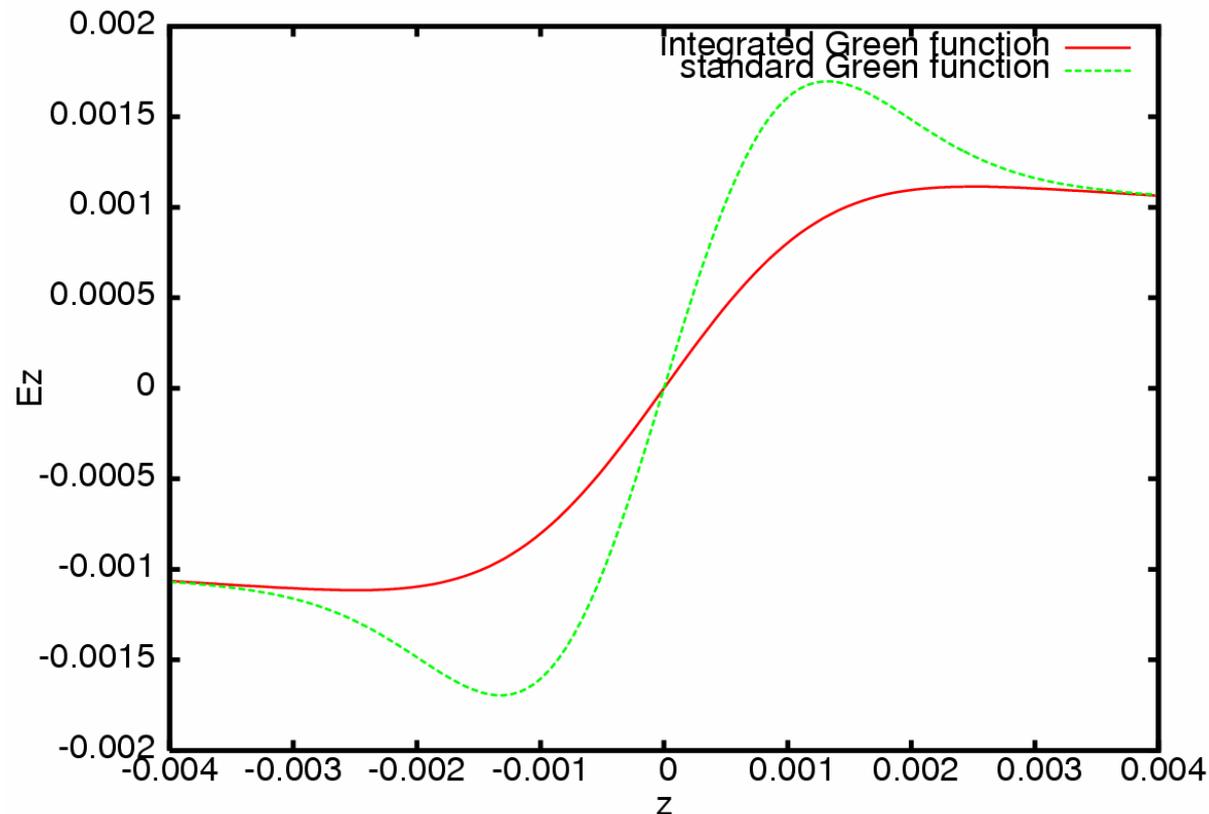


# Integrated Green Function Solution of Poisson's Equation



$$\mathbf{f}_c(r_i) = \sum_{i'=1}^{2N} G_i(r_i - r_{i'}) \mathbf{r}_c(r_{i'})$$

$$G_i(r, r') = \oint G_s(r, r') dr'$$

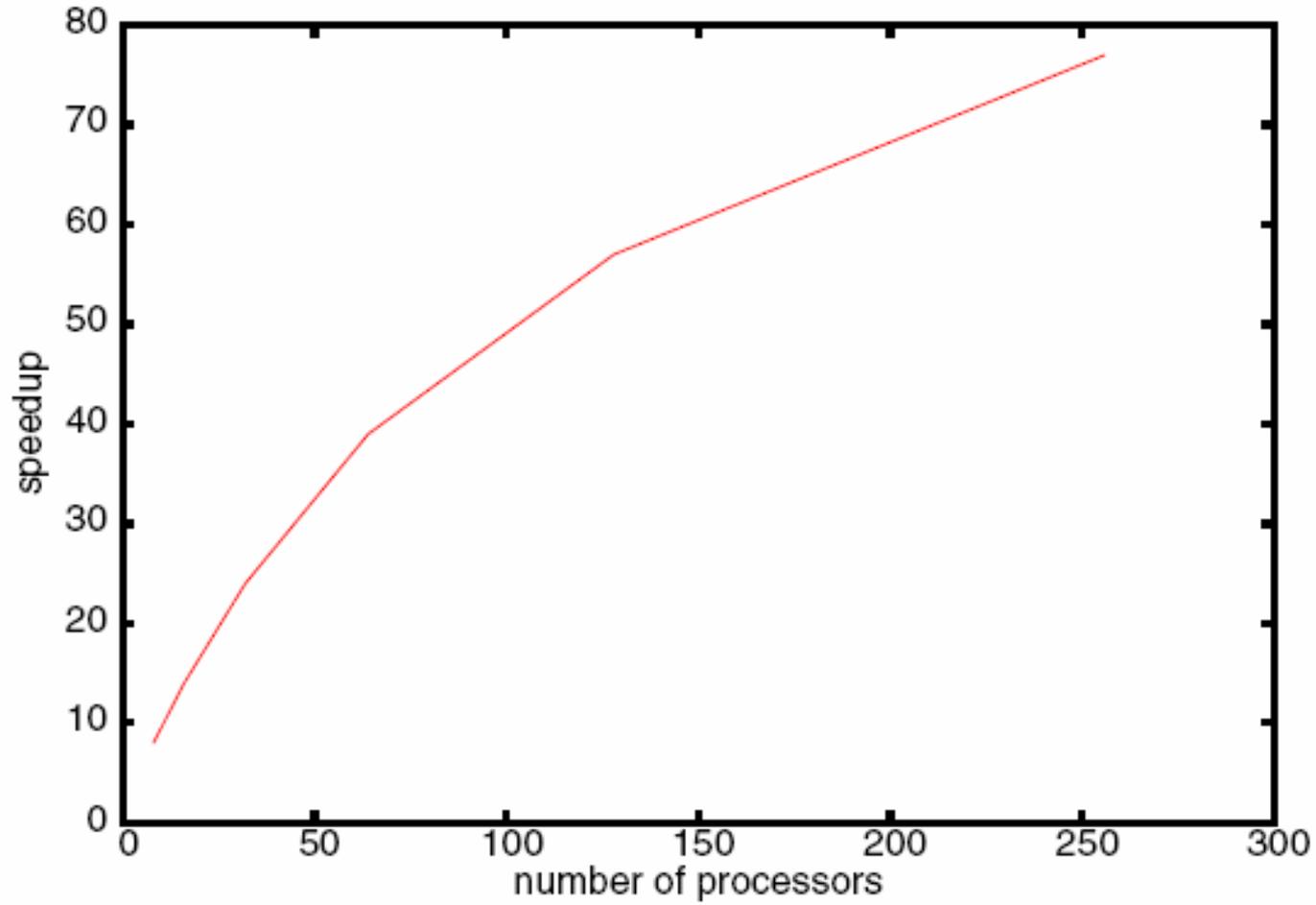


# The IMPACT-T code

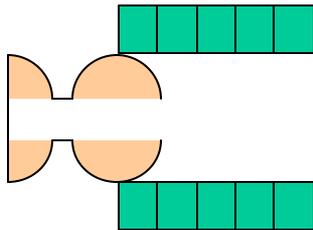
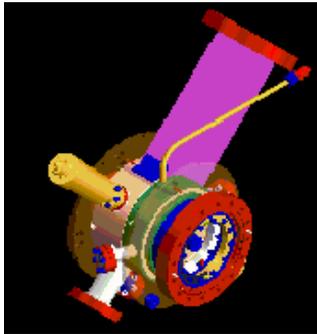


- 3D Integrated Green method to accurately compute the space-charge forces for a beam with large aspect ratio
- 3D Shifted Green method to efficiently compute the space-charge forces from the image charge
- Multiple slices/bins to handle the beam with large energy spread
- Arbitrary overlap of external fields to allow the modeling of both standing wave and traveling wave structure
- Transverse and longitudinal wakefield effects included (in testing)
- Parallel implementation on high performance computer to allow multiple million, high resolution simulation

# Speed up of the IMPACT-T code vs. Number of Processors

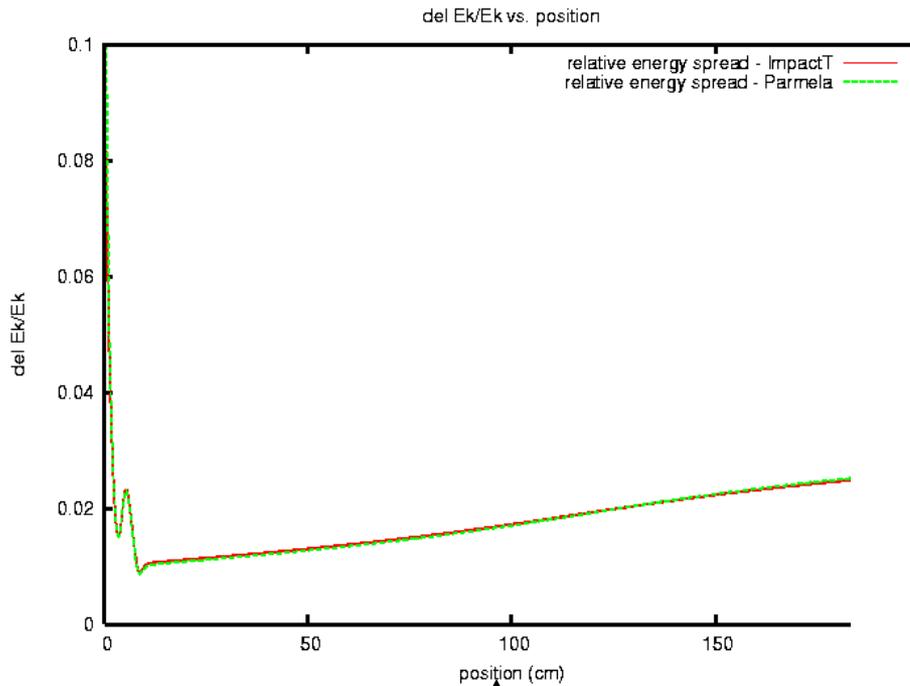


# A Benchmark Example



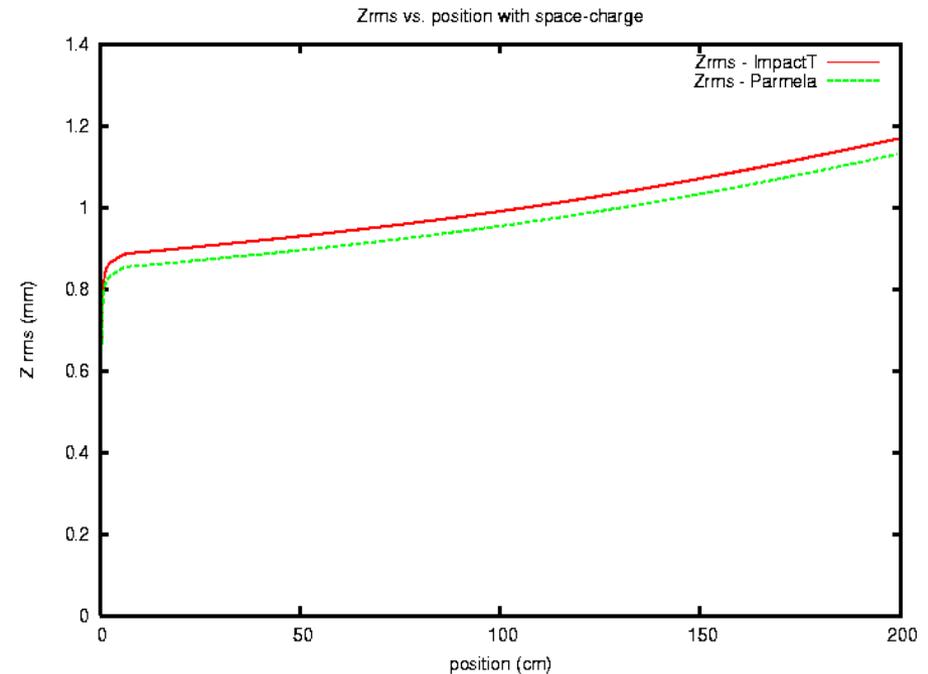
1nC  
10ps square pulse,  
1 mm uniform transverse  
laser pulse  
No Thermal emittance  
110MV/m  
Solenoid 2.541 kG

# Zrms and Relative Energy Spread vs. Position

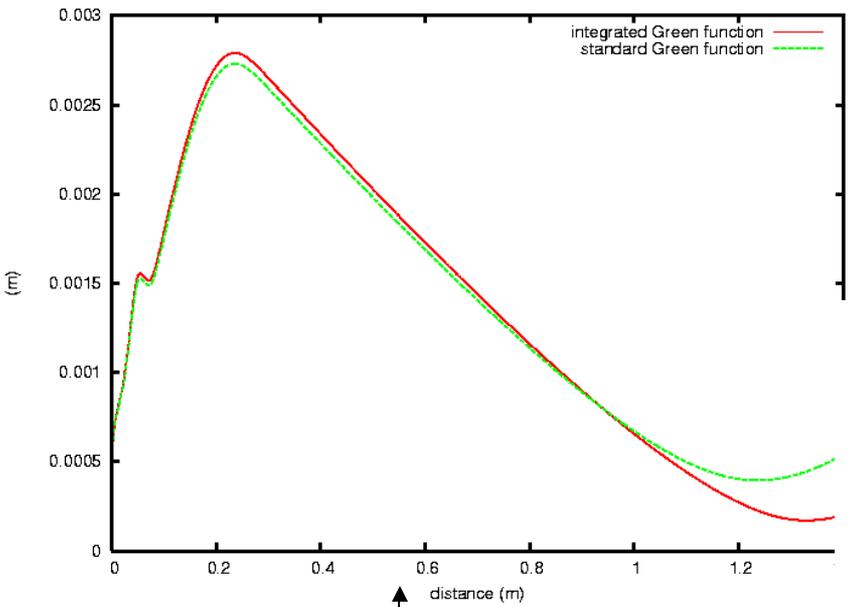


rms energy spread

longitudinal rms size

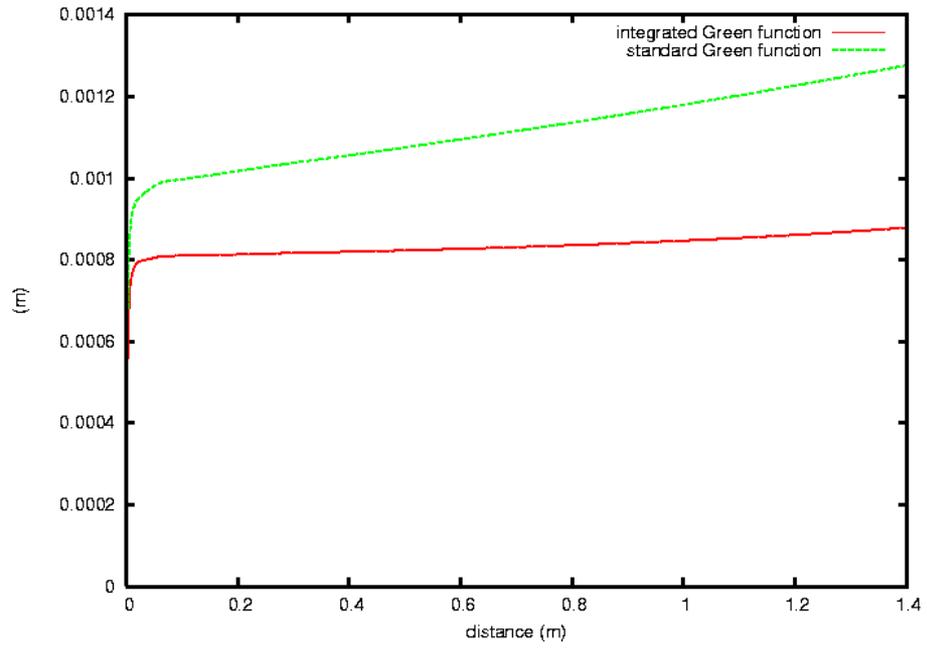


# Xrsm vs. Distance with Integrated Green Function and Standard Green Function for Space-Charge Forces Calculation

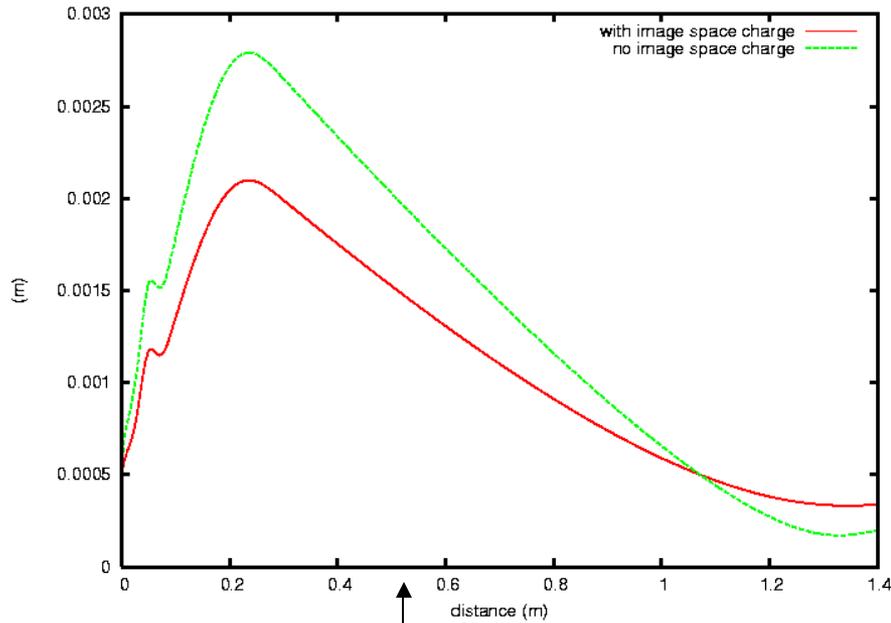


transverse

longitudinal

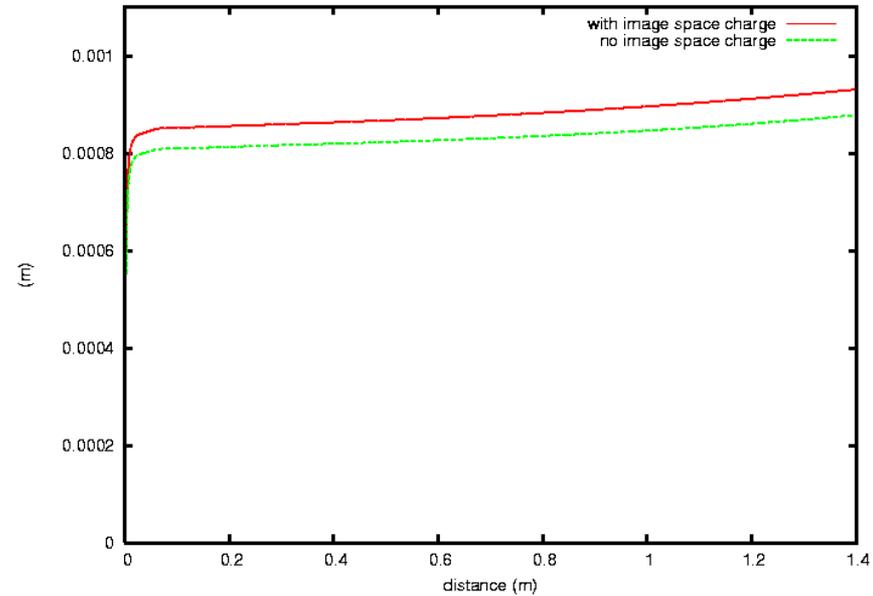


# Xrsm vs. Distance with/without Image Charge Effect of Cathode

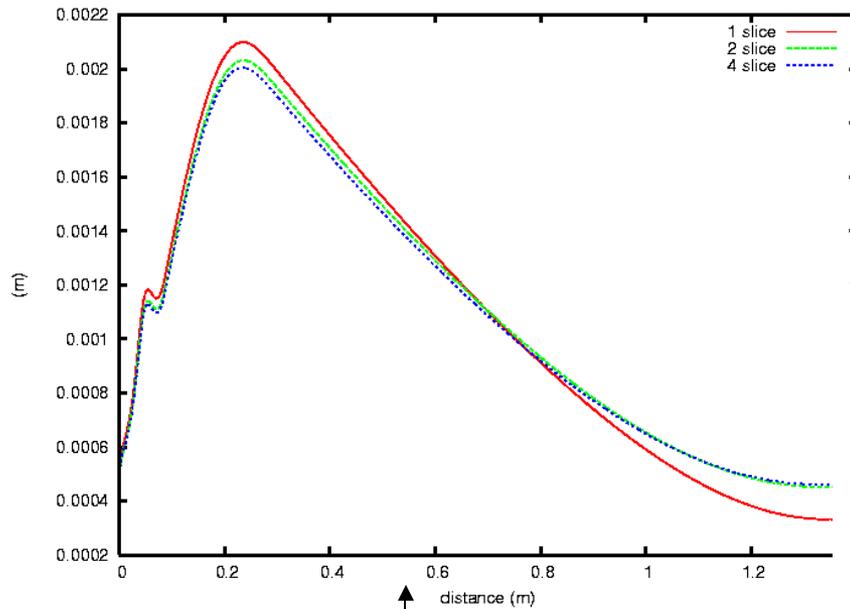


transverse

longitudinal

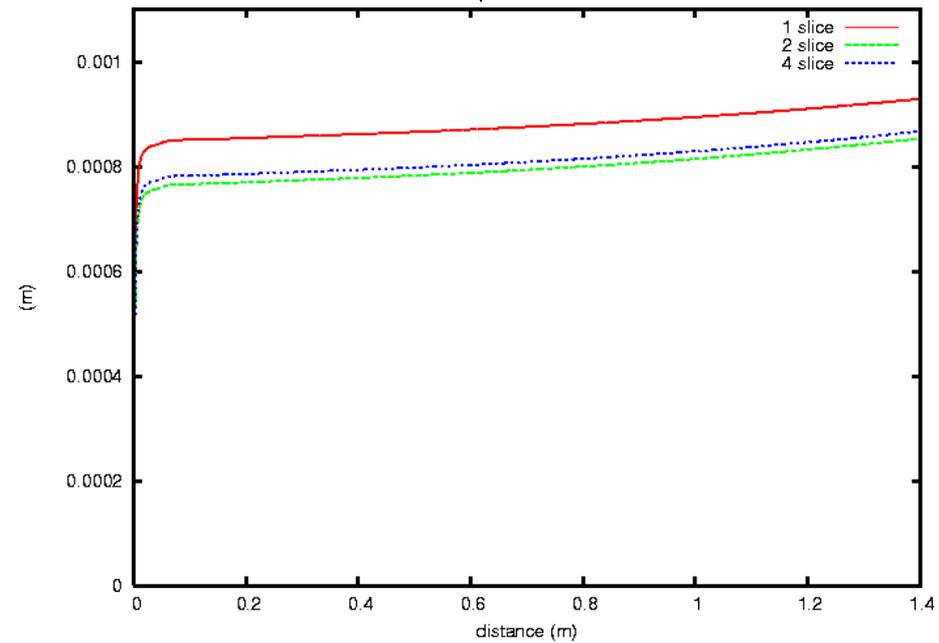


# Transverse and Longitudinal RMS Size with 1, 2, and 4 Slices

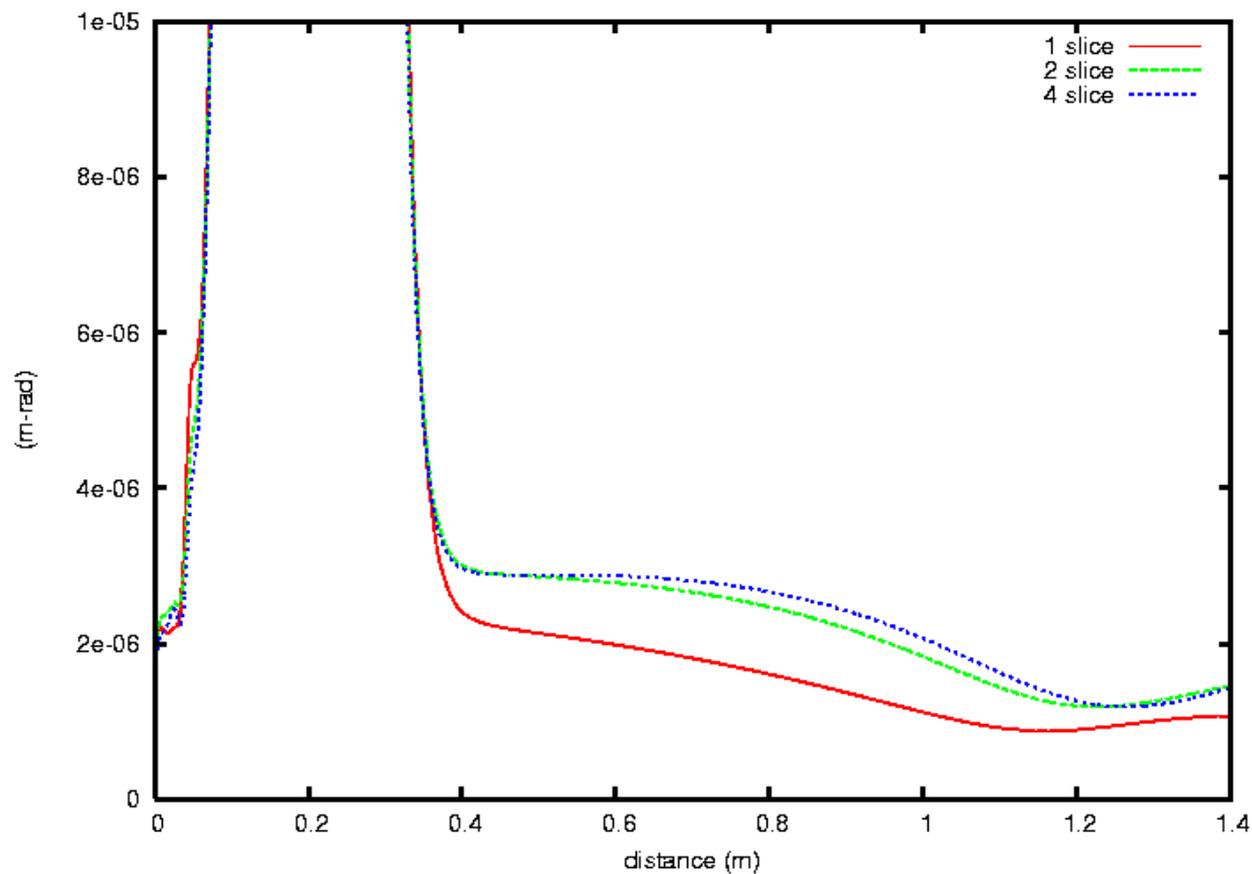


transverse

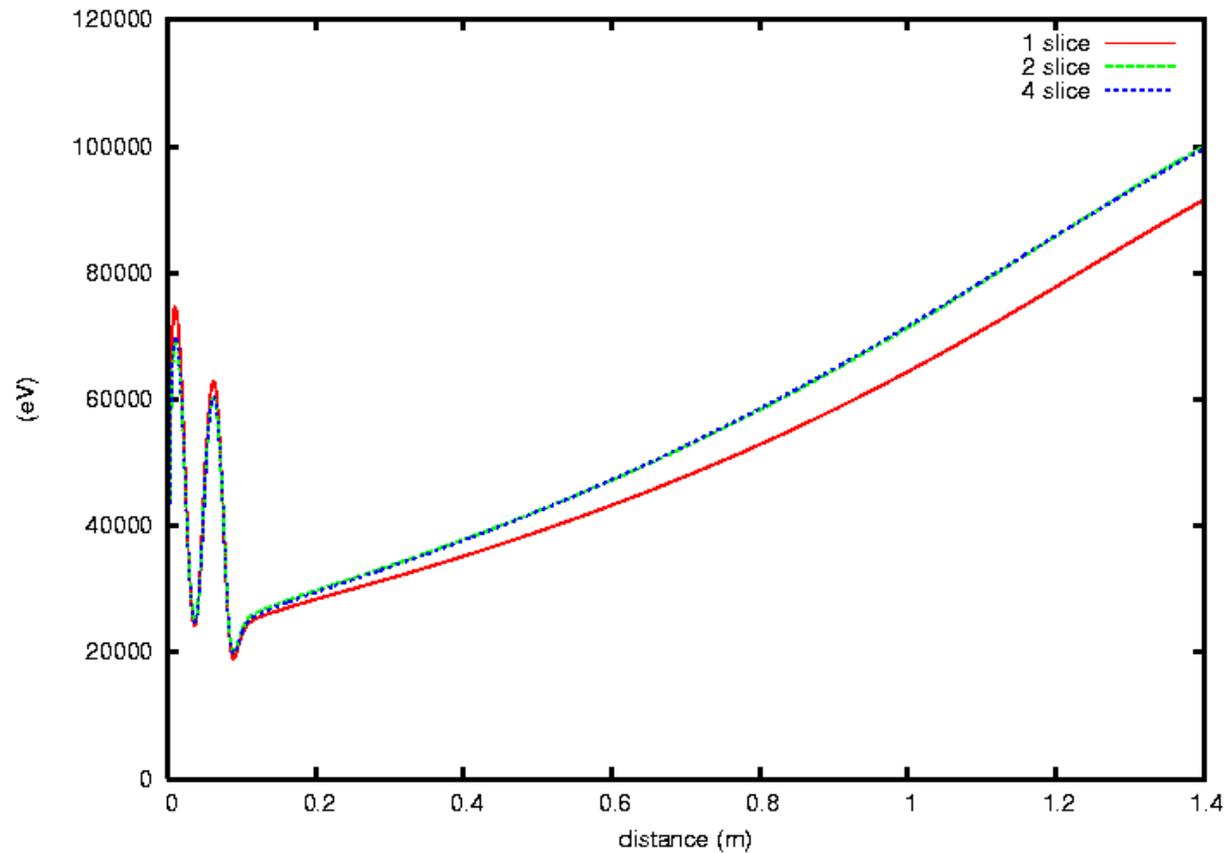
longitudinal



# Transverse RMS Emittance with 1, 2, and 4 Slices

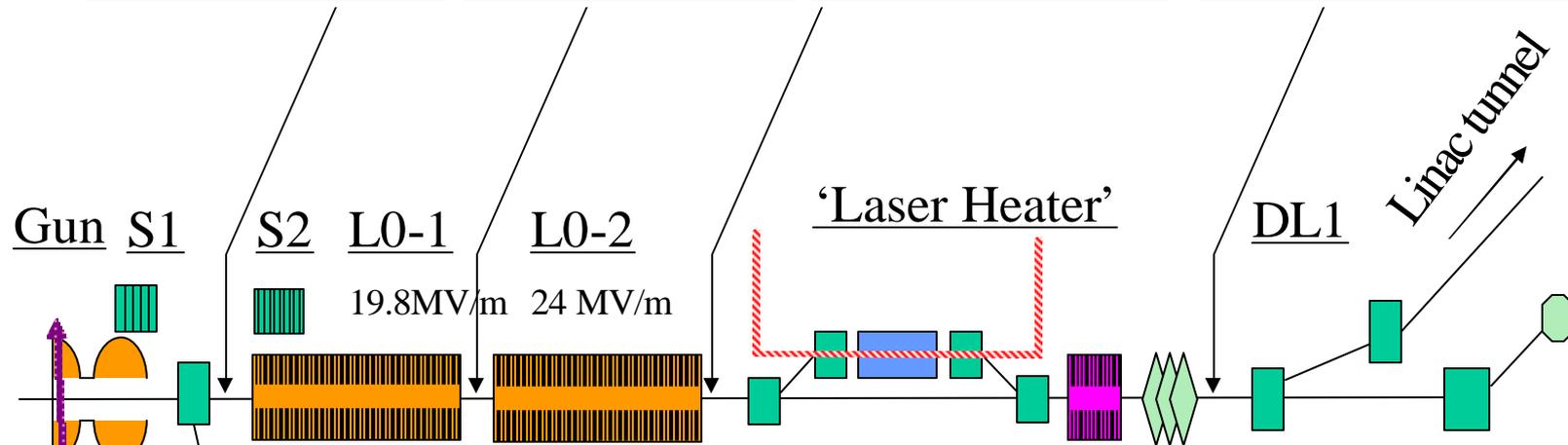


# Correlated RMS Energy Spread with 1, 2, and 4 Slices



# A Schematic Plot of LCLS Injector Layout

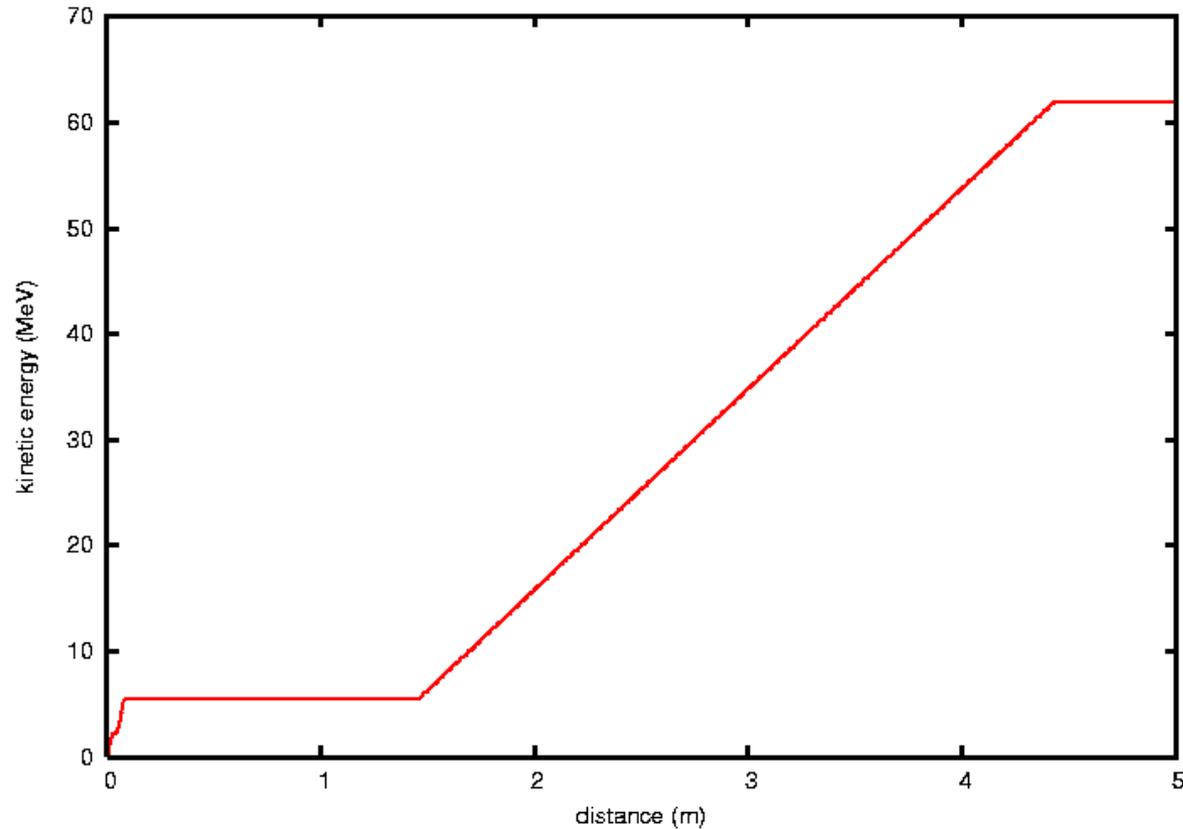
6 MeV $\epsilon = 1.6 \mu\text{m}$ $\sigma_{\delta,un.} = 3\text{keV}$	63 MeV $\epsilon = 1.08 \mu\text{m}$ $\sigma_{\delta,un.} = 3\text{keV}$	135 MeV $\epsilon = 1.07 \mu\text{m}$ $\sigma_{\delta,un.} = 3\text{keV}$	135 MeV $\epsilon = 1.07 \mu\text{m}$ $\sigma_{\delta,un.} = 40\text{keV}$
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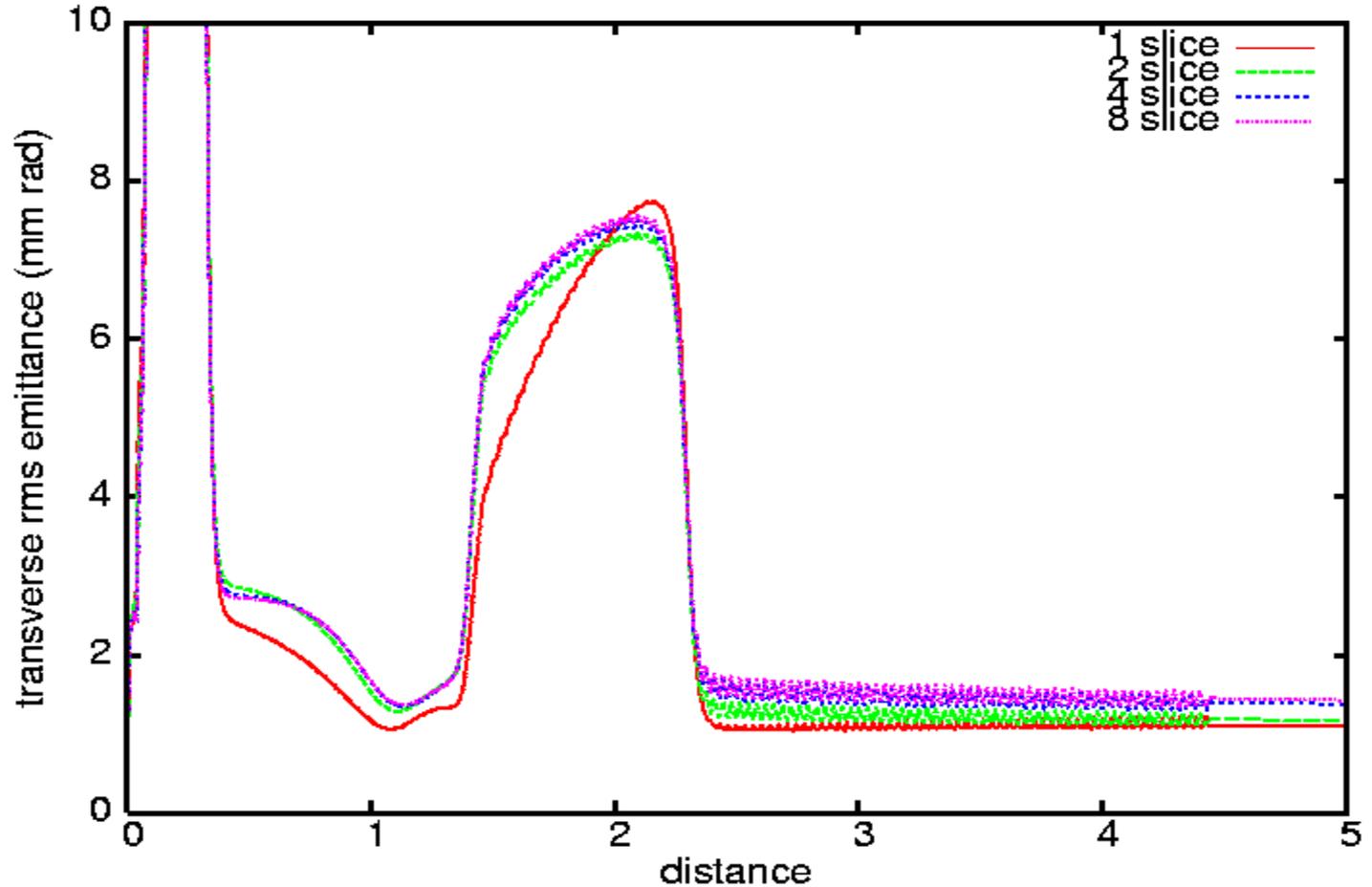
UV Laser 200  $\mu\text{J}$ ,  
 $\lambda = 255 \text{ nm}$ , 10ps,  $r = 1.2 \text{ mm}$

Peak Current	100 A
Charge	1 nC
$\epsilon_{\text{projected}}, \epsilon_{\text{slice}}$	$\leq 1.2, 1 \mu\text{m}\cdot\text{rad}$
Repetition rate	120 Hz

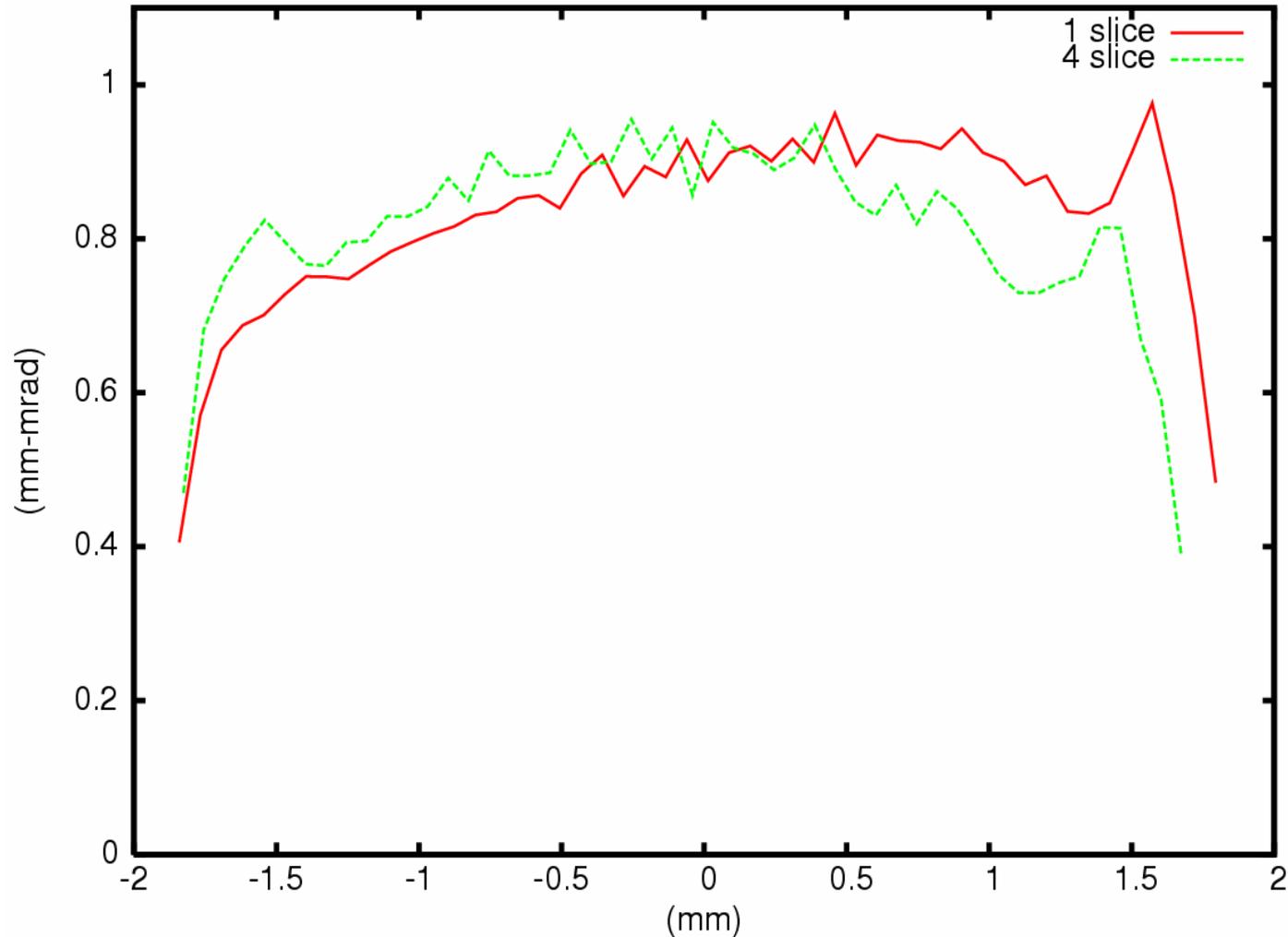
# Kinetic Energy vs. Distance at LCLS Injector



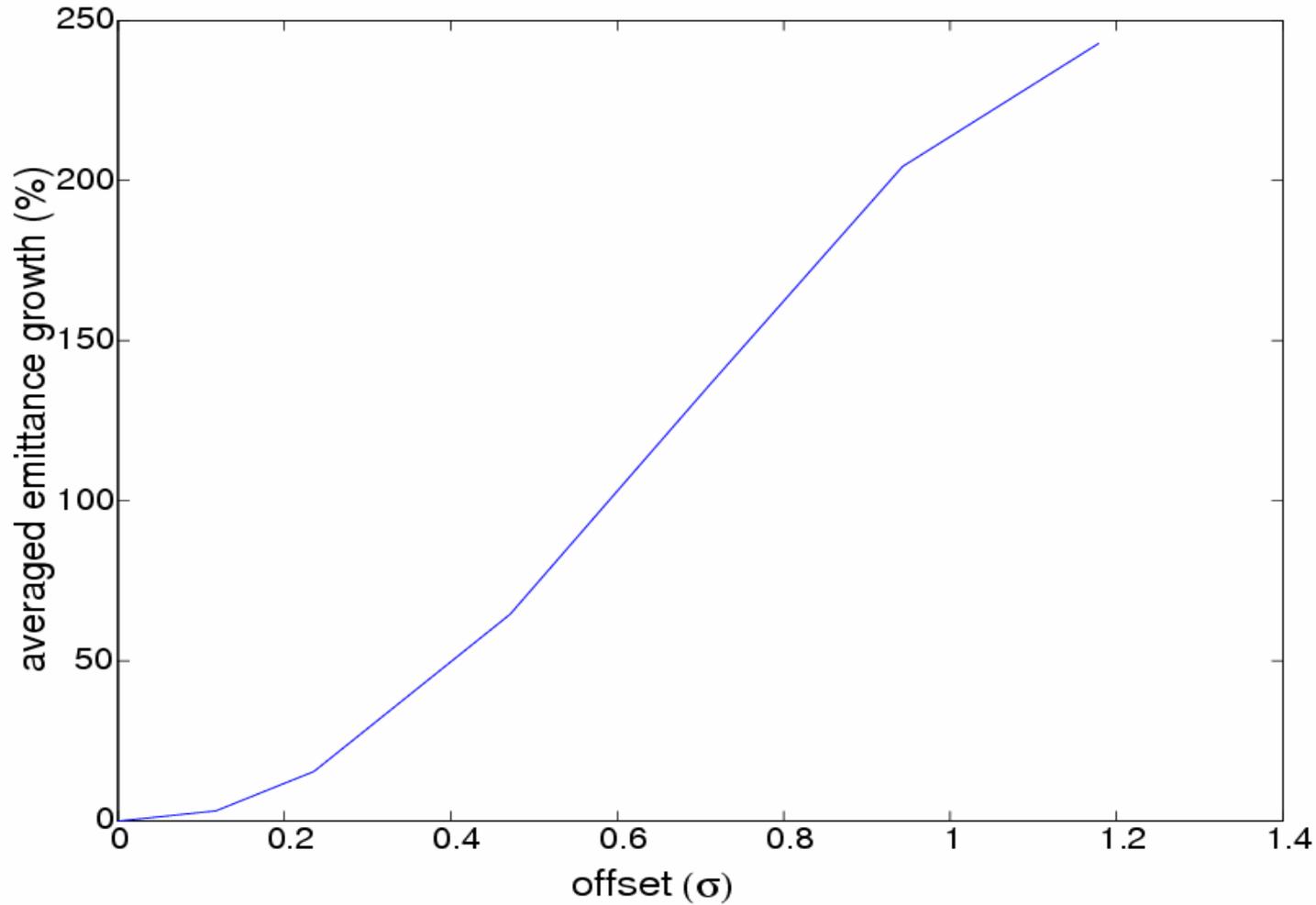
# Transverse Projected RMS Emittance vs. Distance with Different Longitudinal Slices



# Transverse Sliced Emittance after the L0-1 with Different Longitudinal Slices



# Emittance Growth after L0-1 vs. Initial Offset



# Acknowledgements



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